



# Higgs in BSM models

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Tohoku Forum for Creativity  
– Particle Physics and Cosmology after the discovery of a Higgs boson –  
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# Introduction

## What is the Higgs?

It couples to all particles

It gets a VEV ( $v$ ) by EWSB (scalar field)

Higgs mechanism

$$m_W = g v$$

Yukawa interaction

$$m_{q,l} = Y_{q,l} v$$

Dimension 5 operator  
(neutrino mass)

$$m_\nu = C_\nu v^2/M$$

**Higgs = Origin of Mass**

# In 2012 July, a boson was found

The mass is 126 GeV

Spin/Parity  $0^+$

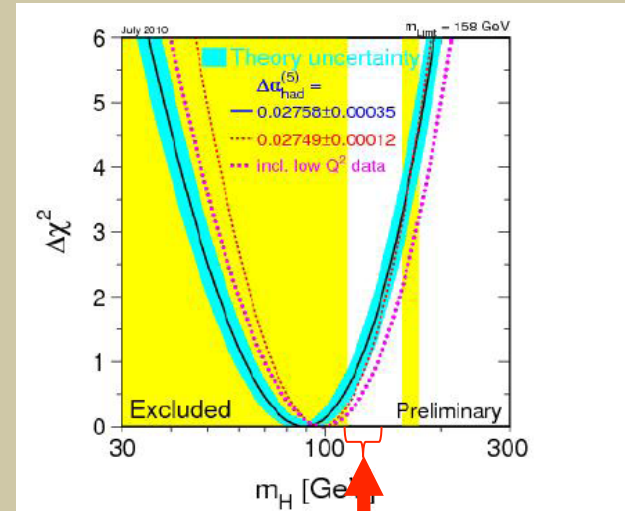
It couples to  $\gamma\gamma, WW, ZZ, bb, \tau\tau, \dots$

This is really a Higgs!

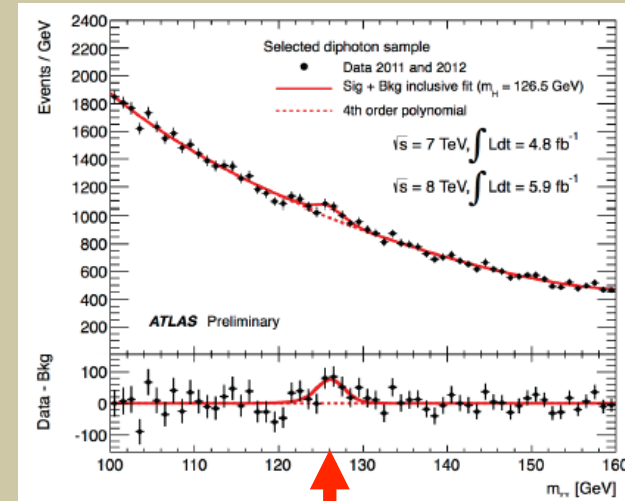


Measured Couplings look consistent with the SM Higgs

Why SM-like???



Higgs Mass indicated by LEP/SLC



ATLAS/CMS July 2012

New Particle !

# Introduction

Minimal Form

Standard Model Higgs Sector:

One  $SU(2)$  doublet  $\Phi$

$$V(\Phi) = +\mu^2 |\Phi|^2 + \lambda |\Phi|^4$$

Assumption of  $\mu^2 < 0 \Rightarrow$  EWSB

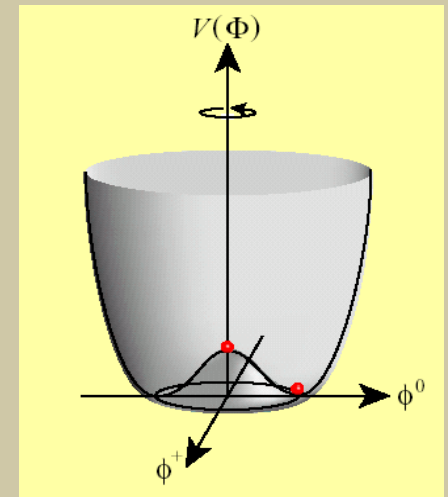
This is simple but ...

Question:

Why **minimal?** (no principle)

Why  $\mu^2 < 0$

What is Origin of the **Higgs force  $\lambda$** ?



Higgs sector = Window for new physics

# Introduction

## Second Higgs boson?

**SM Higgs sector = just a guess!**

No principle for the minimal Higgs sector of the SM

Many possibilities for **non-minimal** Higgs sectors

These extended Higgs sectors can provide source for

- Baryogenesis (CP violation/1st Order Phase Transition)
- Dark Matter
- Neutrino Mass

**Higgs sector = Window for new physics**

# Introduction

Scalar field is problematic

Problem of quadratic divergences

**Hierarchy problem**

Ideas of new physics to solve the problem

- Supersymmetry
- Dynamical Symmetry Breaking (Technicolor)
- Little Higgs mechanism
- Extra Dimensions
- ...

Many of these NP models predict specific extended Higgs sectors

**Higgs sector = Window for new physics**

$$\delta m_H^2 = \frac{\Lambda_{cutoff}^2}{16\pi^2}$$

# Introduction

Higgs is important not only for **EWSB** but also as a **window** to new physics beyond SM

Discovery of a **Higgs boson**:

Great step to construct the Higgs sector  
and to understand the essence of the Higgs field

From the detailed study of the Higgs sector, we can  
determine models of **new physics**

**New era has started !**

# Beyond the **S**tandard **M**odel

There are many reasons to consider New Physics of BSM

## Unification of Law

- Paradigm of Grand Unification
- Yukawa structure (flavor physics)

## Problem in the SM Higgs

- Hierarchy Problem

## BSM Phenomena

- Dark Matter
- Neutrino mass and mixing
- Baryon Asymmetry of Universe
- Inflation, Dark Energy, Gravity,...

New Physics is necessary

At which scale?

If TeV scale, they should have connection with Higgs physics



# Contents

- Introduction
- **BSM models and extended Higgs sectors**
- **Deviation in couplings of the SM-like Higgs  $h$  in non-minimal models**
- Direct search of the second Higgs bosons
- **Summary**

# Higgs and New Physics

## What is the essence of the Higgs field?

**Higgs Nature**



**BSM Paradigm**

- **Elementary Scalar**
- **Composite**
- **Pseudo NG Boson**
- **A gauge field in Extra D**
- **.....**

- Supersymmetry**
- Dynamical Symmetry Breaking**
- Little Higgs**
- Gauge-Higgs unification**
- .....**

Each model has a specific (extended) Higgs sector

# SUSY and $m_h = 126\text{GeV}$

Higgs potential

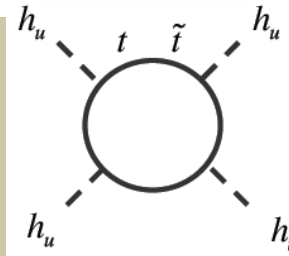
$$V = |D|^2 + |F|^2 + (\text{soft-breaking})$$

MSSM: **Type-II 2HDM** ( $H_u, H_d$ )

Self-coupling comes from **gauge couplings  $g, g'$**   $\Rightarrow$   **$m_h < m_Z$  at tree level**

$$m_h^2 < m_Z^2 \cos^2 2\beta + \frac{3m_t^4}{2\pi^2 v^2} \left[ \ln \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{A_t^2}{m_t^2} \left( 1 - \frac{A_t^2}{12m_{\tilde{t}}^2} \right) \right]$$

Loop effect



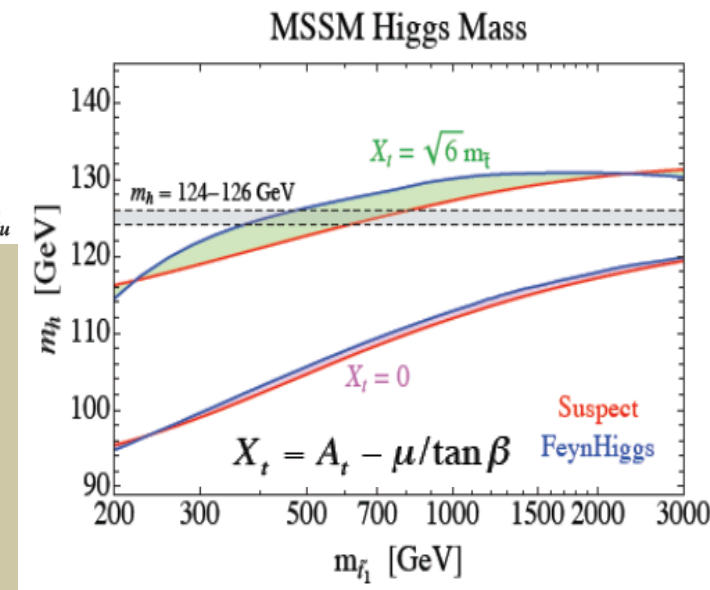
126 GeV can be realized by

**Large Stop Masses OR Large Stop LR-mixing**

$$M_{SUSY} \sim 10\text{TeV} \quad (X_t=0)$$

Consistent with the data

But **tension with Hierarchy Problem**



Hall, Pinner, Ruderman (2011)

# Phenomena beyond the SM

We already know BSM phenomena:

- **Neutrino oscillation**

$$\Delta m^2 \sim 8 \times 10^{-5} \text{ eV}^2, \quad \Delta m^2 \sim 2 \times 10^{-3} \text{ eV}^2$$

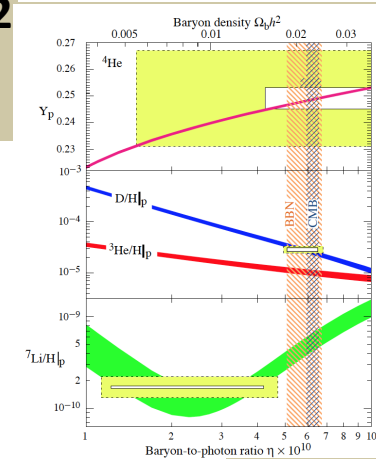
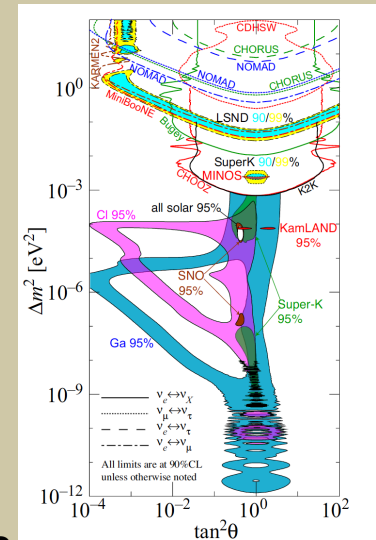
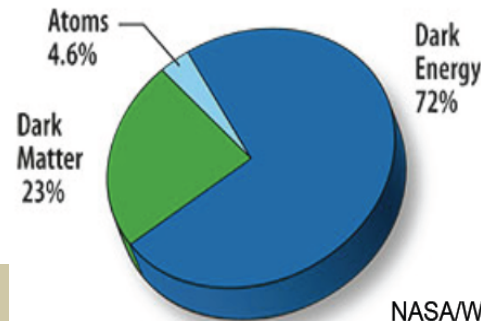
- **Dark Matter**

$$\Omega_{\text{DM}} h^2 \sim 0.11$$

- **Baryon Asymmetry of the Universe**

$$n_B/n_\gamma \sim 6 \times 10^{-10}$$

$$\eta_B = \frac{n_B}{n_\gamma} = \frac{n_b - n_{\bar{b}}}{n_\gamma}$$



To understand these phenomena, we need to go beyond-SM

At which scale?

# Electroweak Baryogenesis

$$\Gamma \sim e^{-E_{\text{sph}}/T} \quad (T < T_c)$$

$$\Gamma \sim \kappa(\alpha_W T)^4 \quad (T_c < T)$$

## Sakharov's conditions:

**B Violation**

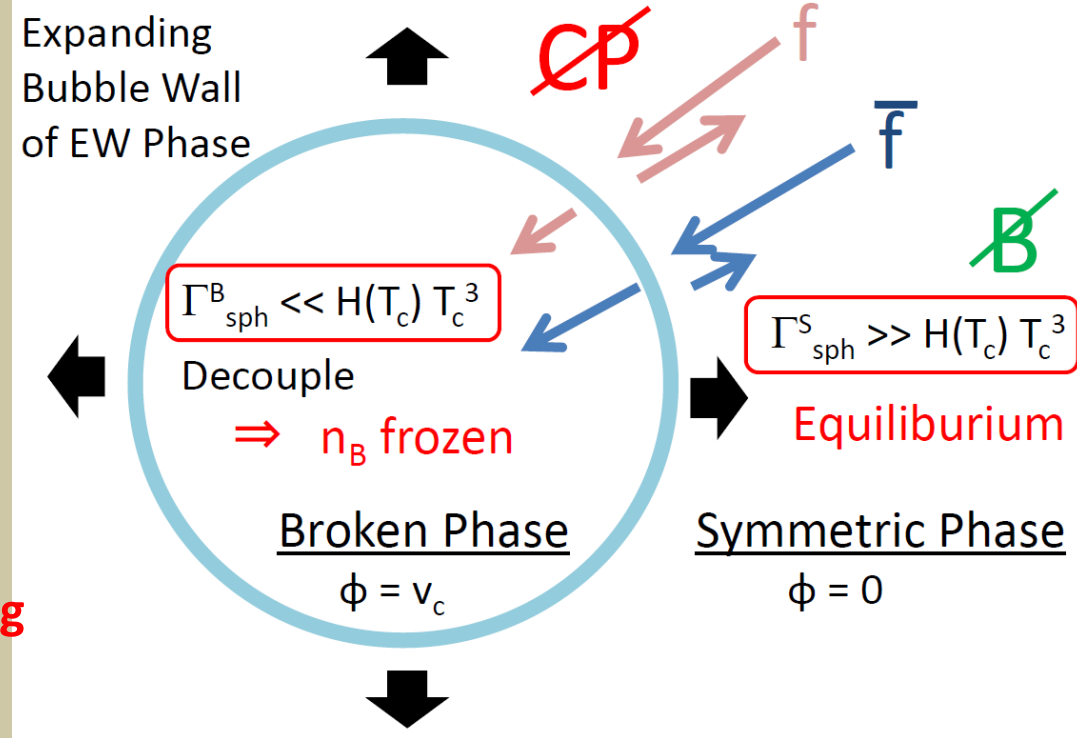
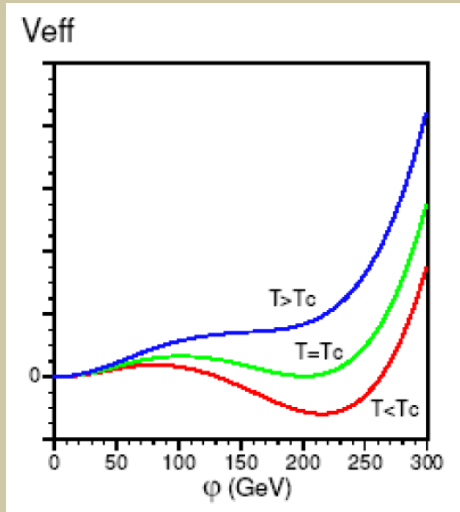
**C and CP Violation**

**Departure from Equilibrium**

→ **Sphaleron transition at high  $T$**

→ **CP Phases in extended scalar sector**

→ **1<sup>st</sup> Order EW Phase Transition**



**Condition of quick sphaleron decoupling**

**to keep sufficient baryon number in Broken Phase**

$$\frac{\varphi_c}{T_c} \gtrsim 1$$

**Physics of Higgs potential !**

# Condition of Strong 1<sup>st</sup> OPT ( $\phi_c/T_c > 1$ )

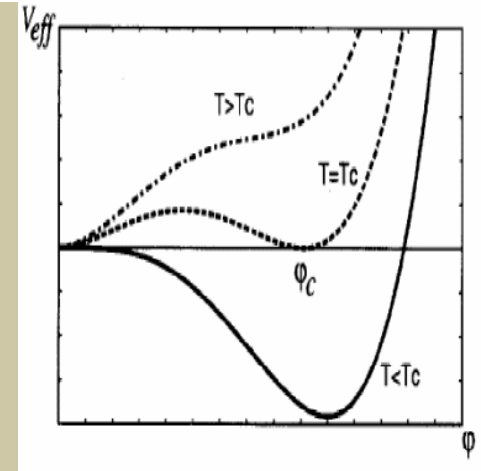
## Finite Temperature Potential

$$V_T(\phi, T) = D(T^2 - T_0^2)\phi^2 - ET\phi^3 + \frac{\lambda_T}{4}\phi^4 + \dots$$

$$\phi_c/T_c > 1 \Rightarrow 2E/\lambda_{T_c} > 1$$

Excluded in the SM

$$E = \frac{1}{12\pi v^3}(6m_W^3 + 3m_Z^3) \Rightarrow m_h = 60 \text{ GeV!}$$



Muti-Higgs models can satisfy the condition

$$V(\phi_{SM}, \Phi) = \dots + \lambda_{SM} \phi_{SM}^4 + \lambda' \phi_{SM}^2 \Phi^2 + \dots$$

2HDM, MSSM, ...

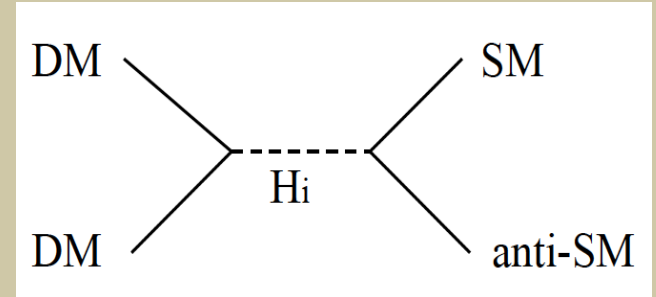
$$E \propto \frac{m_\Phi^3}{\lambda_T} = \frac{(\lambda')^{3/2}}{\lambda_T} \Rightarrow \lambda' > \lambda_{SM} = 0.3 \text{ (for } m_h = 126 \text{ GeV)}$$

$$\phi_c/T_c > 1 \text{ when } \lambda' > O(1)$$

# WIMP Dark Matter

## Higgs Portal Dark Matter

SM gauge singlet field ( $S$ ,  $\psi$ , or  $V$ )  
with **odd** under  $Z_2$



**SM+DM**

DMs annihilate into bottom pairs

**2HDM (Type-X)+DM, ...** DMs annihilate into tau pairs

Strong correlation with **direct/indirect searches**,  
thermal relic **abundance** and **invisible decay** of Higgs boson(s)

## Inert Doublet Model **SM+ H'**

**$Z_2$ -odd iso-doublet field  $H'$**  (neutral component is DM)

**A class of 2HDM, but one of the doublets has no VEV**

# BSM: Neutrino Masses

Neutrino Mass Term (= Effective dim-5 operator)

$$L^{\text{eff}} = (c_{ij}/M) \nu^i_L \nu^j_L \phi \phi$$

$$\langle \phi \rangle = v = 246 \text{ GeV}$$

Mechanism for tiny masses:

$$m^{\nu}_{ij} = (c_{ij}/M) v^2 < 0.1 \text{ eV}$$

Seesaw (tree level)

$$m^{\nu}_{ij} = y_i y_j v^2 / M \quad (M \gg 1 \text{ TeV or } y_i \ll 1)$$

Quantum Effects

N-th order of perturbation theory

$$m^{\nu}_{ij} = [g^2 / (16\pi^2)]^N C_{ij} v^2 / M \quad (M \text{ can be } 1 \text{ TeV})$$

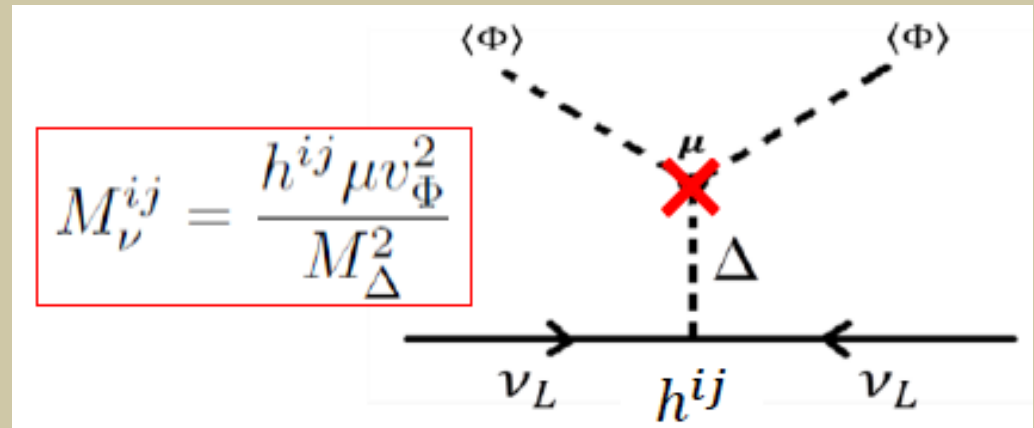


# Type-II Seesaw (Higgs triplet model)

*Cheng, Li (1980)*

*Mohapatra, Senjanovic (1981)*

$$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} + \Delta = \begin{pmatrix} \frac{\Delta^+}{\sqrt{2}} & \Delta^{++} \\ \Delta^0 & \frac{\Delta^+}{\sqrt{2}} \end{pmatrix}$$



Appearance of  
Doubly ( $H^{++}$ ) and singly ( $H^+$ )  
charged Higgs bosons

Seesaw Mechanism

$$h^{ij} \mu v_{\Delta} \ll M_{\Delta}^2$$

Unique Phenomenology

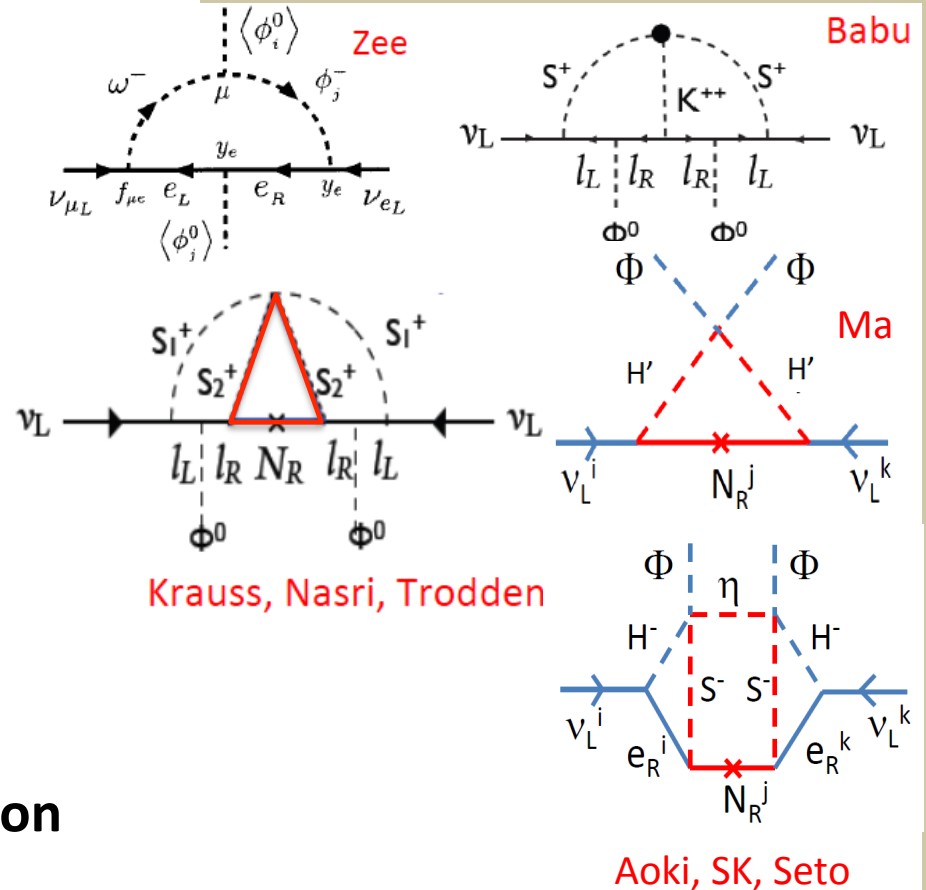
# Loop induced mass at TeV scale

## Radiative Seesaw Scenario

- Extended Higgs sector
- $Z_2$  parity
  - **Neutrino mass** generated at the loop level
  - **WIMP Dark Matter**
    - Lightest  $Z_2$ -odd particle
    - LSP (in SUSY extension)

## Electroweak Baryogenesis

- Sphaleron
- Additional CP Phases
- Strong 1<sup>st</sup> Order Phase Transition



These scenarios are strongly related to the Higgs physics!

# Radiative seesaw with $Z_2$

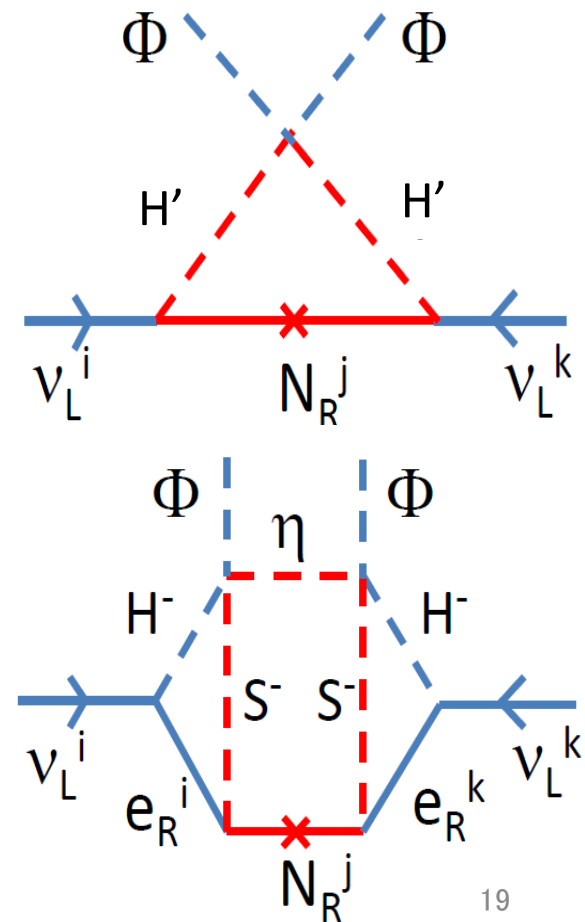
- $Z_2$ -parity plays roles:
1. **No tree-level seesaw** (Radiative neutrino mass)
  2. **Stability** of the lightest  $Z_2$ -odd particle (WIMP)

## Ex1) 1-loop *Ma (2006)*

- Simplest model
- **SM + Inert doublet ( $H'$ ) +  $N_R$**
- DM candidate [  $H'$  or  $N_R$  ]

## Ex2) 3-loop *Aoki-SK-Seto (2008)*

- Neutrino mass from  **$O(1)$**  coupling
- **2HDM +  $\eta^0 + S^+ + N_R$**
- DM candidate [  $\eta^0$  (or  $N_R$ ) ]
- Electroweak Baryogenesis



# Extended Higgs Sector

## bottom up approach

The “**SM-like**” does not necessarily mean the SM.

All extended Higgs sector can contain the SM-like Higgs boson.

# Extended Higgs

If the Higgs sector contains more than one scalar bosons, possibility would be

- SM + extra Singlets (NMSSM, B-L Higgs, ...)
- SM + extra Doublets (MSSM, CPV, EW Baryogenesis, Neutrino mass, ...)
- SM + extra Triplets (Type II seesaw, LR models....)
- ....

**Basic experimental quantities:**

- Electroweak rho parameter
- Flavor Changing Neutral Current (FCNC)

# Electroweak rho parameter

$$\rho_{\text{exp}} = 1.0008^{+0.0017}_{-0.0007}$$

$$Q = I_3 + Y/2$$

$$\rho \equiv \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} = \frac{\sum_i [4T_i(T_i + 1) - Y_i^2] |v_i|^2 c_i}{\sum_i 2Y_i^2 |v_i|^2}$$

$T_i$ :  $SU(2)_L$  isospin

$Y_i$ : hypercharge

$v_i$ : v.e.v.

$c_i$ : 1 for complex representation

1/2 for real representation

## Possibility

1.  $\rho=1$  SM + doublets ( $\phi$ ) + singlets (S), (septet, ...)

2.  $\rho \approx 1$  SM + Triplets ( $\Delta$ )

a)  $v_\Delta \ll v_\phi$

b) Combination of several representations

[ (ex) Georgi-Machasek model]  $v_\Delta \approx v_\phi$

$$\rho_{\text{tree}} = \frac{1 + \frac{2v_\Delta^2}{v_\phi^2}}{1 + \frac{4v_\Delta^2}{v_\phi^2}} \simeq 1 - \frac{2v_\Delta^2}{v_\phi^2}$$

Multi-doublets (+singlets) seem the most natural choice?

# 2 Higgs Doublet Model

$$V_{\text{THDM}} = +m_1^2 |\Phi_1|^2 + m_2^2 |\Phi_2|^2 - \frac{m_3^2}{2} (\Phi_1^\dagger \Phi_2 + \Phi_2^\dagger \Phi_1) \\ + \frac{\lambda_1}{2} |\Phi_1|^4 + \frac{\lambda_2}{2} |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 \\ + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \frac{\lambda_5}{2} \left[ (\Phi_1^\dagger \Phi_2)^2 + (\text{h.c.}) \right]$$

$\Phi_1$  and  $\Phi_2 \Rightarrow h, H, A^0, H^\pm \oplus$  Goldstone bosons

$\begin{array}{cccc} \uparrow & \uparrow & \uparrow & \text{charged} \\ \text{CPEven} & \text{CPodd} & & \end{array}$

$$m_h^2 = v^2 \left( \lambda_1 \cos^4 \beta + \lambda_2 \sin^4 \beta + \frac{\lambda}{2} \sin^2 2\beta \right) + \mathcal{O}\left(\frac{v^2}{M_{\text{soft}}^2}\right),$$

$$m_H^2 = M_{\text{soft}}^2 + v^2 (\lambda_1 + \lambda_2 - 2\lambda) \sin^2 \beta \cos^2 \beta + \mathcal{O}\left(\frac{v^2}{M_{\text{soft}}^2}\right),$$

$$m_{H^\pm}^2 = M_{\text{soft}}^2 - \frac{\lambda_4 + \lambda_5}{2} v^2,$$

$$m_A^2 = M_{\text{soft}}^2 - \lambda_5 v^2.$$

$M_{\text{soft}}$ : soft breaking scale

$$\Phi_i = \begin{bmatrix} w_i^+ \\ \frac{1}{\sqrt{2}}(h_i + v_i + i a_i) \end{bmatrix} \quad (i = 1, 2)$$

**Diagonalization**

$$\begin{bmatrix} h_1 \\ h_2 \end{bmatrix} = \begin{bmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{bmatrix} \begin{bmatrix} H \\ h \end{bmatrix} \quad \begin{bmatrix} z_1^0 \\ z_2^0 \end{bmatrix} = \begin{bmatrix} \cos \beta & -\sin \beta \\ \sin \beta & \cos \beta \end{bmatrix} \begin{bmatrix} z^0 \\ A^0 \end{bmatrix} \\ \begin{bmatrix} w_{1^\pm} \\ w_{2^\pm} \end{bmatrix} = \begin{bmatrix} \cos \beta & -\sin \beta \\ \sin \beta & \cos \beta \end{bmatrix} \begin{bmatrix} w^\pm \\ H^\pm \end{bmatrix}$$

$$\frac{v_2}{v_1} \equiv \tan \beta$$

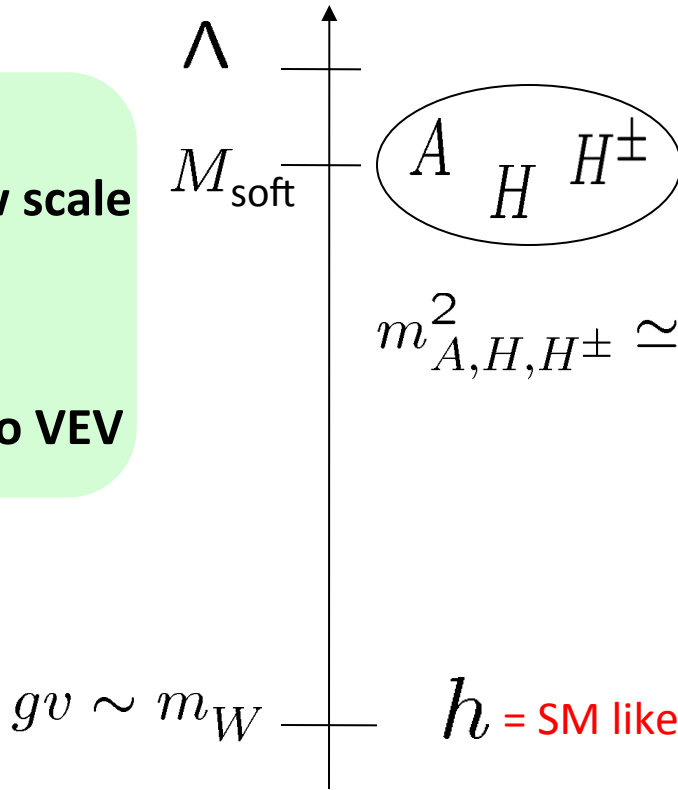
$$M_{\text{soft}} \left( = \frac{m_3}{\sqrt{\cos \beta \sin \beta}} \right):$$

soft-breaking scale  
of the discrete symm.

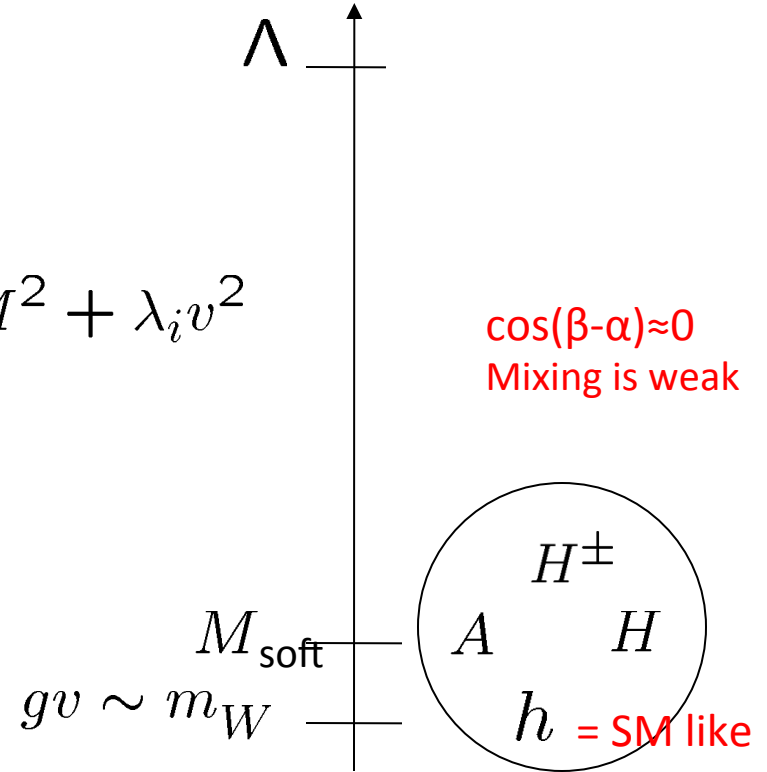
# The SM-like $h$ (two possibilities)

$\Lambda$  :  
Cutoff, New scale

$M_{\text{soft}}$  :  
Mass scale  
irrelevant to VEV



$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \frac{v^2}{M_{\text{soft}}^2} \mathcal{O}^{(6)}$$



$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{nonSM}} + \frac{v^2}{\Lambda^2} \mathcal{O}^{(6)}$$



# FCNC Suppression

Multi-Higgs model: **FCNC appears via Higgs mediation**

ex) **2 Higgs doublet models:**

to avoid FCNC, impose a discrete symmetry

$$\Phi_1 \rightarrow +\Phi_1, \quad \Phi_2 \rightarrow -\Phi_2$$

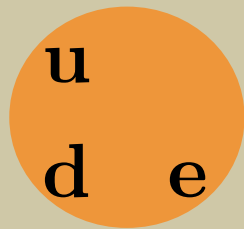
Each quark or lepton couples only one Higgs doublet

**No FCNC at tree level**

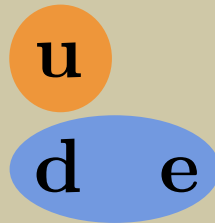
## Four Types of Yukawa coupling

*Barger, Hewett, Phillips*

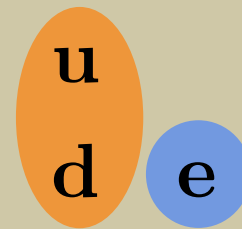
Classified by  $Z_2$  charge assignment



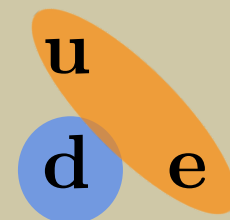
Type-I



Type-II



Type-X



Type-Y

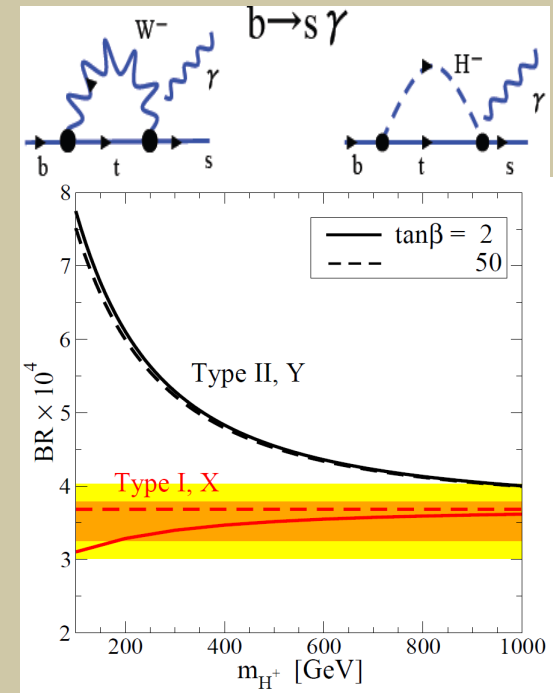
# Type of 2HDM

**Type-I** Fermiophobic 2HDM  
Neutrinophilic 2HDM

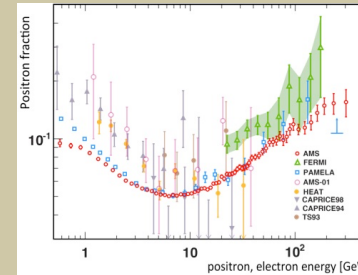
**Type-II** MSSM, NMSSM, other  
SUSY extended Higgs models

**Type-X** Lepton-specific 2HDM  
Neutrino Masses  
Positron Excess  
H portal DM (tau specific)

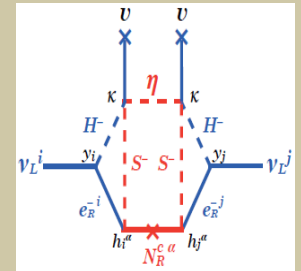
**Type-Y** Flipped 2HDM



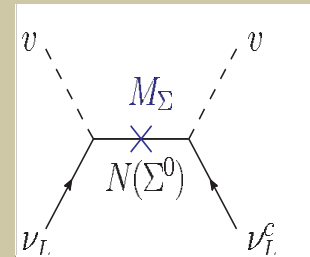
Aoki, SK, Tsumura, Yagyu (09)



Goh, Hall, Kumar (09)



Aoki, SK, Seto (09)



Ma (02) 26

# Search for Extended Higgs sectors

Many new physics models predict **non-minimal** Higgs sectors

Experimental determination of the Higgs sector is the Key to clarify the EWSB and also to explore new physics!

- **Direct Search**
  - Discovery of the “second” Higgs boson at LHC
- **Indirect Search** (find deviation in Higgs couplings)
  - How we can extract the shape of the Higgs sector from detailed measurement of the 126GeV SM-like Higgs boson ***h?***
  - **Solid target!**

# Search for Extended Higgs sectors

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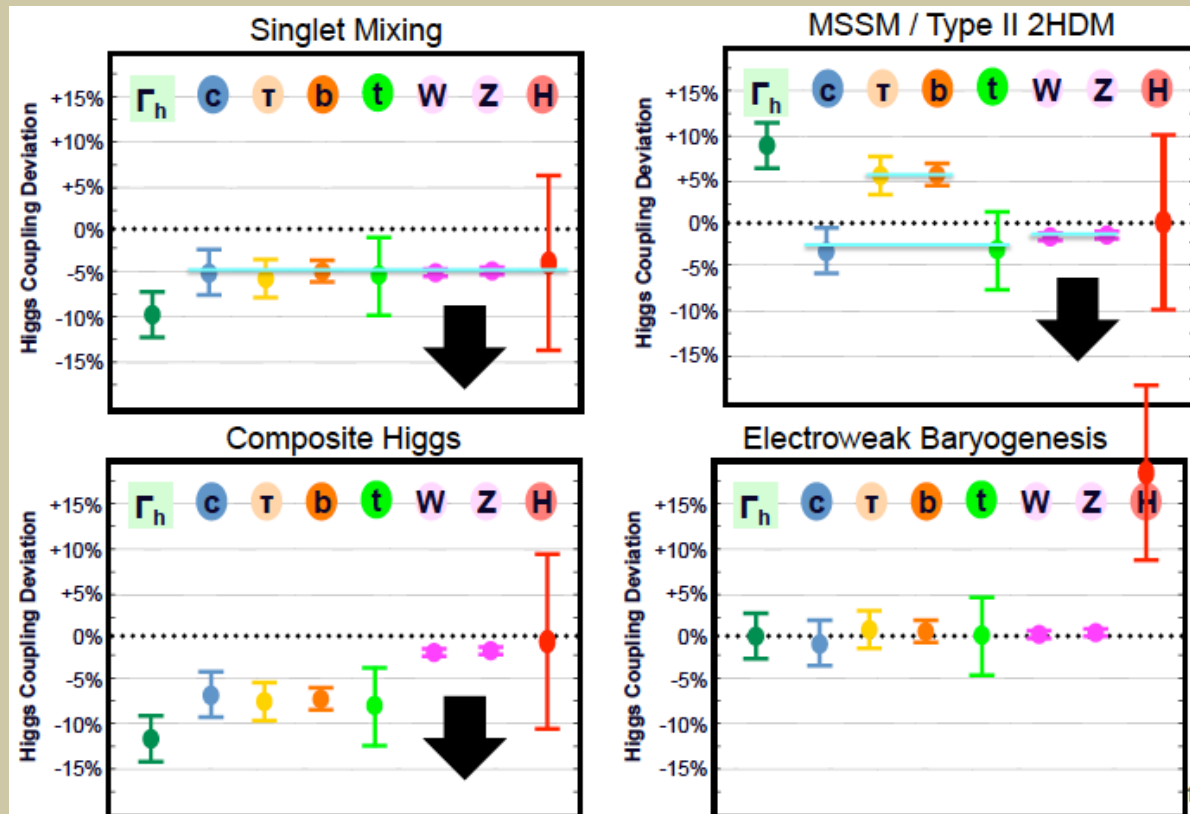
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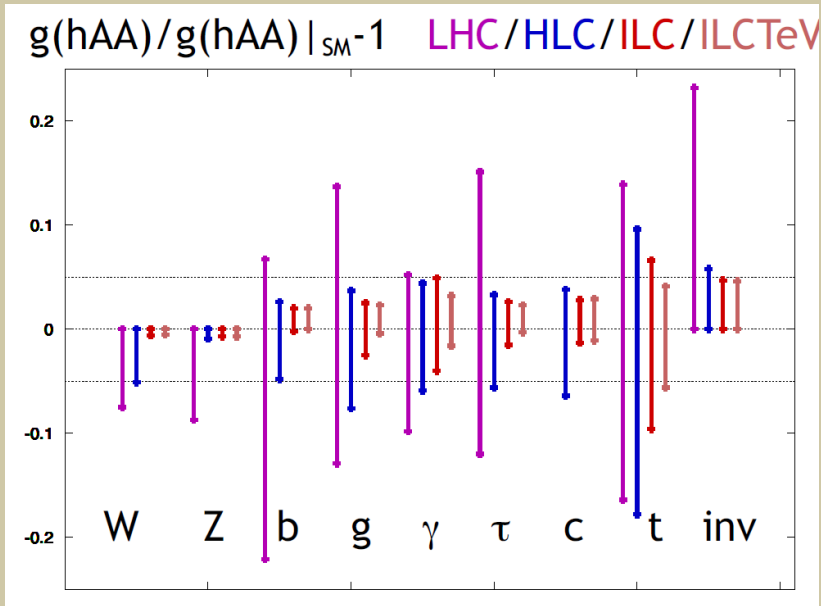
# Precision measurement of the SM-like Higgs boson $h$

Fingerprinting the models via Higgs couplings

*S. Yamashita  
2005*

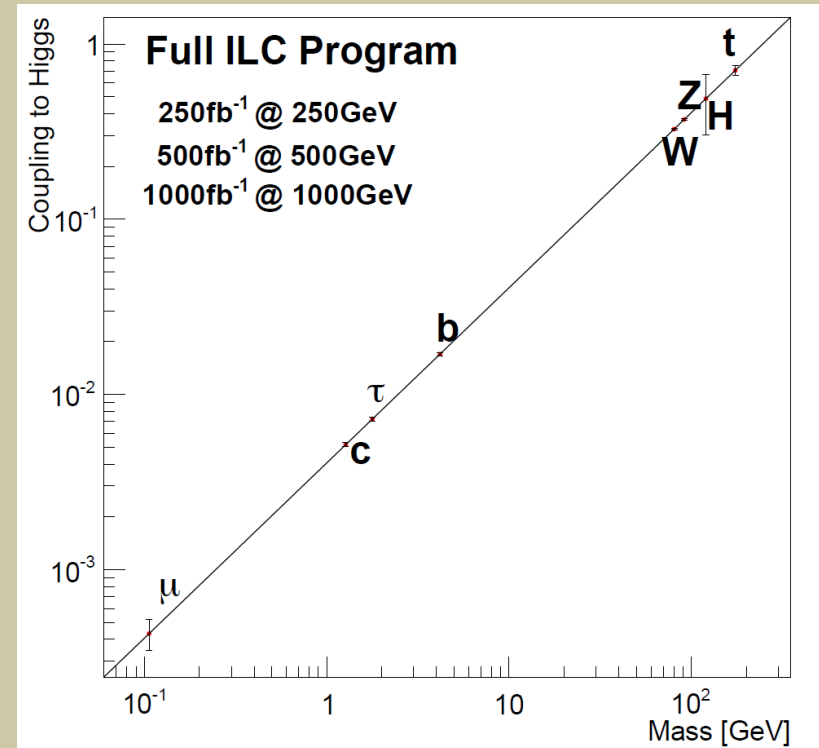


# International Linear Collider



M. Peskin, 2012

Coupling measurable by **a few%**, and  $hhh$  can also be measured by around O(10) %



At ILC, we may be able to distinguish models by detecting a pattern of deviations in the **h** couplings from the SM values!

# Snowmass White Paper (Aug. 2013)

Facility	LHC	HL-LHC	ILC500	ILC500-up	ILC1000	ILC1000-up	CLIC	TLEP (4 IPs)
$\sqrt{s}$ (GeV)	14,000	14,000	250/500	250/500	250/500/1000	250/500/1000	350/1400/3000	240/350
$\int \mathcal{L} dt$ (fb $^{-1}$ )	300/expt	3000/expt	250+500	1150+1600	250+500+1000	1150+1600+2500	500+1500+2000	10,000+2600
$\kappa_\gamma$	5 – 7%	2 – 5%	8.3%	4.4%	3.8%	2.3%	–/5.5/<5.5%	1.45%
$\kappa_g$	6 – 8%	3 – 5%	2.0%	1.1%	1.1%	0.67%	3.6/0.79/0.56%	0.79%
$\kappa_W$	4 – 6%	2 – 5%	0.39%	0.21%	0.21%	0.13%	1.5/0.15/0.11%	0.10%
$\kappa_Z$	4 – 6%	2 – 4%	0.49%	0.24%	0.44%	0.22%	0.49/0.33/0.24%	0.05%
$\kappa_\ell$	6 – 8%	2 – 5%	1.9%	0.98%	1.3%	0.72%	3.5/1.4/<1.3%	0.51%
$\kappa_d$	10 – 13%	4 – 7%	0.93%	0.51%	0.51%	0.31%	1.7/0.32/0.19%	0.39%
$\kappa_u$	14 – 15%	7 – 10%	2.5%	1.3%	1.3%	0.76%	3.1/1.0/0.7%	0.69%

$$g(hxx) = \kappa_x g(hxx)_{SM}$$

ILC Higgs White Paper

*Asner, Barklow, Fujii,  
Haber, Kanemura,  
Miyamoto, Weiglein,  
et al.*

	ILC(250)	ILC(500)	ILC(1000)	ILC(LumUp)
$\sqrt{s}$ (GeV)	250	250+500	250+500+1000	250+500+1000
L (fb $^{-1}$ )	250	250+500	250+500+1000	1150+1600+2500
$\gamma\gamma$	17 %	8.3 %	3.8 %	2.3 %
$gg$	6.1 %	2.0 %	1.1 %	0.7 %
$WW$	4.7 %	0.4 %	0.3 %	0.2 %
$ZZ$	0.7 %	0.5 %	0.5 %	0.3 %
$t\bar{t}$	6.4 %	2.5 %	1.3 %	0.9 %
$b\bar{b}$	4.7 %	1.0 %	0.6 %	0.4 %
$\tau^+\tau^-$	5.2 %	1.9 %	1.3 %	0.7 %
$\Gamma_T(h)$	9.0 %	1.7 %	1.1 %	0.8 %
$\mu^+\mu^-$	91 %	91 %	16 %	10 %
$hhh$	–	83 %	21 %	13 %
BR(invis.)	< 0.7 %	< 0.7 %	< 0.7 %	< 0.3 %
$c\bar{c}$	6.8 %	2.9 %	2.0 %	1.1 %

See Tian's Talk

# Discrimination of models via coupling of the 125GeV Higgs boson $h$

BSM models can be distinguished by the pattern in deviations of the SM-like Higgs couplings

$h\gamma\gamma$ ,  $hgg$ ,  $hWW$ ,  $hZZ$ ,  $htt$ ,  $hff$ ,  $hhh$

## Scalar Mixing ( $h \Leftrightarrow \varphi$ )

Gauge couplings ( $hVV$ ):

Yukawa couplings ( $hff$ ):

The pattern of deviation strongly depend on the model

## Quantum effects (Non-decoupling effect)

Large deviation in loop-induced processes ( $h \rightarrow \gamma\gamma$  and  $h \rightarrow gg$ )

Large quantum correction can also appear in the  $hhh$  coupling



# Deviation in $\kappa_i^2$ and the scale of BSM

- Mass of the second Higgs boson is a free parameter
- Correlation with the **SM-like  $h$  couplings**
  - Structure of BSM (MSSM)
  - Unitarity and Vacuum Stability in general
- If  $\kappa_V^2 < 1$  is observed by experiment, the scale of the second Higgs boson is obtained

# Unitarity bound in the 2HDM

$$\kappa_V^2 = \sin^2(\beta - \alpha)$$

If  $\kappa_V^2$  is found to be less than 1, the upper bound on the mass of the second Higgs is obtained

$\Phi_1$  and  $\Phi_2$  share  $v=246$  GeV

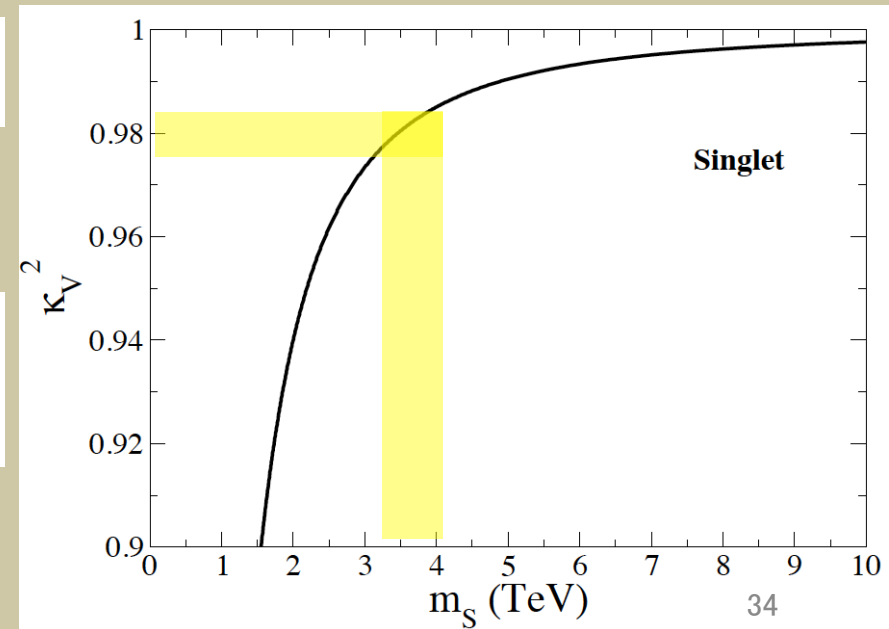
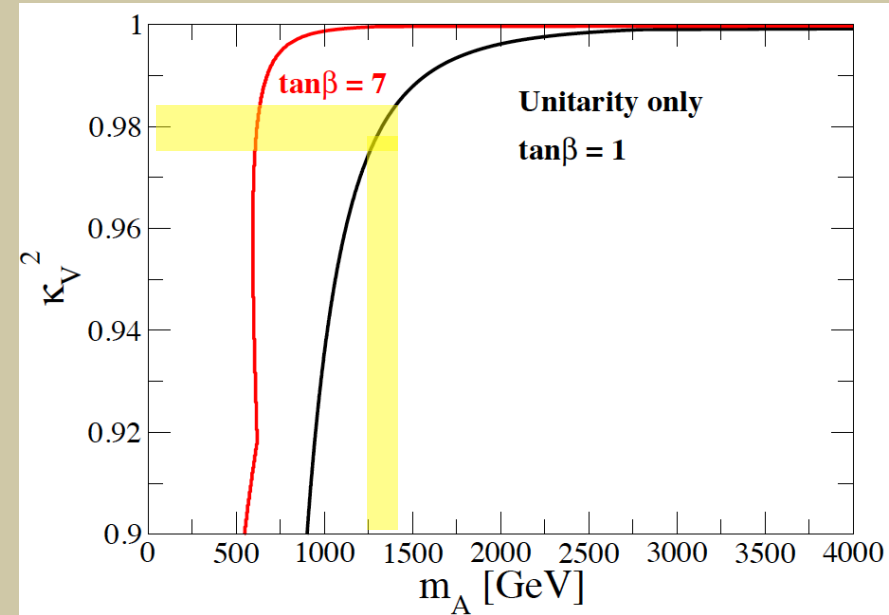
$$v_1^2 + v_2^2 = v^2$$

# In Higgs Singlet model ( $\Phi+S$ )

$$\kappa_V^2 = \cos^2\theta$$

Situation is similar, but the bound is much relaxed

$S$  has the VEV but it does not share  $v$  (= 246 GeV)

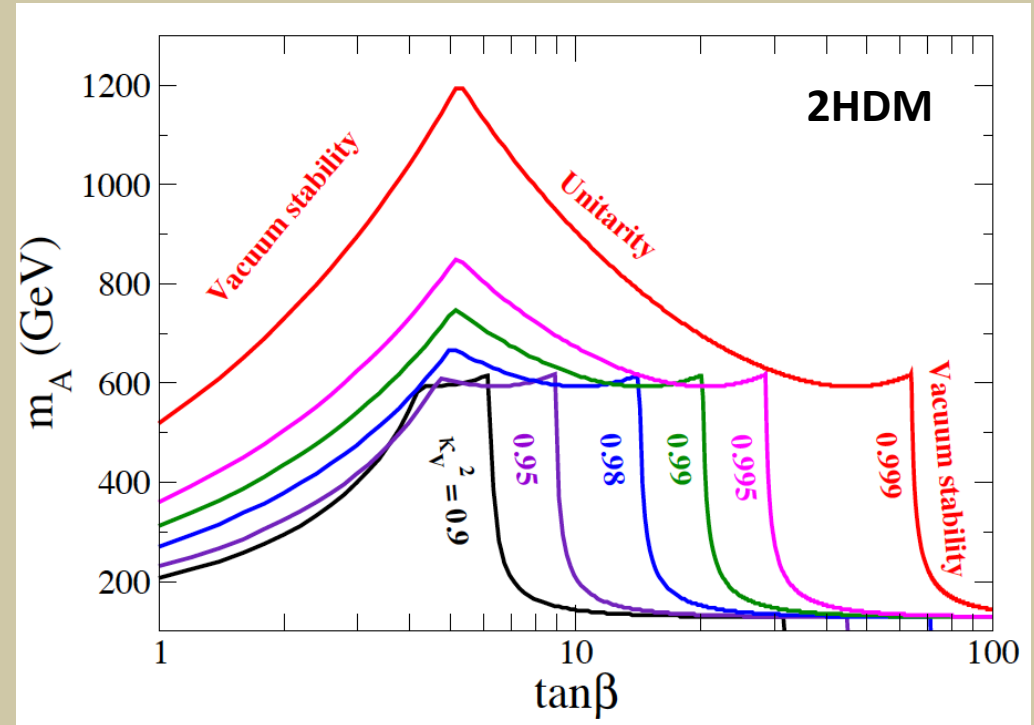


# Theoretical upper bounds on the second Higgs mass, when $\kappa_V^2 < 1$

If measured  $\kappa_V^2$  is slightly smaller than 1 (say, 0.99), the second Higgs must be lighter than 700 GeV.

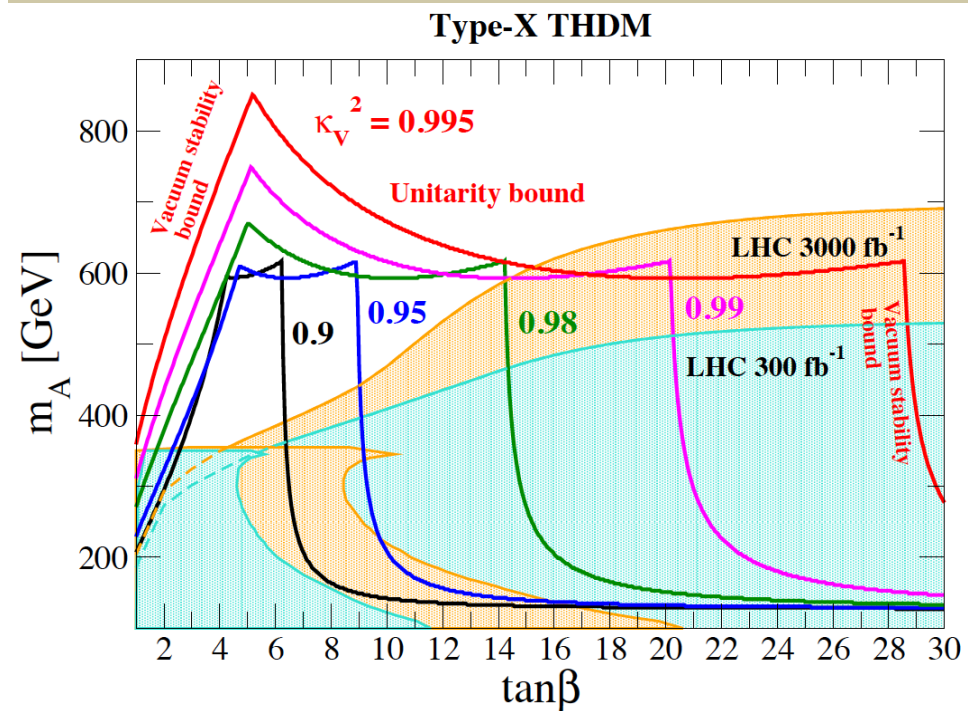
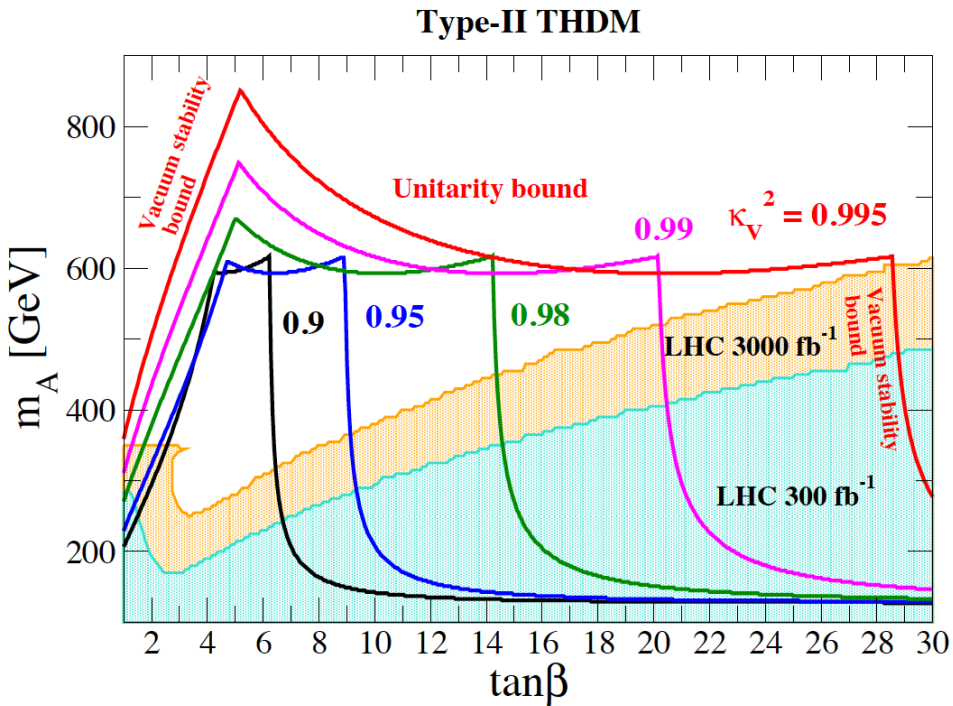
Then, if no second Higgs is found below 700 GeV, the 2HDM is **excluded**

The rest possibility may be the Higgs singlet model, or other exotics



**Precision determination of  $hVV$  coupling is very important**

# LHC can search relatively large $\tan\beta$ regions



# Yukawa couplings $hff$

Effects of the mixing ( $\alpha$ ,  $\tan\beta$ ) change Yukawa couplings of  $h$

**Type-II**  $hbb \propto \sin(\beta-\alpha) - \tan\beta \cos(\beta-\alpha)$   
 $h\tau\tau \propto \sin(\beta-\alpha) - \tan\beta \cos(\beta-\alpha)$

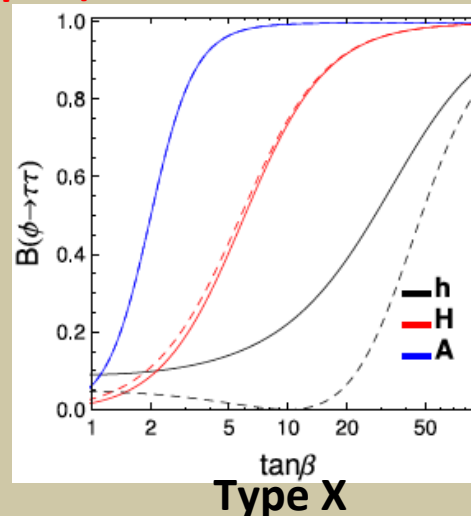
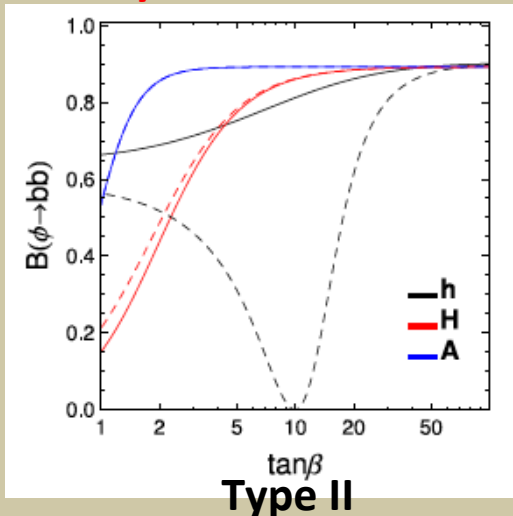
**Type-X**  $hbb \propto \sin(\beta-\alpha) + \cot\beta \cos(\beta-\alpha)$   
 $h\tau\tau \propto \sin(\beta-\alpha) - \tan\beta \cos(\beta-\alpha)$

	$\Phi_1$	$\Phi_2$	$u_R$	$d_R$	$\ell_R$	$Q_L, L_L$
Type I	+	-	-	-	-	+
Type II (SUSY)	+	-	-	+	+	+
Type X (Lepton-specific)	+	-	-	-	+	+
Type Y (Flipped)	+	-	-	+	-	+

	$\xi_h^u$	$\xi_h^d$	$\xi_h^\ell$
Type-I	$c_\alpha/s_\beta$	$c_\alpha/s_\beta$	$c_\alpha/s_\beta$
Type-II	$c_\alpha/s_\beta$	$-s_\alpha/c_\beta$	$-s_\alpha/c_\beta$
Type-X	$c_\alpha/s_\beta$	$c_\alpha/s_\beta$	$-s_\alpha/c_\beta$
Type-Y	$c_\alpha/s_\beta$	$-s_\alpha/c_\beta$	$c_\alpha/s_\beta$

Coefficient of  $hff$

Nearly SM-like case:  $\sin^2(\beta-\alpha)=0.99$



S.K., K. Tsumura, H. Yokoya 2013

# Pattern in deviations of $g_{hVV}$ and $Y_{hff}$

Model	$\mu$	$\tau$	$b$	$c$	$t$	$g_V$
Singlet mixing	↓	↓	↓	↓	↓	↓
2HDM-I	↓	↓	↓	↓	↓	↓
2HDM-II (SUSY)	↑	↑	↑	↓	↓	↓
2HDM-X (Lepton-specific)	↑	↑	↓	↓	↓	↓
2HDM-Y (Flipped)	↓	↓	↑	↓	↓	↓

$\cos(\beta-\alpha) < 0$

Singlet can be distinguished from the Type-I 2HDM

$Y_{hff}/g_V=1$  in the singlet model but  $Y_{hff}/g_V \neq 1$  in the 2HDM-I

In the triplet model, quark-Yukawa couplings are universally smaller, Lepton-Yukawa deviate universal.  $\kappa_V$  can be greater than 1

$\kappa_V > 1$  is a signature of exotic Higgs (with higher representations)

Extended Higgs models are distinguishable by precisely measuring  $hVV$  and  $hff$

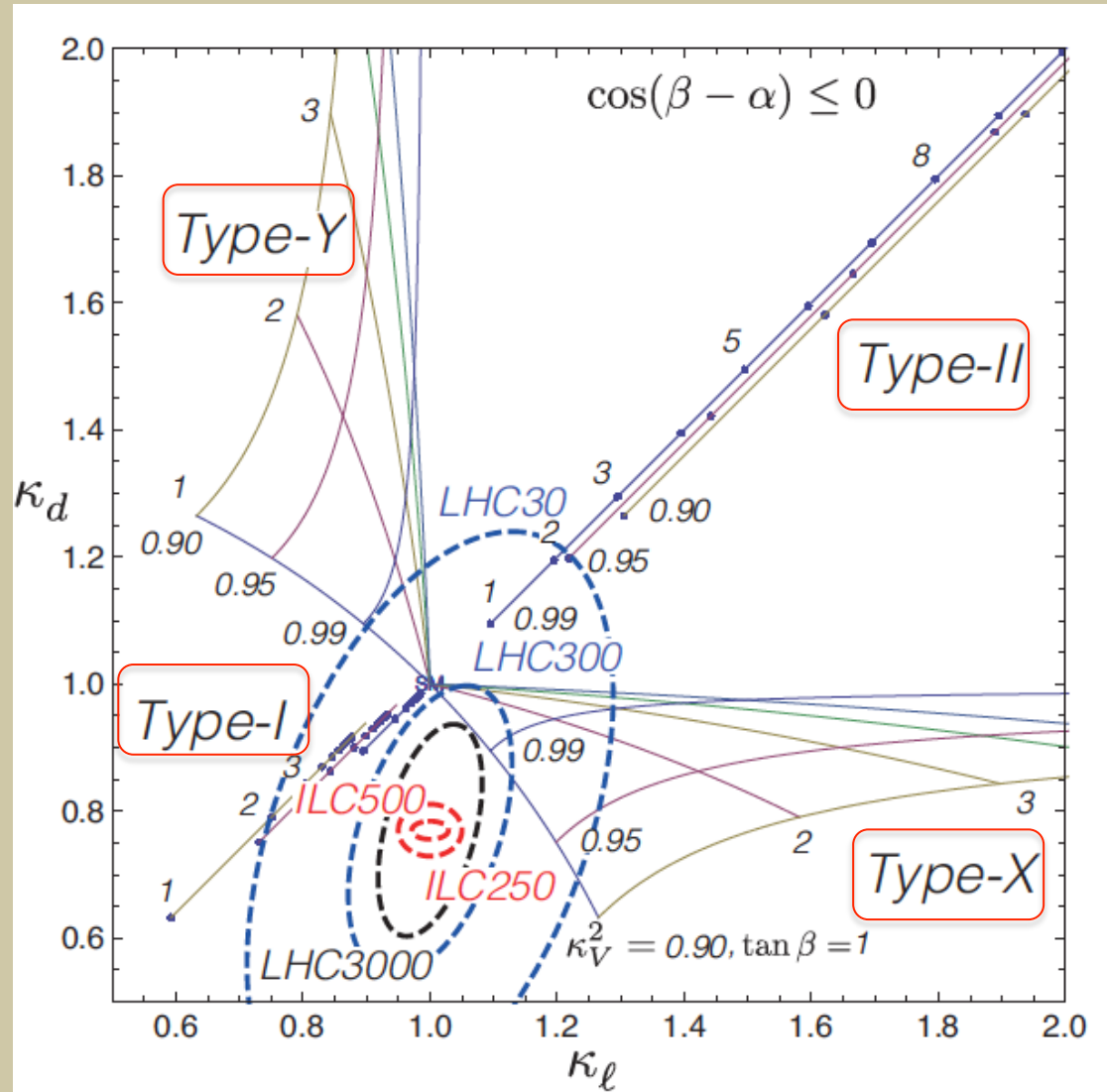
# Fingerprinting the model (2HDM)

SK, K. Tsumura, K. Yagyu, H. Yokoya 2013

**hbb vs h $\tau\tau$**

We can determine  
the type of  
Yukawa interaction  
in the 2HDM

Ellipse = 68.27% CL



# Fingerpointing the model (Exotics)

SK, K. Tsumura, K. Yagyu, H. Yokoya 2013

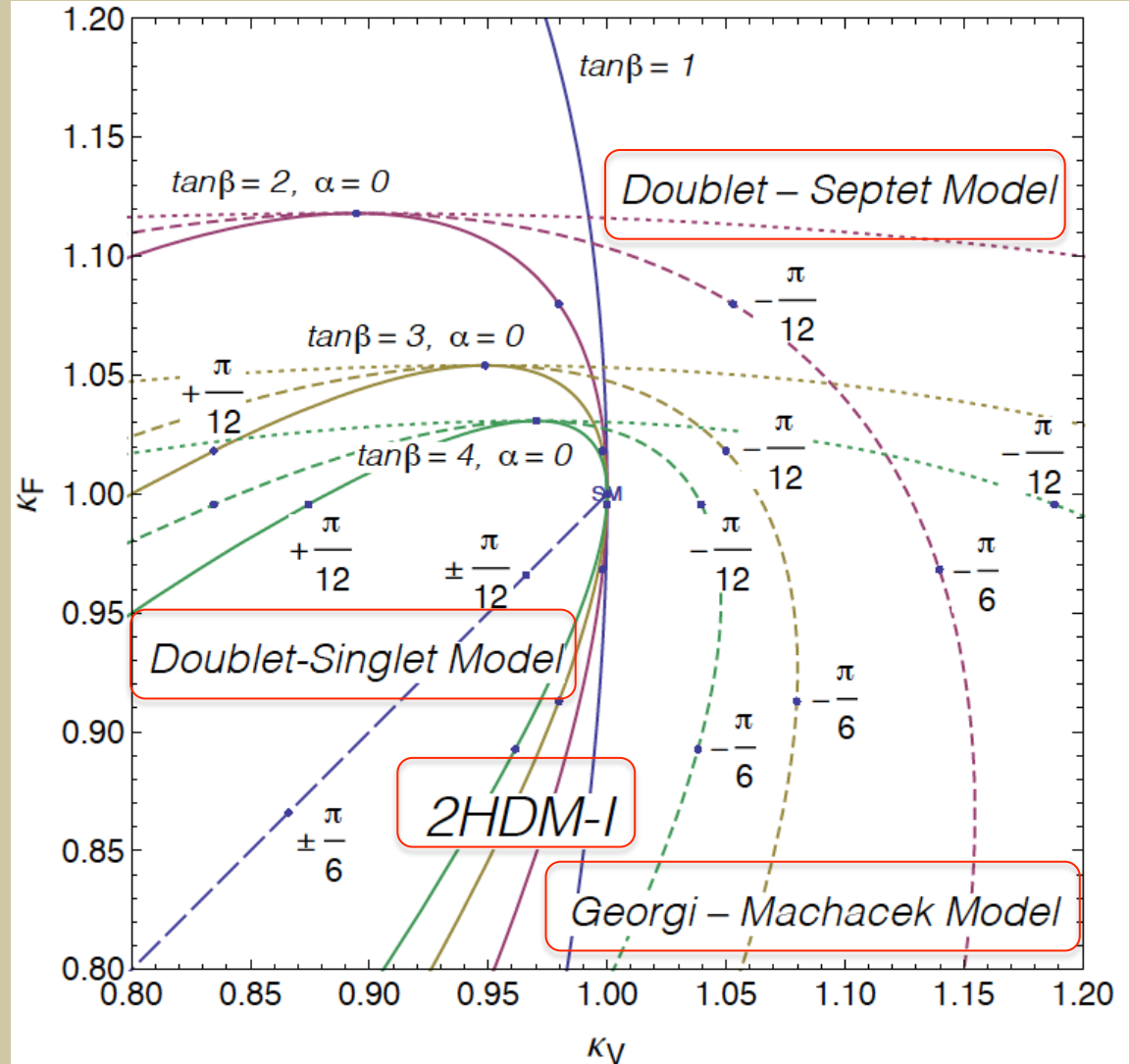
Universal Fermion  
Coupling ( $\kappa_F$ )

VS

$hVV$  coupling ( $\kappa_V$ )

Exotic models  
predict  $\kappa_V > 1$

We can discriminate  
Exotic models





# Measurement of $\tan\beta$ at ILC

SK, Tsumura, Yokoya, arXiv:1305.5424

$\sin(\beta-\alpha)$  and  $\tan\beta$  are important

$hVV \rightarrow \sin(\beta-\alpha)$

How about  $\tan\beta$ ?

## $\tan\beta$ determination

1. Branching ratio of  $H, A$

useful for small  $\tan\beta$

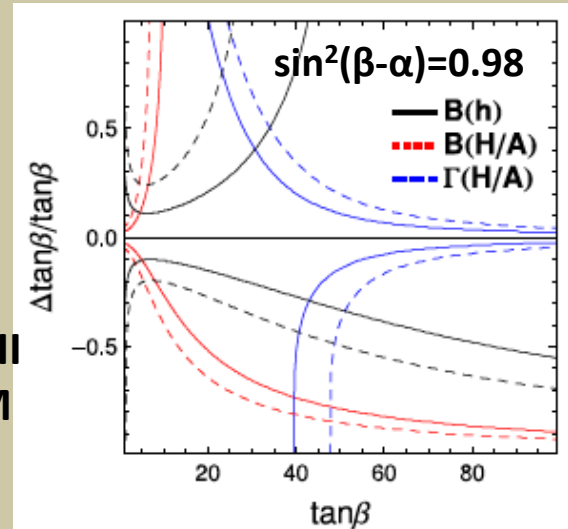
2. Total width of  $H, A$  Berger, Han, jiang (01)  
Gunion, Han, Jiang, Sopczak (03)

useful for large  $\tan\beta$

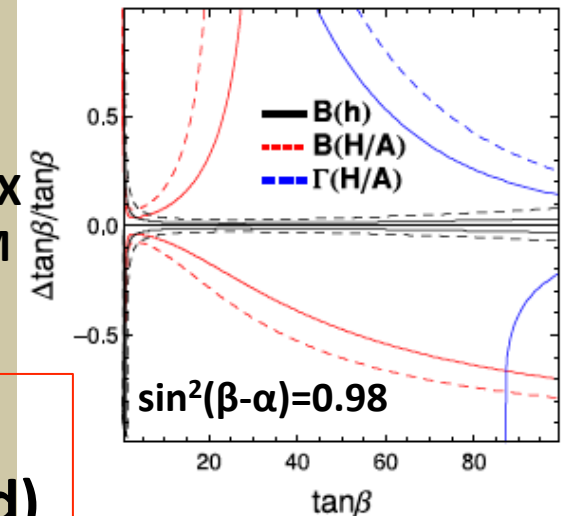
3. Decay of **SM-like Higgs  $h$**  when  $\sin(\beta-\alpha)$  is slightly smaller than 1

SK, Tsumura, Yokoya, arXiv:1305.5424

Type-II  
2HDM



Type-X  
2HDM



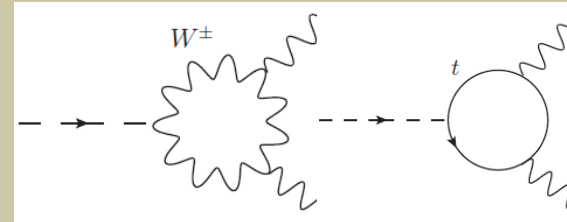
Precision measurement of **the  $h$  decay at ILC** is very useful (information of  $H, A$  not required)

# Di-photon Decay Width

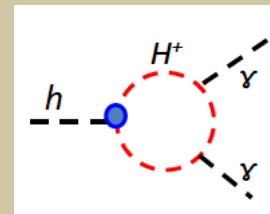
Loop induced process in the SM  
**New physics effect enters** at the same order of perturbation

New physics particles which realize a large deviation in  $h\gamma\gamma$

- $W'$  boson
- Singly/Doubly Charged Scalars
- New Charged Leptons
- SUSY
- .....

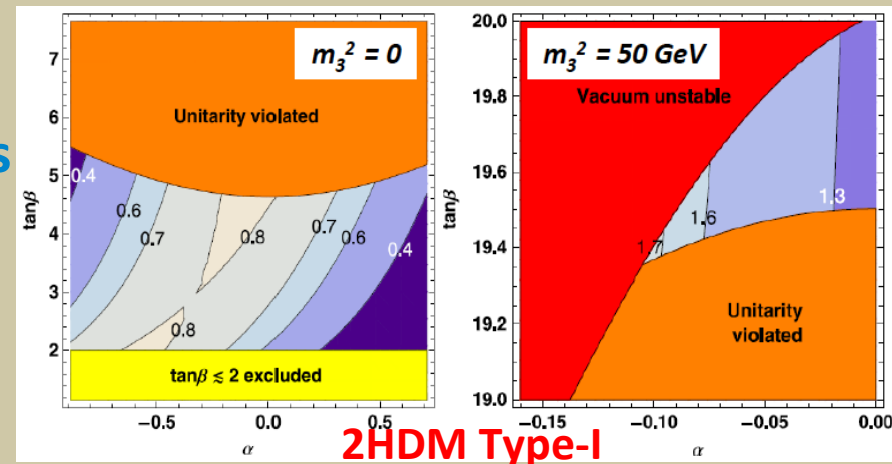


SM loop  
destructive



$H^+$  loop  
in 2HDM

*P. Posch (2011)*



2HDM Type-I

Parameters can be constrained

⇒ Test a model by correlation to the other observable

# Self-coupling $hhh$

It is important to determine the structure of Higgs potential

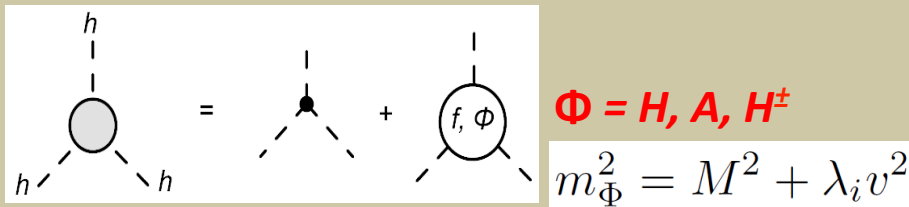
$$V_{\text{Higgs}} = \frac{1}{2} m_h^2 h^2 + \frac{1}{3!} \lambda_{hhh} h^3 + \frac{1}{4!} \lambda_{hhhh} h^4 + \dots$$

Even if  $h$  is SM-like ( $\sin(\alpha-\beta)=1$ ), a large deviation can appear due to non-decoupling loop effects

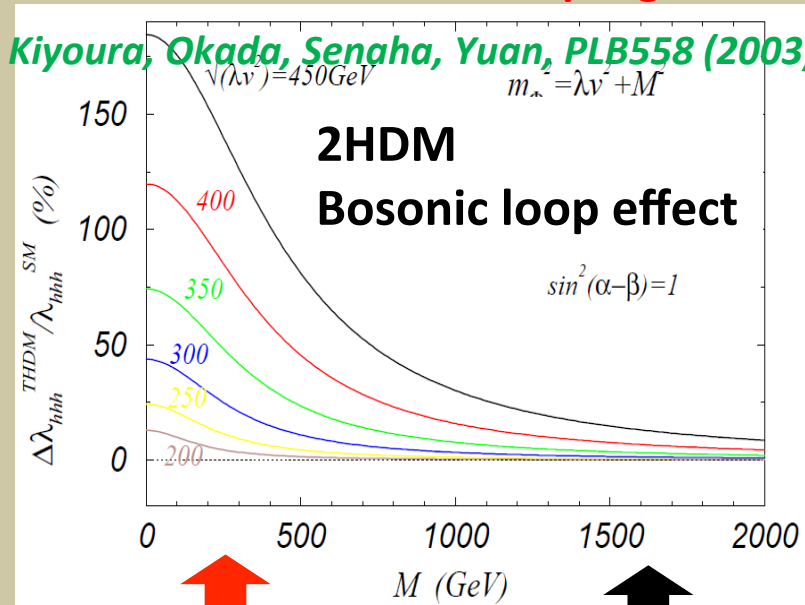
SM

$$\lambda_{hhh}^{\text{SMloop}} \sim \frac{3m_h^2}{v} \left( 1 - \frac{N_c m_t^4}{3\pi^2 v^2 m_h^2} + \dots \right)$$

Non-decoupling effect



SK, Kiyoura, Okada, Senaha, Yuan, PLB558 (2003)



In extended Higgs models the deviation can be  $\sim 100\%$  by bosonic loop effect

Non-decoupling effect

Decoupling

# EW Baryogenesis and the $hhh$ coupling

## Higgs Potential at Finite Temperatures

$$V_T(\phi, T) = D(T^2 - T_0^2)\phi^2 - ET\phi^3 + \frac{\lambda_T}{4}\phi^4 + \dots$$

$$\phi_c/T_c = 2E/\lambda_{T_c}$$

$$E = \frac{1}{12\pi v^3}(6m_W^3 + 3m_Z^3) + \text{Non-decoupling effect of new particles}$$

$$\lambda_T = m_h^2/2v^2 + \text{log corrections}$$

### Condition of strongly 1<sup>st</sup> OPT

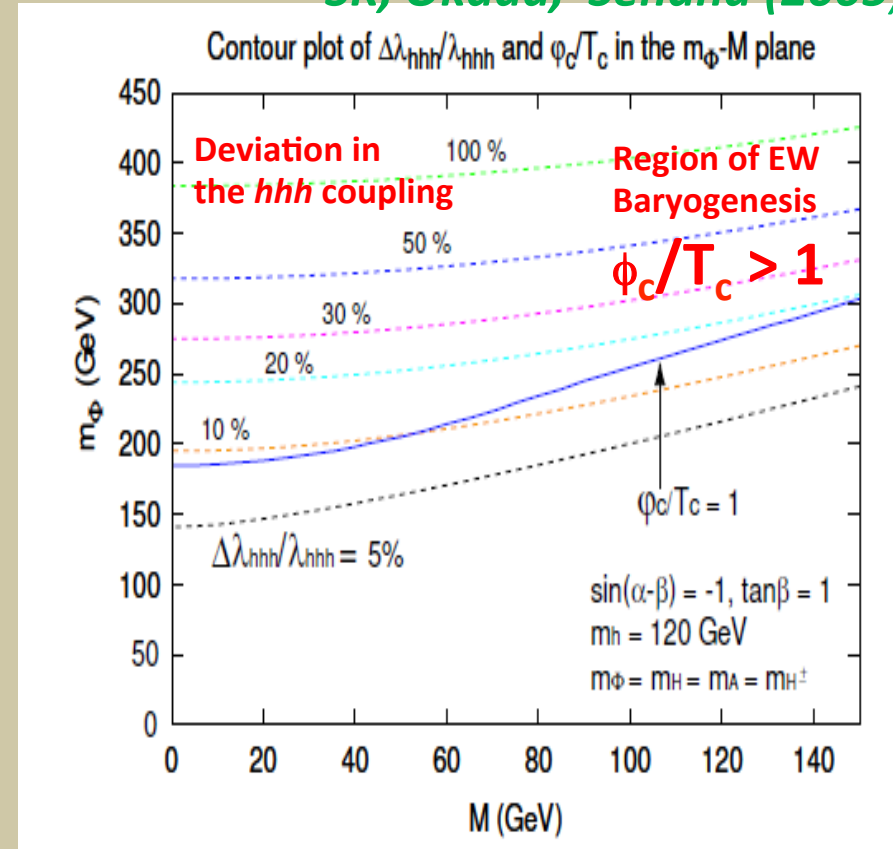
$$\phi_c/T_c > 1 \Rightarrow 2E/\lambda_{T_c} > 1$$

### EW Baryogenesis

↔ Non-decoupling effect

↔ large deviation in  $hhh$

SK, Okada, Senaha (2005)



If  $hhh$  can be measured by O(10) %, the scenario of EW Baryogenesis can be tested

Connection between cosmology and collider physics

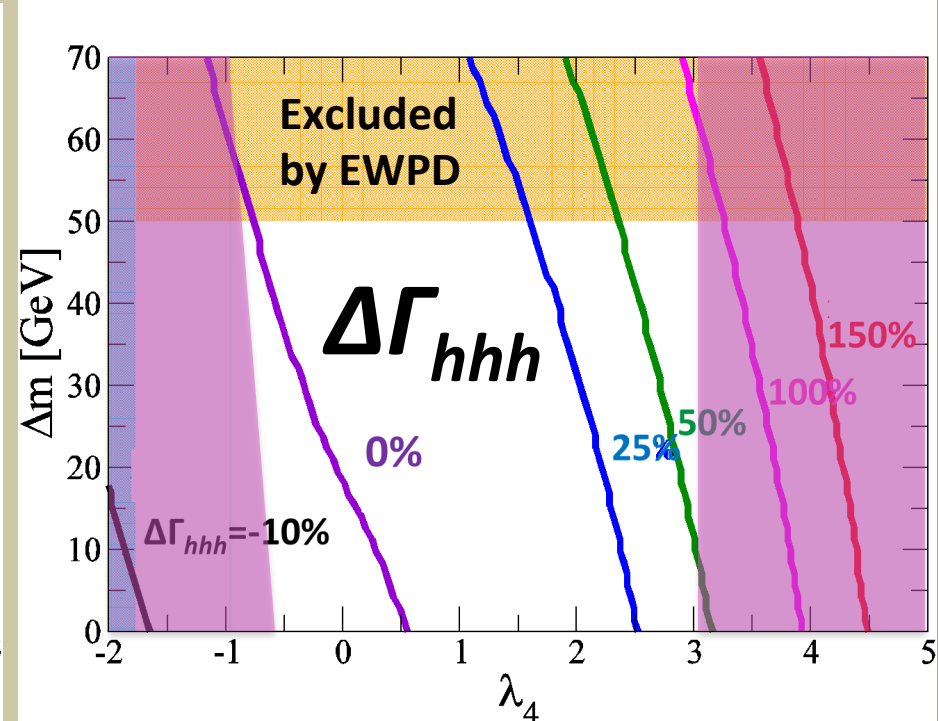
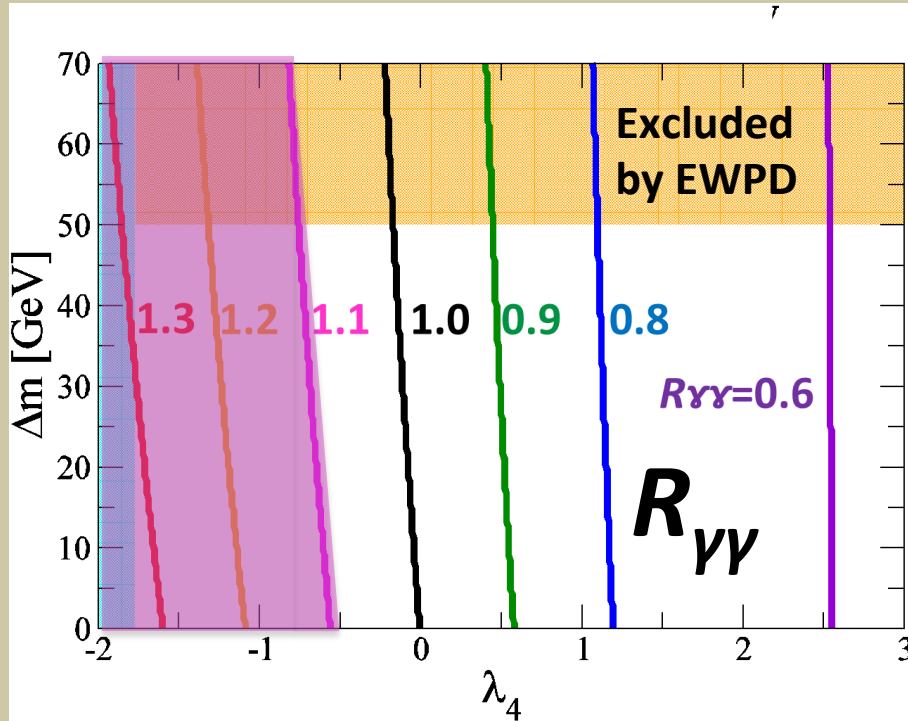
# Correlation between $h\gamma\gamma$ and $hhh$

Ex) Higgs Triplet Model (SM-like  $h$  + Triplet)

$$m_{H^{++}}=300\text{GeV}, v_{\Delta}=1\text{MeV}$$

$$\Delta m = m_{H^+} - m_{H^{++}}$$

$$R_{\gamma\gamma} = 0.8 \pm 0.3 \text{ (CMS)}$$

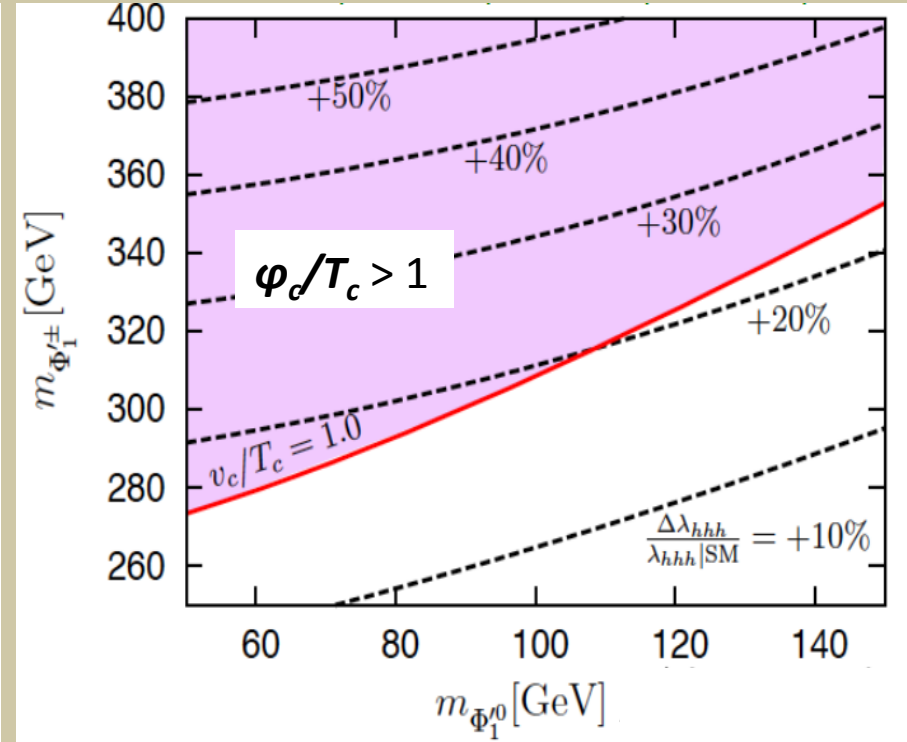
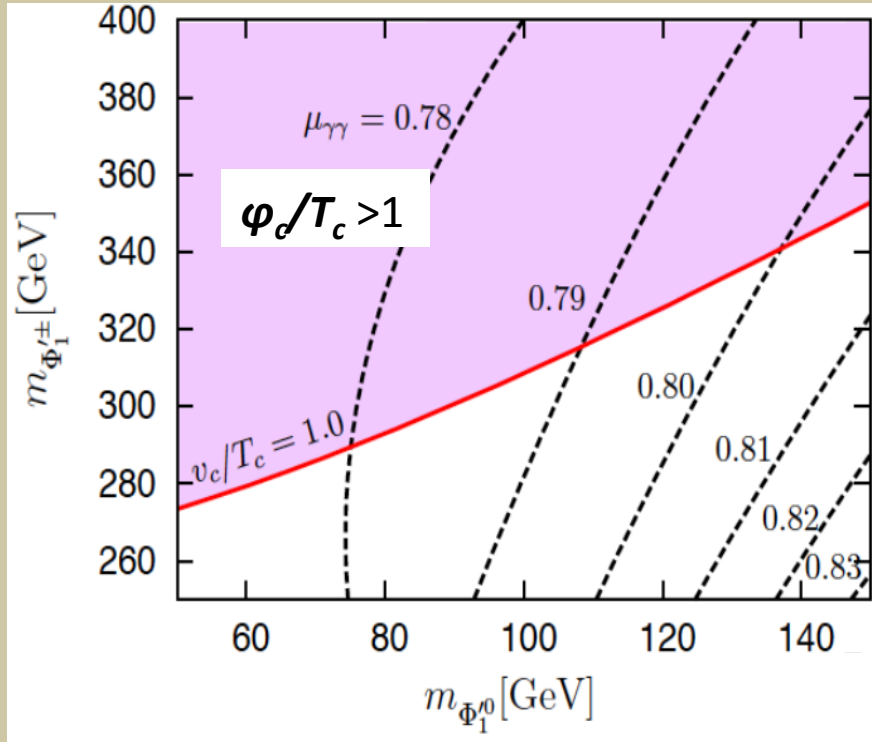


$$R_{\gamma\gamma} \equiv \frac{\sigma(gg \rightarrow h)_{\text{HTM}} \times \text{BR}(h \rightarrow \gamma\gamma)_{\text{HTM}}}{\sigma(gg \rightarrow h)_{\text{SM}} \times \text{BR}(h \rightarrow \gamma\gamma)_{\text{SM}}}$$

$$\Delta\Gamma_{hhh} \equiv \frac{\text{Re}\Gamma_{hhh} - \text{Re}\Gamma_{hhh}^{\text{SM}}}{\text{Re}\Gamma_{hhh}^{\text{SM}}}$$

# Correlation between $h\gamma\gamma$ and $hhh$

Ex) Strong-but-light scenario in the SUSY  $SU(2)_H$  Model for EWBG



Deviation in the  $h\gamma\gamma$  coupling is **-20%**  
 Deviation in the  $hhh$  coupling is **+20%**

# Properties of extra Higgs bosons

*$H, A, H^+, H^{++}$*

# MSSM (Type-II 2HDM)

SM-like Higgs  
 $m_h = 126$  GeV

$h$

$hVV: \sin(\beta - \alpha) \approx 1$

$$\sin(\beta - \alpha) \simeq 1 - \frac{2m_Z^4}{m_A^4 \tan^2 \beta}$$

Extra Higgs bosons

$H, A, H^\pm$

$HVV: \cos(\beta - \alpha) \ll 1$

$HAZ: \sin(\beta - \alpha) \approx 1$

$H^+H^-\gamma: 1$

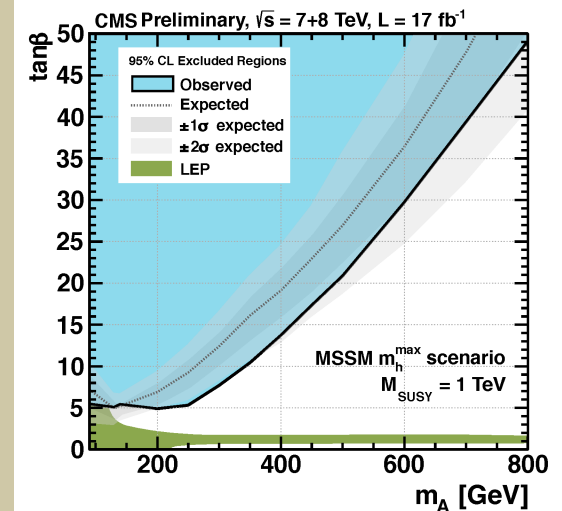
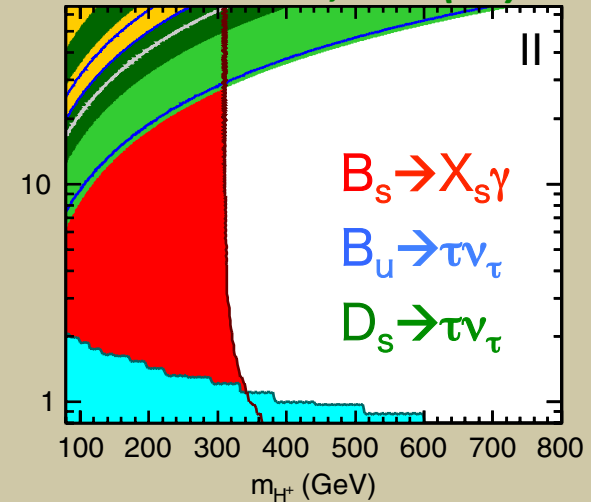
$Htt$  ( $A\tau\tau$ ):  $m_t \cot \beta$

$Hbb$  ( $A\tau\tau$ ):  $m_b \tan \beta$

$H\tau\tau$  ( $A\tau\tau$ ):  $m_\tau \tan \beta$

Flavor experiments and LHC give strong constraints on MSSM (Type-II 2HDM)

Mahmoudi, Stal (09)





# MSSM vs Type X 2HDM

**Type II:  $H, A$  decay into  $bb$**

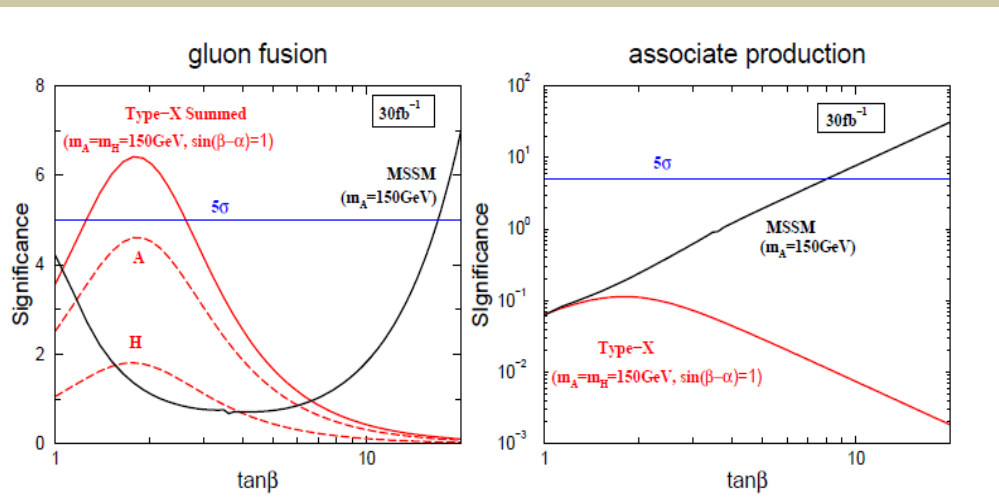
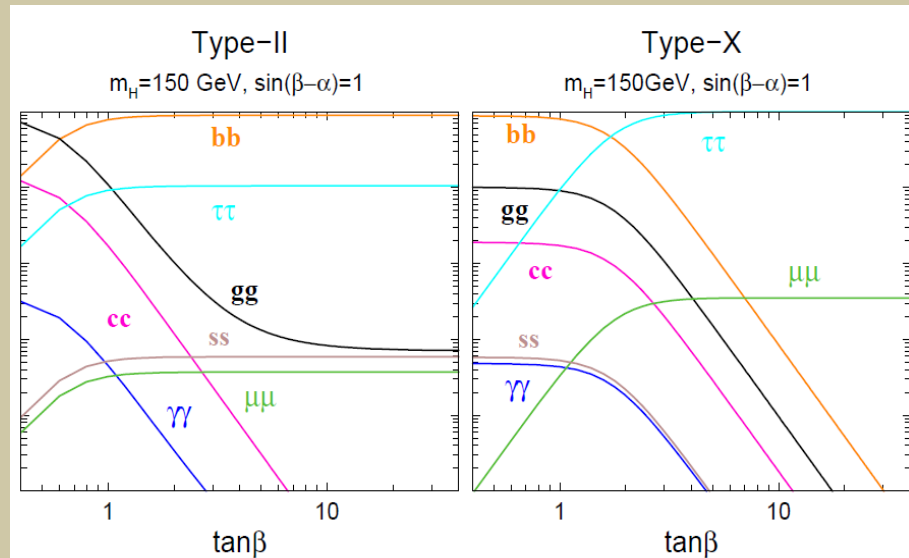
**Type X:  $H, A$  decay into  $\tau\tau$**

At LHC, **Type X 2HDM** can be discriminated from **MSSM (Type-II)** by the combination of  $\tau\tau$  gluon fusion

$$pp \rightarrow A (H) \rightarrow \tau\tau$$

and  $bb$  associate (H)A production

$$pp \rightarrow bbA (bbH)$$

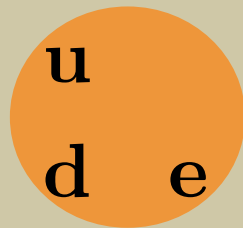
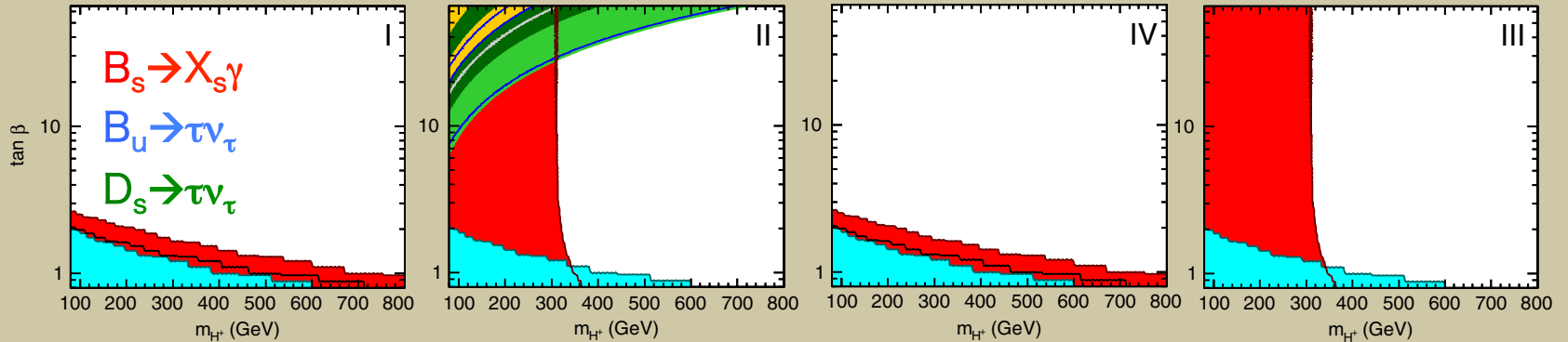


	$\xi^u$	$\xi^d$	$\xi^\ell$
Type-I	$1/\tan\beta$	$-1/\tan\beta$	$-1/\tan\beta$
Type-II	$1/\tan\beta$	$\tan\beta$	$\tan\beta$
Type-X	$1/\tan\beta$	$-1/\tan\beta$	$\tan\beta$
Type-Y	$1/\tan\beta$	$\tan\beta$	$-1/\tan\beta$

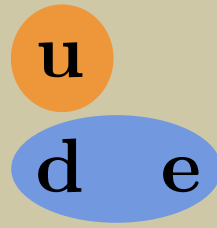
# Non-SUSY 2HDM

## Constraint from flavor physics

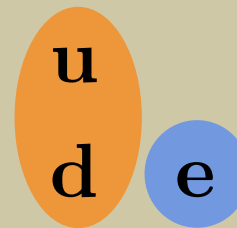
*Mahmoudi, Stal (09)*



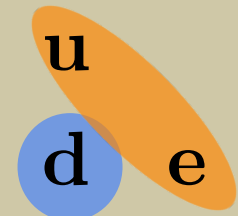
Type-I



Type-II



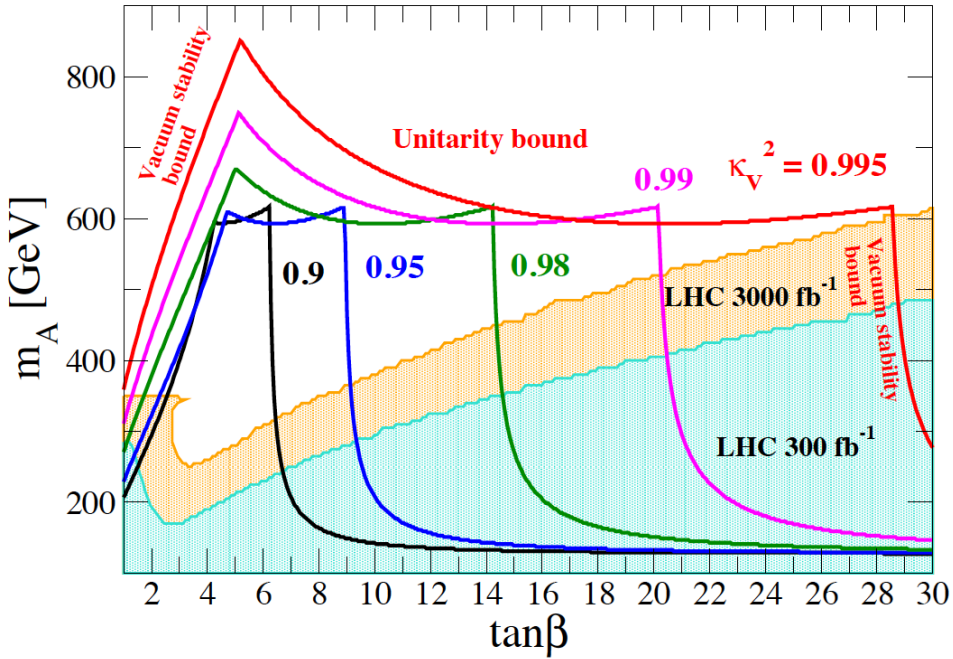
Type-X



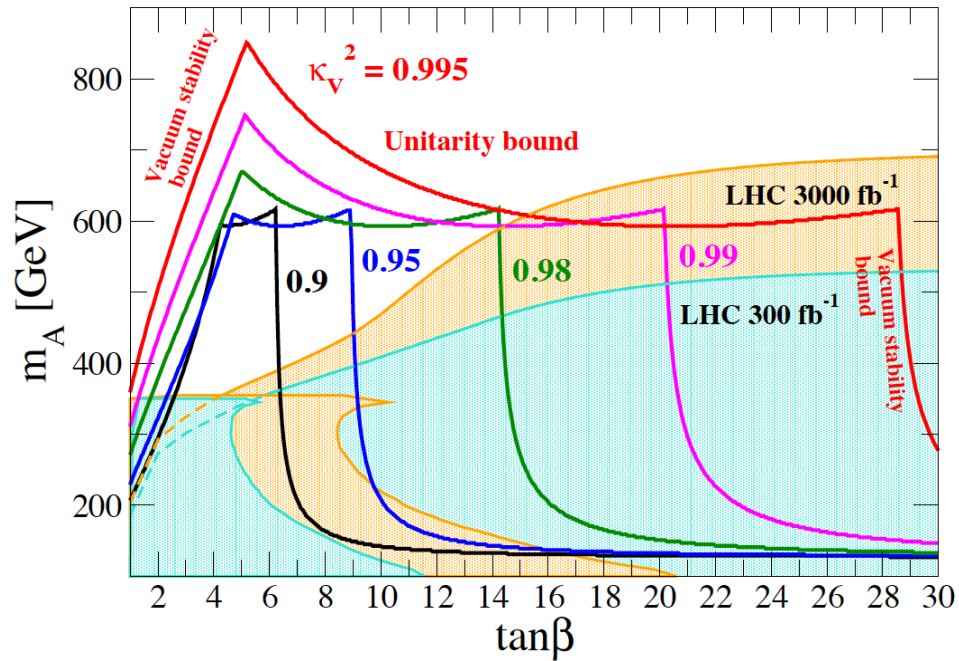
Type-Y

In Type-I and **Type-X**, **light**  $H, A, H^+$  can be allowed  
 $\Rightarrow$  **Pair Production**

Type-II THDM

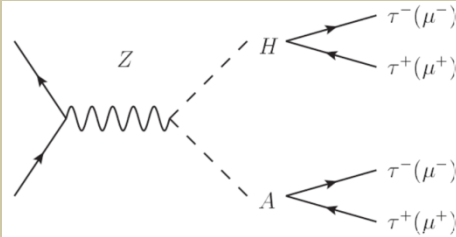


Type-X THDM



# HA Production (Type X 2HDM)

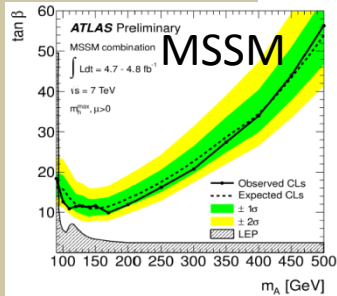
LHC



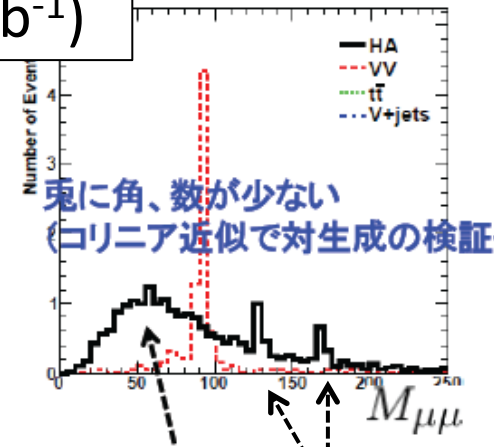
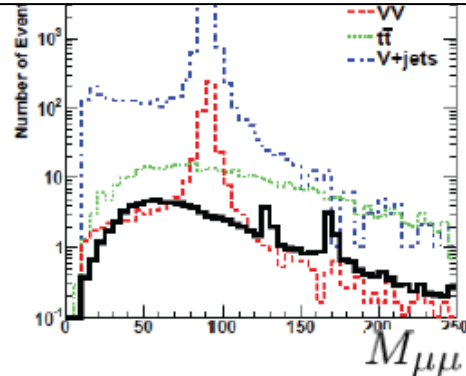
$$\sigma(pp \rightarrow HA) = \mathcal{O}(10-100) \text{ fb}$$

Differently from MSSM  
( $bbH, H \rightarrow \mu\mu, \tau\tau$ )

Rather hard to see Type-X at LHC



$\tau_h \tau_h \mu\mu$  event ( $100 \text{ fb}^{-1}$ )



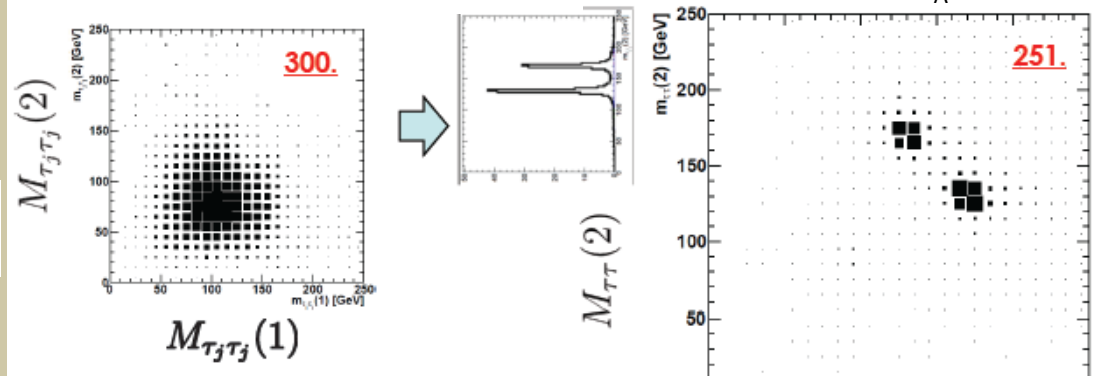
$4\tau \rightarrow 2\mu 2\tau_j$   
 $m_H = 130 \text{ GeV}$   
 $m_A = 170 \text{ GeV}$

ILC

HA can be reconstructed  
by collinear approximation

$$\vec{p}_\nu \simeq c \vec{p}_{\tau_j} \quad \vec{p}_{\tau_j} \simeq z \vec{p}_\tau = \frac{1}{1+c} \vec{p}_\tau$$

$4\tau_h$ event analysis	HA	VV	$t\bar{t}$	$S$ ( $100 \text{ fb}^{-1}$ )
Pre-selection	300.	10.6	1.2	38.
$0 \leq z_{1-4} \leq 1$	251.	6.2	0.1	38.
$(m_Z)_{\tau\tau} \pm 20 \text{ GeV}$	238.	1.8	0.	43.



Reconstruction of invariant  
masses of the two  $\tau$  systems is  
possible

SK, Tsumura, Yokoya (11)

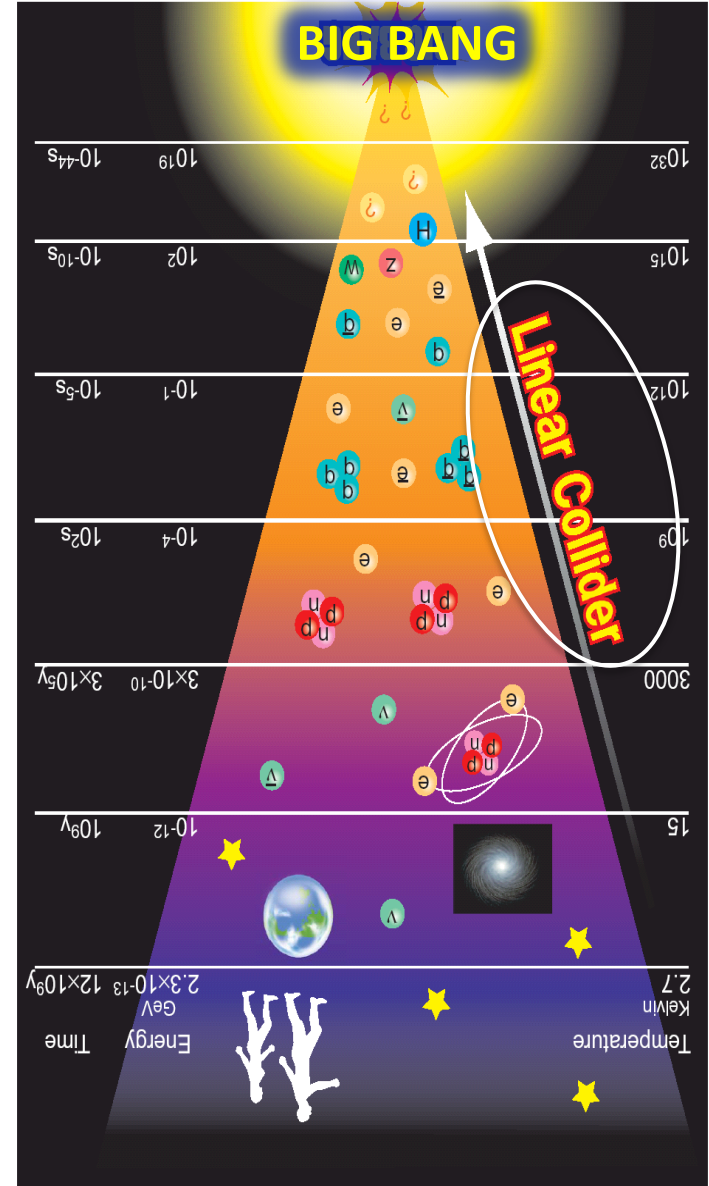
# Summary

- A SM-like Higgs boson  $h$  was discovered
- The Higgs sector remains unknown SM-like  $\neq$  SM

## Extended Higgs ( $\Leftrightarrow$ New Physics)

- Detailed study of  $h$  makes it clear the shape and dynamics of Higgs sector (**Finger printing models**)
- Direct Searches of  $H, A, H^+, H^{++}$  at LHC (and ILC)
- **Higgs is a good probe of new physics BSM!**

# We need LC



# ***Back Up Slides***

# Decoupling and heavy Higgs mass

Mass scales of  $H, A, H^\pm$  can be determined by precision measurements of the  $h$  couplings

**MSSM** ( $\alpha$  is a function of  $\tan\beta$  and  $m_A$ )

Ratio of branching ratios

$$R_{cc+gg/bb} \simeq \left( \frac{m_A^2 - m_h^2}{m_A^2 + m_Z^2} \right)^2 R_{cc+gg/bb}(SM)$$

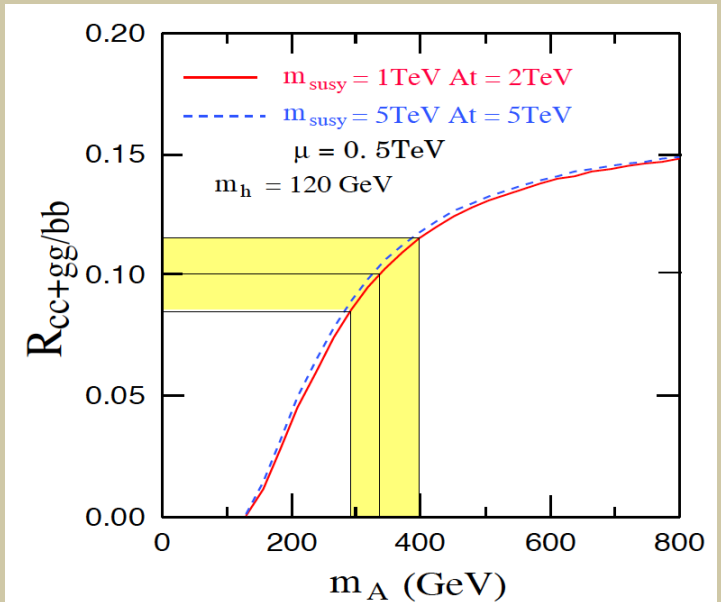
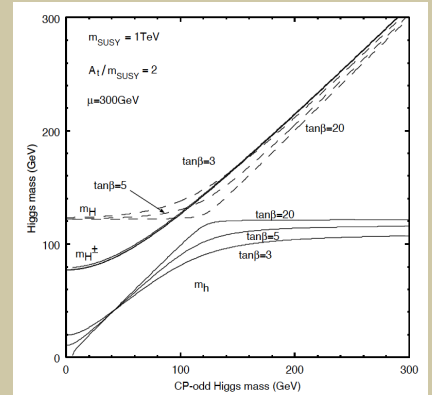
$\tan\beta=5$

$$\frac{g_{hVV}}{g_{SMVV}} \simeq 1 - 0.3\% \left( \frac{200 \text{ GeV}}{m_A} \right)^4$$

$$\frac{g_{htt}}{g_{SMtt}} = \frac{g_{hcc}}{g_{SMcc}} \simeq 1 - 1.7\% \left( \frac{200 \text{ GeV}}{m_A} \right)^2$$

$$\frac{g_{hbb}}{g_{SMbb}} = \frac{g_{h\tau\tau}}{g_{SM\tau\tau}} \simeq 1 + 40\% \left( \frac{200 \text{ GeV}}{m_A} \right)^2.$$

*Peskin et. al (2012)*



*Y. Okada (01)*



# SUSY and $m_h = 126\text{GeV}$

Higgs potential

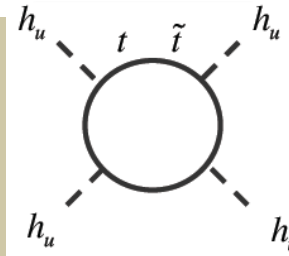
$$V = |D|^2 + |F|^2 + (\text{soft-breaking})$$

MSSM is type-II 2HDM ( $H_u, H_d$ )

Self-coupling comes from gauge couplings  $g, g' \Rightarrow m_h < m_Z$  at tree level

$$m_h^2 < m_Z^2 \cos^2 2\beta + \frac{3m_t^4}{2\pi^2 v^2} \left[ \ln \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{A_t^2}{m_t^2} \left( 1 - \frac{A_t^2}{12m_{\tilde{t}}^2} \right) \right]$$

Loop effect



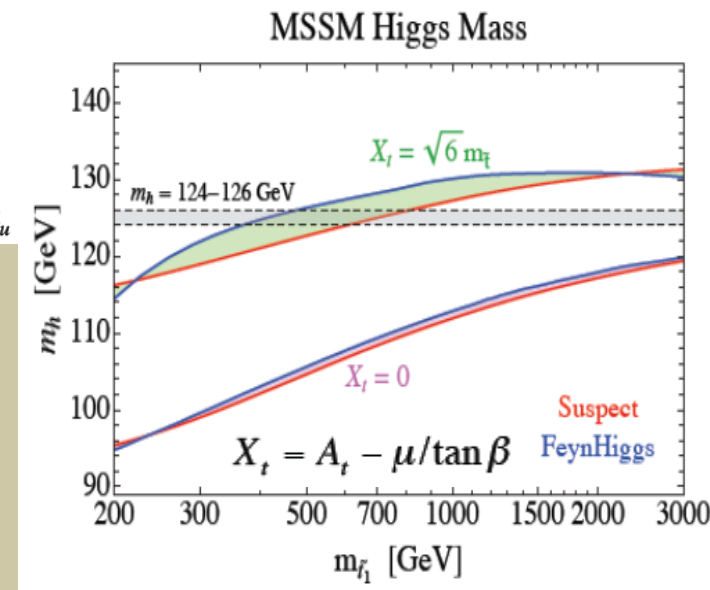
126 GeV can be realized by

Large Stop Masses OR Large Stop LR-mixing

$$M_{SUSY} \sim 10\text{TeV} (X_t=0)$$

Consistent with the data

But tension with Hierarchy Problem



Hall, Pinner, Ruderman (2011)

# Extended SUSY models

It is possible to gain  $m_h$  by NEW F-term, D-term or loop effects

$$m_h^2 = \left[ \text{Diagram 1} \right] + \left[ \text{Diagram 2} \right] \quad \text{MSSM}$$

Diagram 1: Tree-level Higgs mass contribution from  $D_{W,B}$  terms. It shows two vertices, each with two external  $h_u$  lines and a central dashed line labeled  $D_{W,B}$ . The vertices are labeled  $g_{1,2}$ .

Diagram 2: Tree-level Higgs mass contribution from the top quark loop. It shows a circle with four external  $h_u$  lines. The top quark ( $t$ ) and anti-top quark ( $\bar{t}$ ) are indicated on the top arc of the loop.

**F-term** +  $\left[ \text{Diagram 3} \right]$

Diagram 3: Tree-level Higgs mass contribution from the F-term. It shows two vertices, each with two external  $h_u$  lines and a central dashed line labeled  $F_S$ . The vertices are labeled  $\lambda$ .

**Addition of new Singlet, Triplet**

Ex) NMSSM

$$\Delta m_h^2 = \frac{\lambda_S^2 v^2}{2} \sin^2 2\beta$$

**D-term** +  $\left[ \text{Diagram 4} \right]$

Diagram 4: Tree-level Higgs mass contribution from the D-term. It shows two vertices, each with two external  $h_u$  lines and a central dashed line labeled  $D_{Z'}$ . The vertices are labeled  $g_X$ .

**New gauge symmetry  $U(1)_X$**

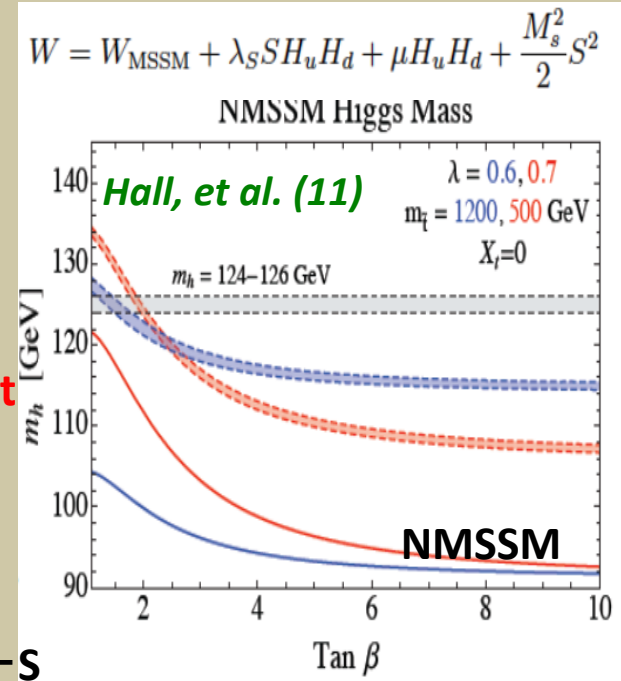
Ex) MSSM + RH-Neutrino + S + S

$$\Delta m_h^2 \simeq 2g_X^2 x^2 (v_{H_u}^2 + v_{H_d}^2) \cos^2(2\beta) \frac{2m_S^2}{2m_S^2 + m_{Z'}^2}$$

**Loop effect by new matter particles**

Ex) Strong-but-Light Scenario (for EWBG)

$$\Delta m_h^2 = \frac{3Y'^4 v^2}{4\pi^2} \ln \frac{m_S^2}{m_F^2}$$

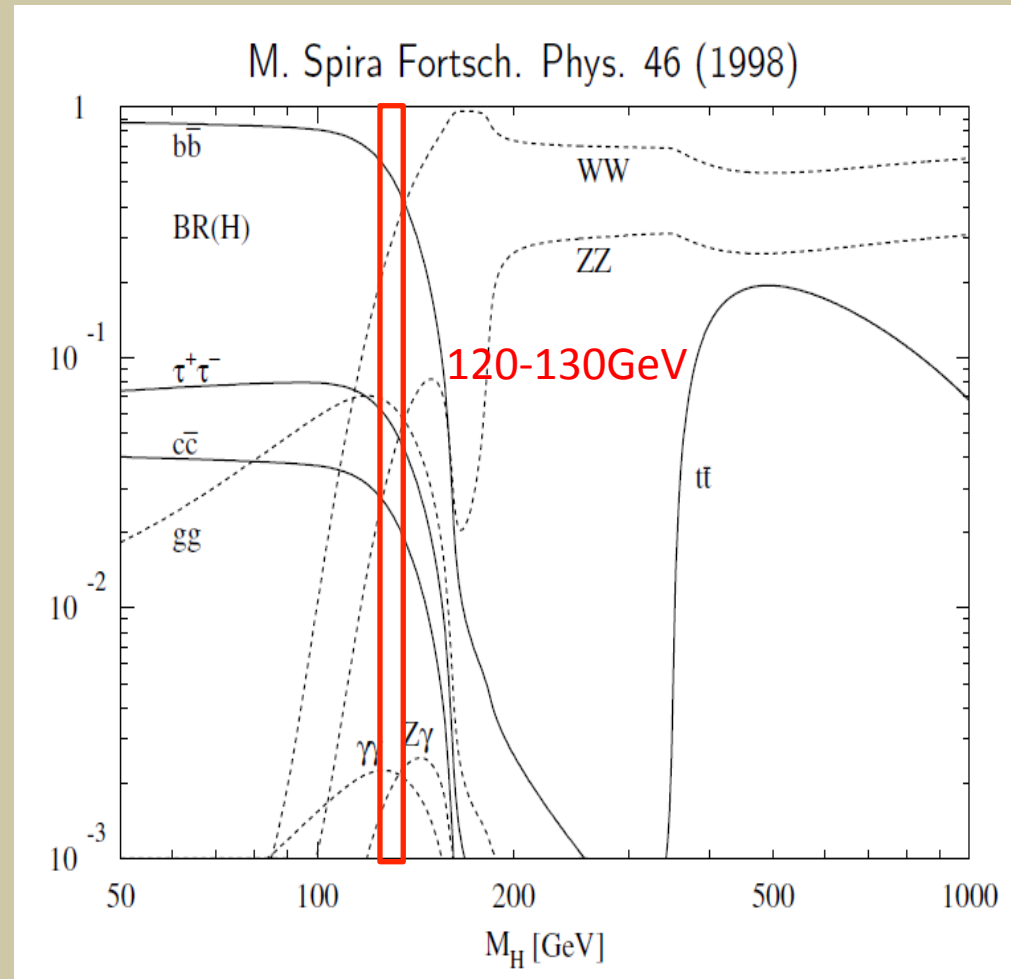


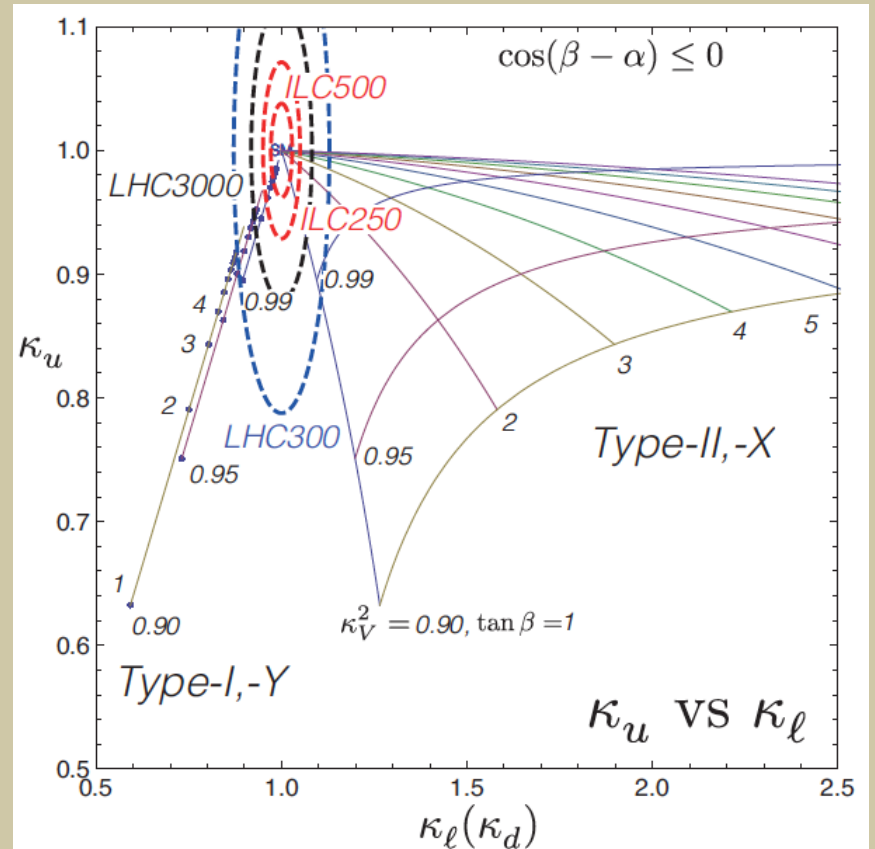
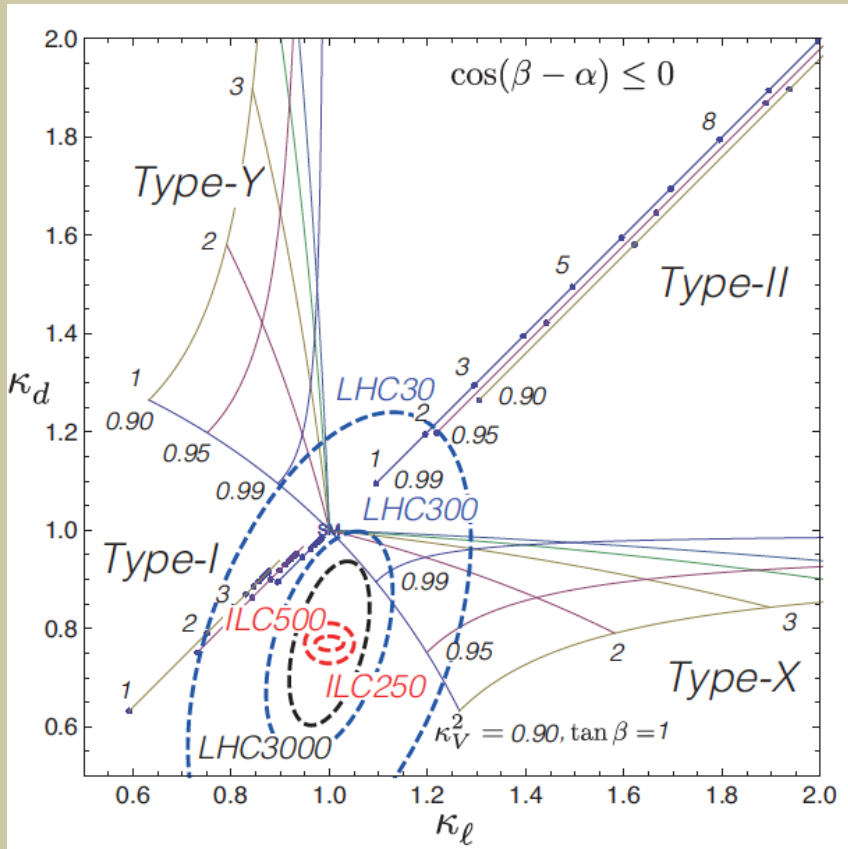
*Endo, Hamaguchi, Iwamoto, Yokozaki (11)*

*SK, Shindo, Yamada (12)*

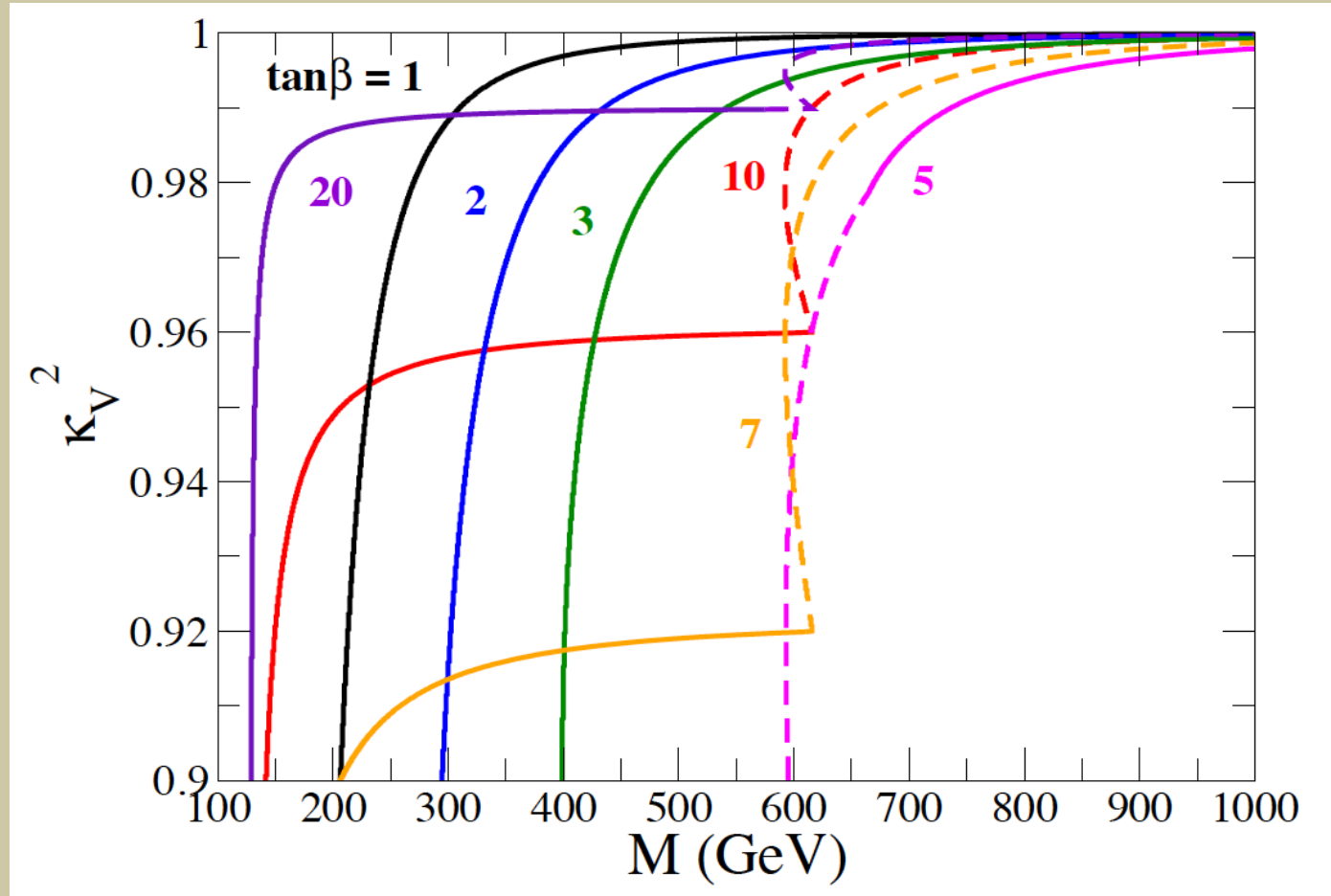
# Decay branching ratios of SM Higgs

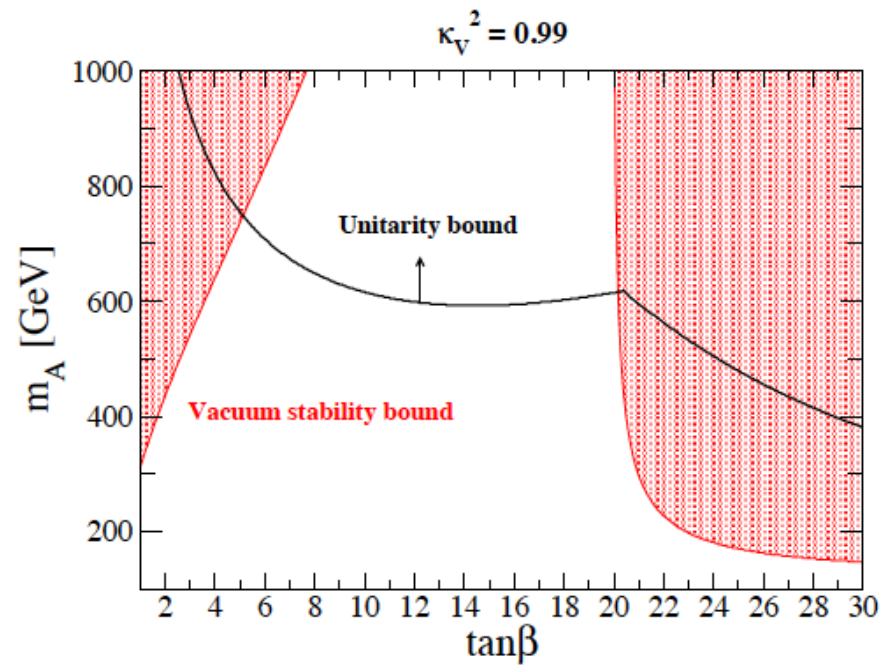
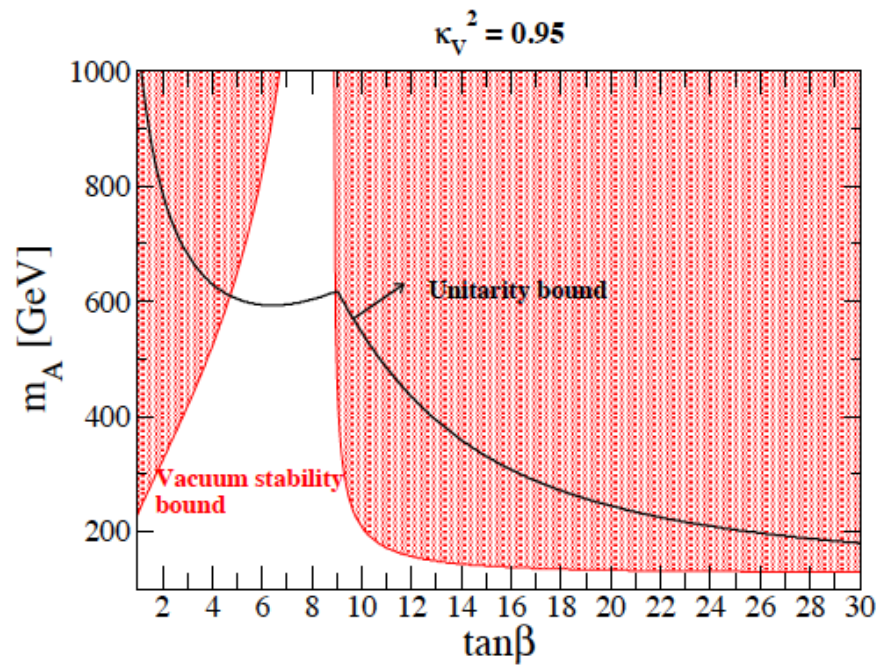
- SM Higgs couples to all the particles  
[ $h\gamma\gamma$ ,  $hgg$  (via loop)  
 $hh\nu\nu$  (dim-5)]
- For  $m_h=126$  GeV,  
various decay modes  
can be available



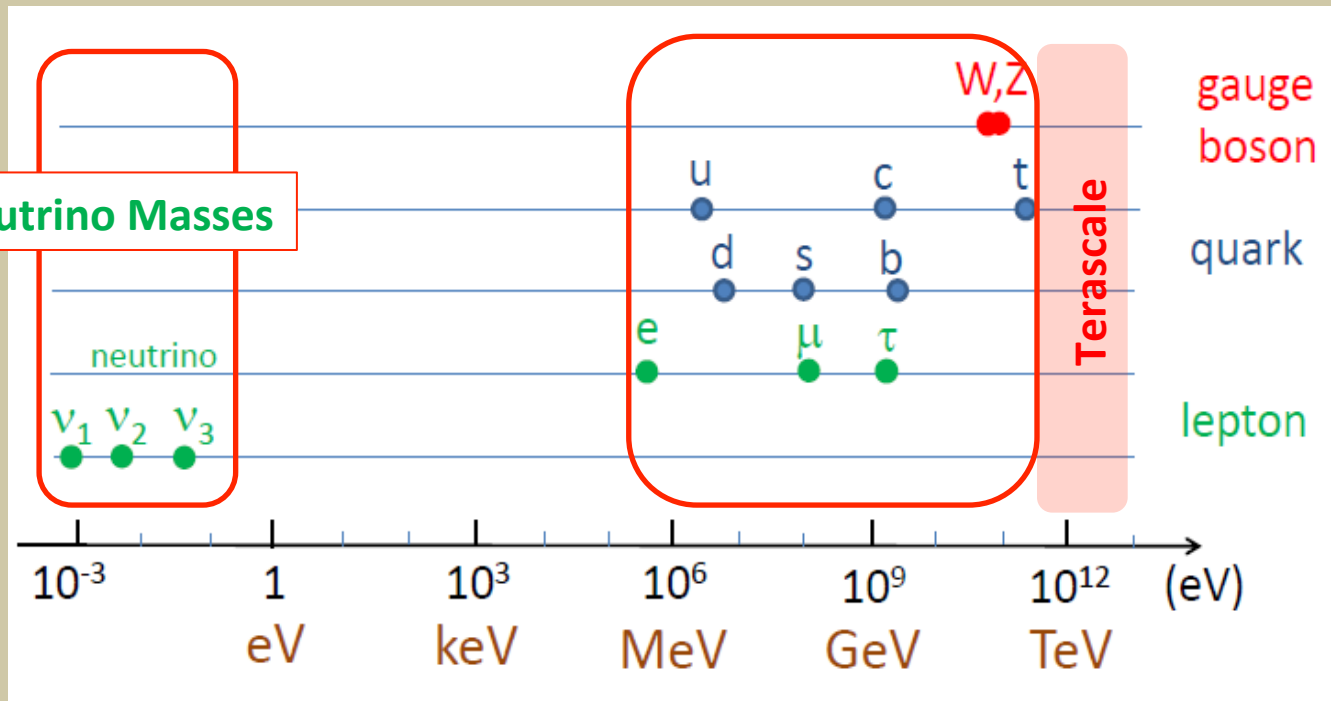


# Vacuum stability bound also important





# Mass spectrum of particles



Masses of particles are zero in the Lagrangian Vacuum gives masses to them by EWSB

# Radiative seesaw with $Z_2$

$Z_2$ -parity plays roles: 1. **No tree-level seesaw** (Radiative neutrino mass)  
2. **Stability** of the lightest  $Z_2$ -odd particle (WIMP)

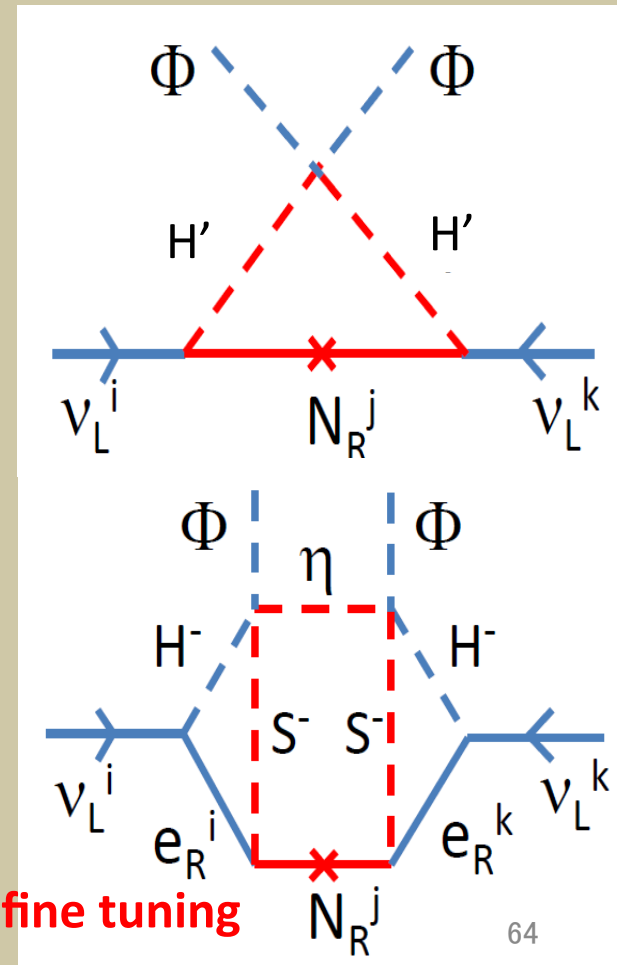
## Ex1) 1-loop Ma (2006)

- Simplest model
- SM +  $N_R$  + Inert doublet ( $H'$ )
- DM candidate [  $H'$  or  $N_R$  ]

## Ex2) 3-loop Aoki-SK-Seto (2008)

- Neutrino mass from  **$O(1)$**  coupling
- 2HDM +  $\eta^0$  +  $S^+$  +  $N_R$
- DM candidate [  $\eta^0$  (or  $N_R$ ) ]
- Electroweak Baryogenesis

All 3 problems may be solved by TeV physics w/o fine tuning



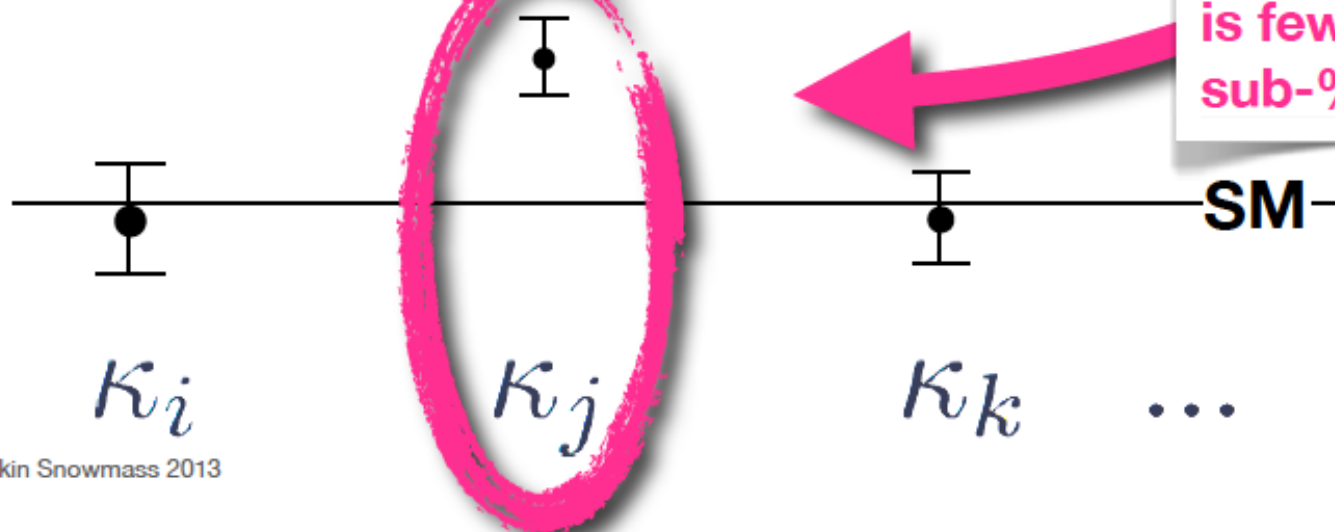


# precision for precision's sake?

No - this is a discovery search

	$\kappa_V$	$\kappa_b$	$\kappa_\gamma$
Singlet Mixing	$\sim 6\%$	$\sim 6\%$	$\sim 6\%$
2HDM	$\sim 1\%$	$\sim 10\%$	$\sim 1\%$
Decoupling MSSM	$\sim -0.0013\%$	$\sim 1.6\%$	$< 1.5\%$
Composite	$\sim -3\%$	$\sim -(3 - 9)\%$	$\sim -9\%$
Top Partner	$\sim -2\%$	$\sim -2\%$	$\sim -3\%$

Benchmark  
for discovery  
is few % to  
sub-%



# Gauge Couplings $hVV$

$$L = g \sin(\beta-\alpha) hVV + g \cos(\beta-\alpha) HVV$$

- Changed by mixing with the other scalars
- Sum-rule for a multi-doublet structure  $g_{hVV}^2 + g_{HVV}^2 = g_V^2$

$$\sin^2(\beta-\alpha) < 1 \Leftrightarrow (g_{hVV}/g_{hVV}^{\text{SM}})^2 < 1$$

- Higgs sector with an exotic representation

$$(g_{hVV}/g_{hVV}^{\text{SM}})^2 > 1 \text{ is also possible!}$$

$$\frac{g_{hVV}^{\text{THDM}}}{g_{hVV}^{\text{SM}}} = \sin(\beta - \alpha)$$

SM-like case  
 $\sin^2(\beta-\alpha) \approx 1$

Higgs triplet model  
Georgi-Machasek model  
Models with a septet field, ...

*Hisano, Tsumura (13)*

*SK, Kikuchi, Yagyu (13)*

# In the Higgs Triplet model

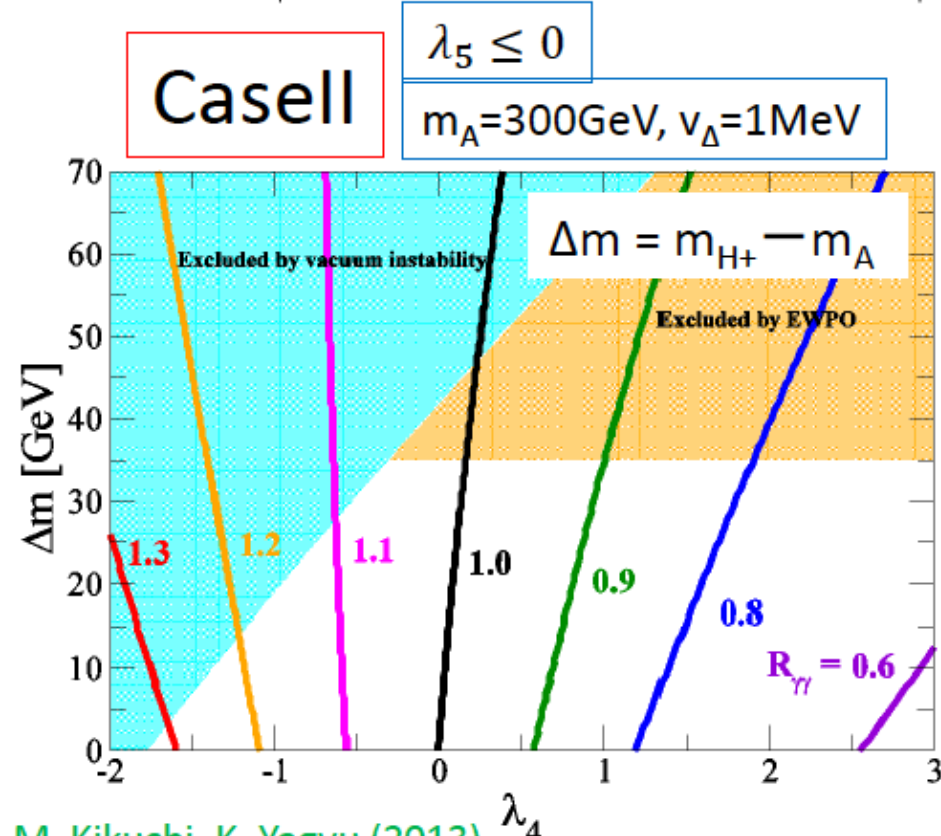
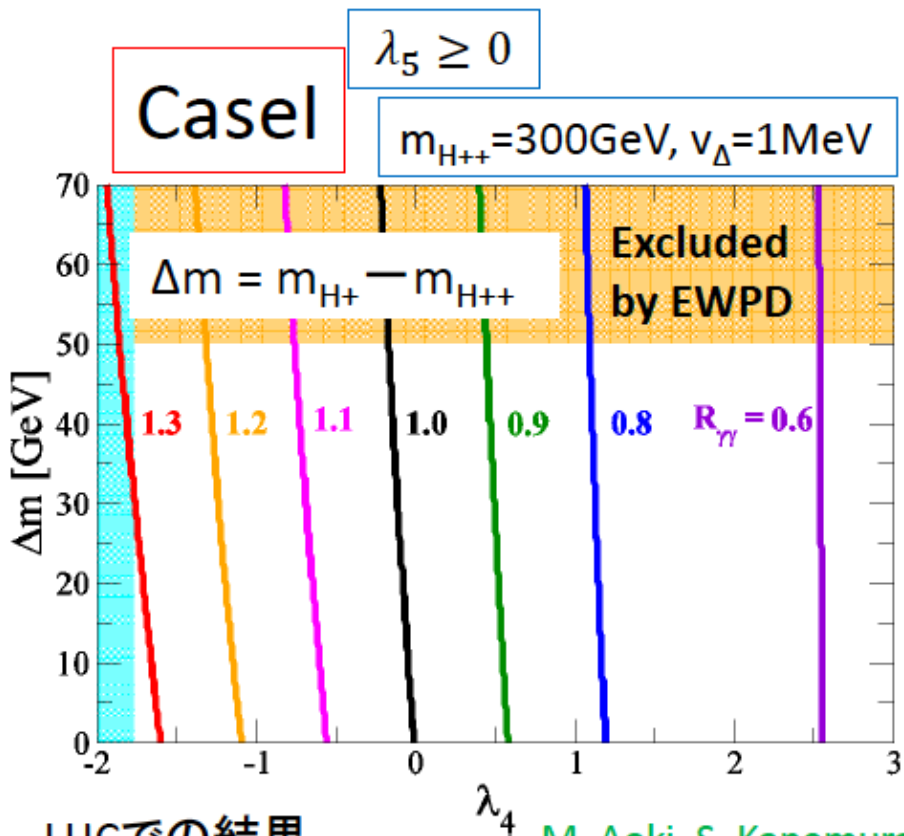
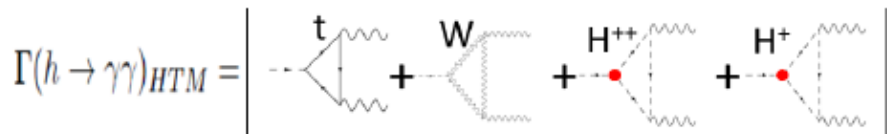
A. Arhrib, R. Benbrik, M. Chabab, G. Moultaka (2012); A. G. Akeroyd, S. Moretti (2012);

▶ イベント率  $h \rightarrow \gamma\gamma$

$R_{\gamma\gamma}$  は  $\lambda_4$  に依存する

$\lambda_{hH^{++}H^{--}} \approx -\lambda_4 v$   
 $\lambda_{hH^+H^-} \approx -(\lambda_4 + \frac{\lambda_5}{2})v$

$$R_{\gamma\gamma} \equiv \frac{\sigma(gg \rightarrow h)_{HTM} \times BR(h \rightarrow \gamma\gamma)_{HTM}}{\sigma(gg \rightarrow h)_{SM} \times BR(h \rightarrow \gamma\gamma)_{SM}}$$



LHCでの結果

$R_{\gamma\gamma}^{\text{exp}} = 0.5 - 1.1$   
 (CMS)

M. Aoki, S. Kanemura, M. Kikuchi, K. Yagyu (2013)

菊地真吏子さんの  
 のスライドより

# Introduction

$W_L^+ W_L^-$  Elastic Scattering

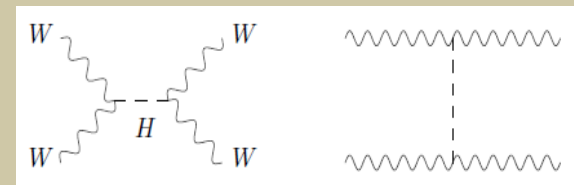
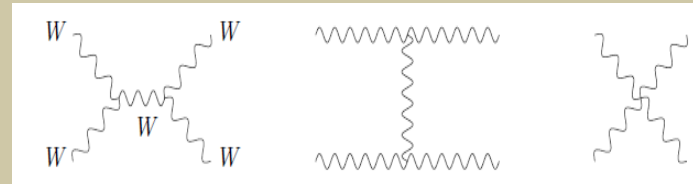
$$a^0(W_L^+ W_L^- \rightarrow W_L^+ W_L^-) \approx A E^4 + B E^2 + C \quad (E \rightarrow \infty)$$

Unitarity Violation if  $A, B \neq 0$

$A=0$  because of gauge symmetry

To make  $B=0$ , **diagrams mediated by a scalar field  $h$  must be added**

**Higgs field is required to save unitarity**



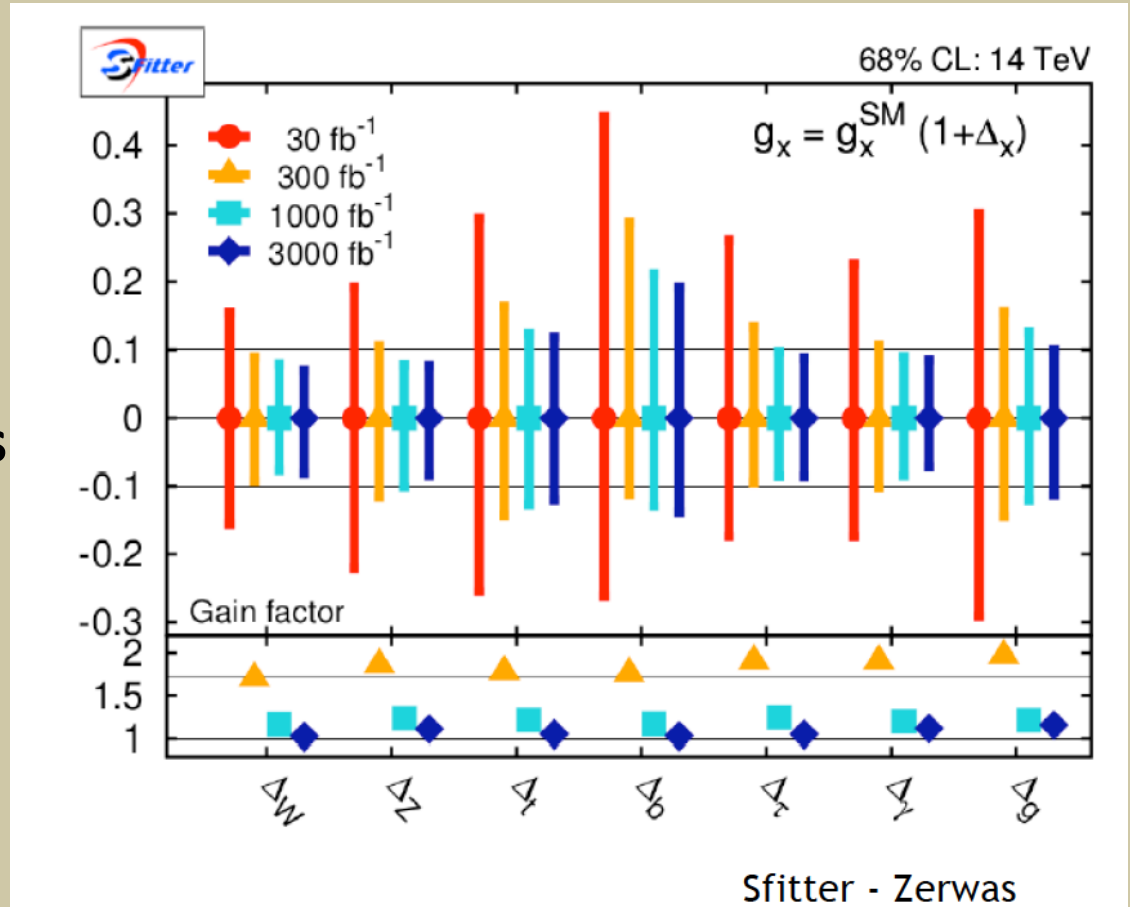
Perturbative Unitarity

$$|a^0(W_L^+ W_L^- \rightarrow W_L^+ W_L^-)| < 1 \Rightarrow m_h < 1.2 \text{ TeV}$$

# Higgs coupling measurement at the LHC

Accuracy is typically  
 $O(10)$  %

Not very well improved  
for  $300 \rightarrow 3000 \text{ fb}^{-1}$   
due to systematic errors



# Fingerpointing the model (Exotics)

SK, K. Tsumura, K. Yagyu, H. Yokoya 2013

Universal Fermion  
Coupling ( $\kappa_F$ )

VS

$hVV$  coupling ( $\kappa_V$ )

Exotic models  
predict  $\kappa_V > 1$

We can discriminate  
Exotic models

Ellipse = 68.27% CL

