

# Minimal Dark Matter and Direct Detection as a Probe of Reheating

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10/22/2013 @ Tohoku Forum for Creativity

Based on arXiv:1310.xxxx (B.Feldstein, MI, T.T.Yanagida)

# Introduction

## ✓ What do we learn from the discovery?

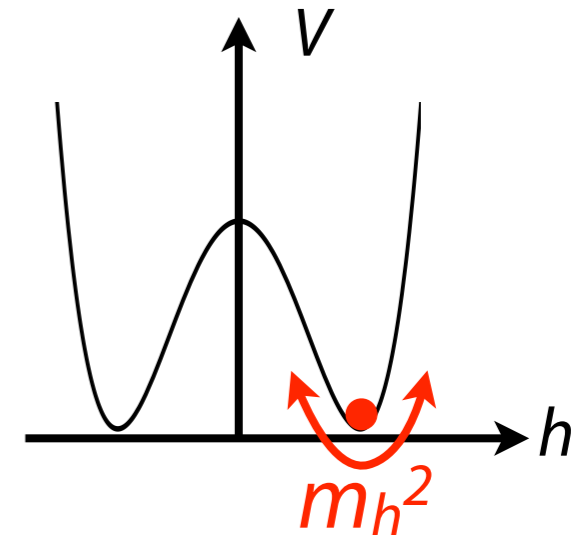
1. Higgsless models are almost excluded !
2. Higgs is more like an **elementary** scalar !

In the simplest implementation...

$$V = - m_{higgs}^2/2 h^\dagger h + \lambda/4 (h^\dagger h)^2$$

$$m_{higgs} = \lambda^{1/2} v \quad [v=174.1\text{GeV}]$$

$$m_{higgs} \sim 125\text{GeV} \longrightarrow \lambda \sim 0.5$$



- ## ✓ The quartic coupling $\lambda$ is small and this simple elementary scalar Higgs description works consistently !

**The Minimal Standard Model works !**

# Introduction

## ✓ Naturalness ?

The mass of the elementary Higgs boson is not protected by any symmetries...

Why  $m_{higgs}^2 \ll M_{GUT}^2, M_{PLANCK}^2$  ?

- ✓ It is quite reasonable to expect new physics behind the Standard Model at around  $O(100)GeV - O(1)TeV$ !
  - ✓ Supersymmetric Standard Models ?
  - ✓ Extra Dimensional Models ?
  - ✓ Composite Higgs Models ?

These are very exciting possibilities to be tested at the  $14TeV$  run of the LHC, at the ILC, at the  $100TeV$  collider experiments !

# Introduction

- ✓ So far, we have no direct observational data which support these possibilities from collider experiments...

cf.) No supersymmetric particles have been discovered at the LHC ;

squark/gluino mass  $> 1.8 \text{ TeV}$

gluino mass  $> 1.4 \text{ TeV}$  for squark  $\gg \text{TeV}$

Negative pressure on Supersymmetry as a solution to the  
*Naturalness problem...*

⚠ We have no imminent need to give up the *Naturalness problem* as a guiding ~~principle~~ *strategy* at all.

As Andrew emphasized in his talk, we might need to start thinking differently.

The success of the simplest Higgs mechanism might suggest that *Simplicity* is a more important guiding strategy in constructing models of new physics...

What can we think of if we impose *Simplicity* on dark matter ?

# Introduction

- ✓ We take  $SU(2)_L$  charged dark matter, so-called minimal dark matter, as an example of *Simple* dark matter model.

$Y \neq 0$ : hypercharged minimal dark matter  
→ a viable *WIMPZILLA* candidate for  $M_{DM} > 10^7 \text{ GeV}$ .

- ✓ Next generation direct detection experiments reach to  $M_{DM} = 10^{10-11} \text{ GeV}$ .
- ✓ Through the direct detection experiments we can determine the reheating temperature to  $T_R \sim 10^{7-9} \text{ GeV} (M_{DM}/2 \times 10^{10} \text{ GeV})$ .

[ cf.  $Y = 0$ : minimal dark matter [’05 Cirelli, Fornengo, Strumia ]

→ a viable WIMP candidate but difficult to be detected at direct detection experiments ]

# Putting *Simplicity* on Dark Matter

## ✓ How to impose *Simplicity* on the dark matter sector ?

No unique definition of simplicity...

There are tons of ways...,

## ✓ Let us explore the extreme cases :

The dark sector consists of just **a single new particle** with the charges under the Standard Model gauge group.

[cf. neutral single dark matter with new higgs interactions

('04 Davoudiasl, Kitano, Li, Murayama; Joseph's talk)]

## ✓ (Integer) Charged dark matter

Neutron star lifetime ['90 Gloud et.al.],

$$\rightarrow M_{DM} > O(10^{17}) \text{ GeV [e.g. '01 Perl et.al.]}$$

## ✓ Colored dark matter (SIMP)

constrained by direct detection experiments, Earth heating

$$\rightarrow M_{DM} > O(10^{16}) \text{ GeV [e.g. '07 Mack et.al.]}$$

# Putting *Simplicity* on Dark Matter

## ✓ How about $SU(2)_L$ charged dark matter ?

The dark matter particle is the neutral component in  $k$ -tuple of  $SU(2)_L$  with  $U(1)_Y$  hypercharge  $Y$ .

$$Q = T_3 + Y = 0$$

ex) doublet ( $k = 2$ ) :  $|Y| = 1/2$       triplet ( $k = 3$ ) :  $|Y| = 0, 1$   
quartet ( $k = 4$ ) :  $|Y| = 1/2, 3/2$       quintet ( $k = 5$ ) :  $|Y| = 0, 1, 2$

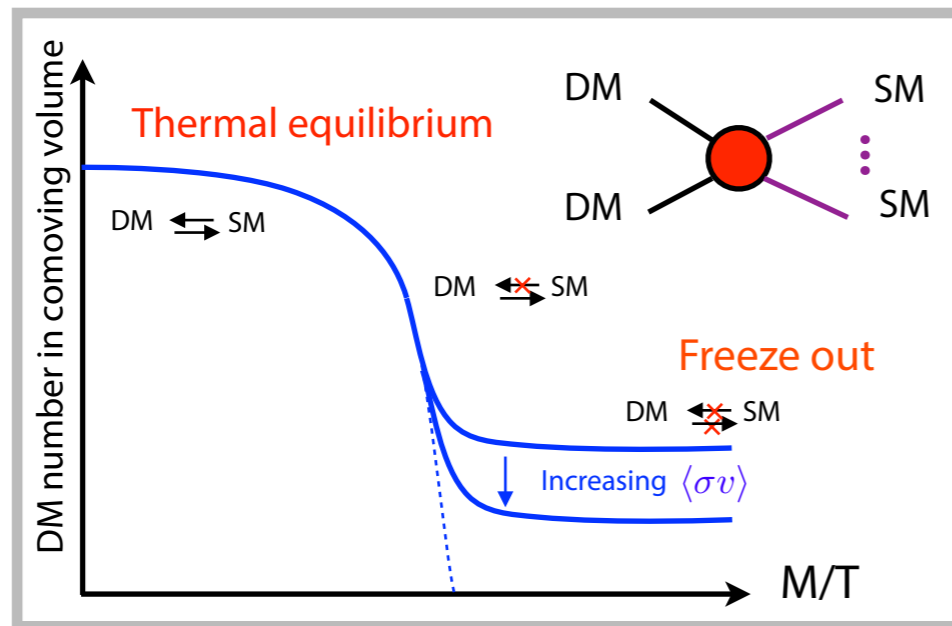
$SU(2)_L$  charged dark matter  $\left\{ \begin{array}{l} Y = 0 : \text{minimal dark matter} \\ Y \neq 0 : \text{hypercharged minimal dark matter} \end{array} \right.$  [’05 Cirelli, Fornengo, Strumia ]

**Stability?** We simply assume there is a  $Z_2$  symmetry.

For  $k > 5$  (7), fermionic (scalar) dark matter is automatically stable due to an accidental symmetry [’05 Cirelli, Fornengo, Strumia ]...

# Putting *Simplicity* on Dark Matter

- ✓  $SU(2)_L$  charged dark matter can be a good candidate of weakly interacting massive particle (WIMP)!



- DM is **in thermal equilibrium** for  $T > M_{DM}$ .
- For  $M_{DM} < T$ , DM is no more created
- DM is still annihilating for  $M_{DM} < T$  for a while...
- DM is also diluted by the cosmic expansion
- DM cannot find each other and stop annihilating at some point
- DM number in comoving volume is **frozen**

The WIMPs works for the annihilation cross section:  $\langle\sigma v\rangle \sim 10^{-9} \text{GeV}^{-2}$

$$\Omega_{DM} h^2 \simeq 0.1 \times \left( \frac{10^{-9} \text{GeV}^{-2}}{\langle\sigma v\rangle} \right)$$

- ✓ Minimal dark matter annihilate into the vector bosons and the fermions!

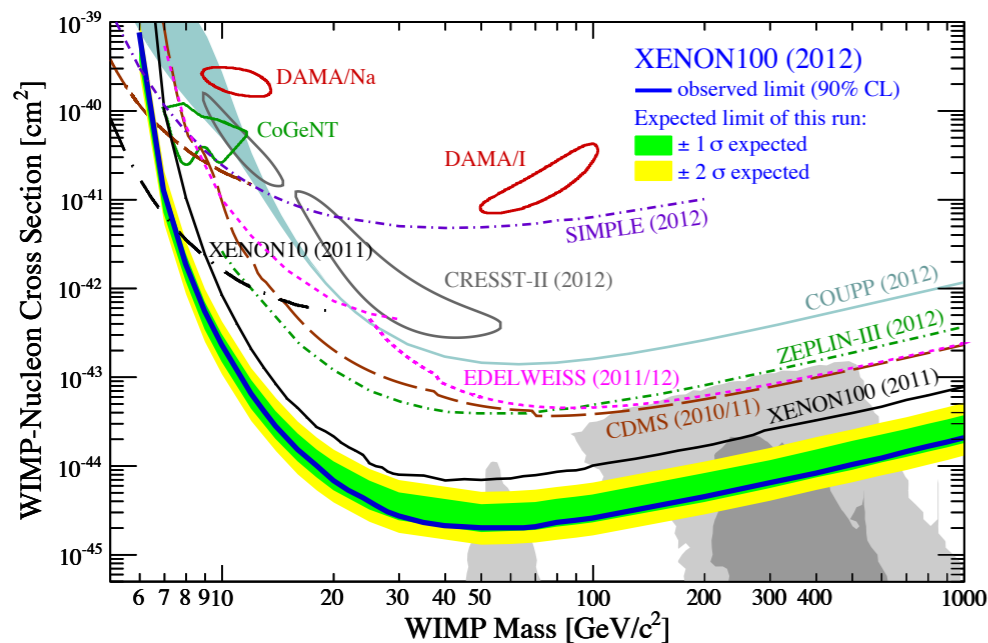
$$\langle\sigma v\rangle \simeq \frac{(g_2^4(2 + 17k^2 - 19) + 4Y^4 g_Y^4(41 + 8Y^2) + 16g_2^2 g_Y^2(k^2 - 1))}{256k\pi k M_{DM}^2}$$

→ good candidate for the WIMP for  $M_{DM} = O(1) \text{TeV}$ !



# Hypercharged Minimal Dark Matter

- ✓ Direct dark matter detection experiments have put severe constraints on hypercharged minimal dark matter!



Nucleus scattering rate via Z-boson exchange

$$\sigma_{\chi N} = \frac{G_F^2 \mu_N^2}{2\pi} Y^2 (N - (1 - 4 \sin^2 \theta_W) Z)^2$$

(x4 for scalar DM)

$G_F$ : Fermi constant,  $(N, Z)$  # of  $(n, p)$

The strongest limit from the XENON100 experiment:

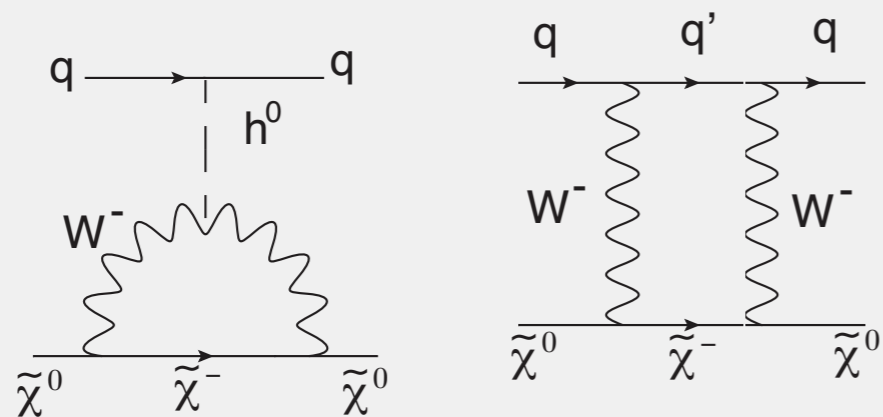
$$\sigma_{\chi \text{Xe}} \gtrsim 6 \times 10^{-36} \text{cm}^2 \times \left( \frac{M_{\text{DM}}}{1 \text{ TeV}} \right) \rightarrow M_{\text{DM}} > 30 \text{ PeV} \times (2Y)^2$$

Hypercharged minimal dark matter cannot be a **WIMP** candidate...

# Hypercharged Minimal Dark Matter

For comparison...

- ✓ Direct dark matter detection experiments of minimal dark matter ( $Y=0$ )
- ✓ The scattering is highly suppressed at the tree-level, due to the absence of tree-level interactions with  $Z$  nor Higgs.
- ✓ At the higher loop level, the cross section on a nucleon is estimated to be  $O(10^{-47})\text{cm}^2$ , which is two-orders of magnitude smaller than the current limit...



One-loop diagrams which contribute to the triplet DM-nucleon scatterings.  
[’10 Hisano, Ishiwata, Nagata]

Minimal dark matter ( $Y=0$ ) is a viable candidate of the **WIMP** !

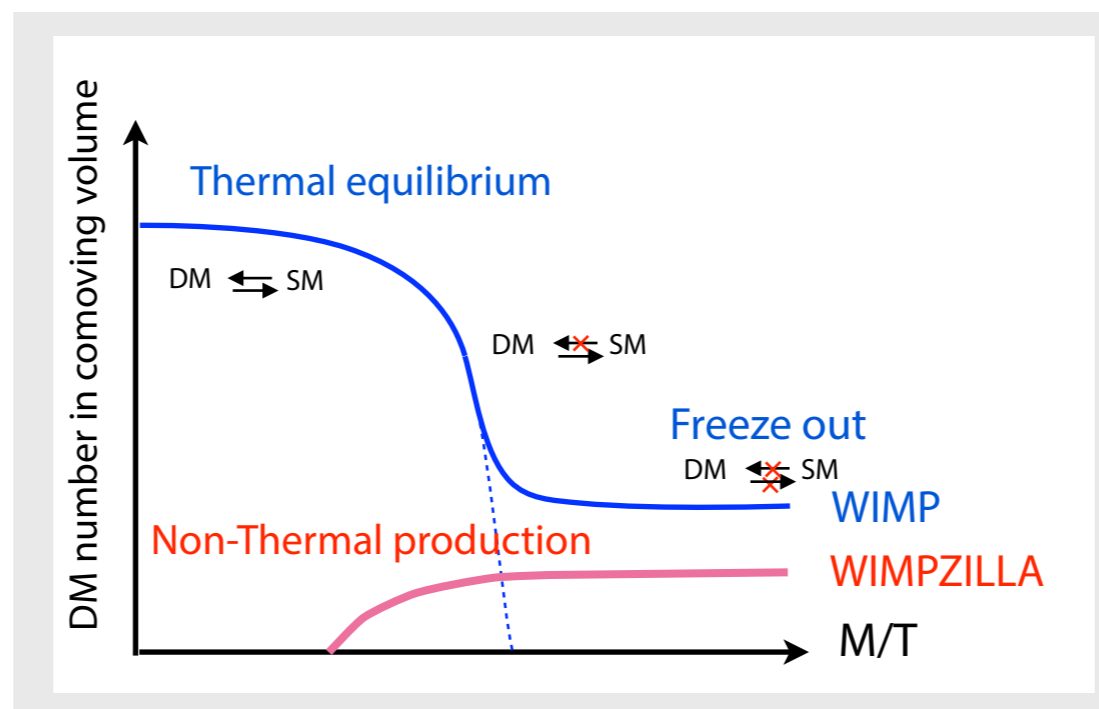
# Hypercharged Minimal Dark Matter

$SU(2)_L$  charged dark matter

}	$Y = 0$ : minimal dark matter → a viable <b>WIMP</b> candidate !
	$Y \neq 0$ : hypercharged minimal dark matter → excluded as a <b>WIMP</b> candidate !

Are hypercharged minimal dark matter scenarios excluded ?

- ✓ Let us **simply** discard the assumption that dark matter has attained thermal equilibrium after inflation...
- ✓ Instead, let us assume that the dark matter density is determined by a delicate choice of the dark matter mass and the temperature after inflation assuming  $M_{DM} > T_R$ .



# Hypercharged Minimal Dark Matter

$SU(2)_L$  charged dark matter

{	$Y = 0$ : minimal dark matter
	$Y \neq 0$ : hypercharged minimal dark matter

→ a viable **WIMP** candidate !

→ excluded as a **WIMP** candidate !

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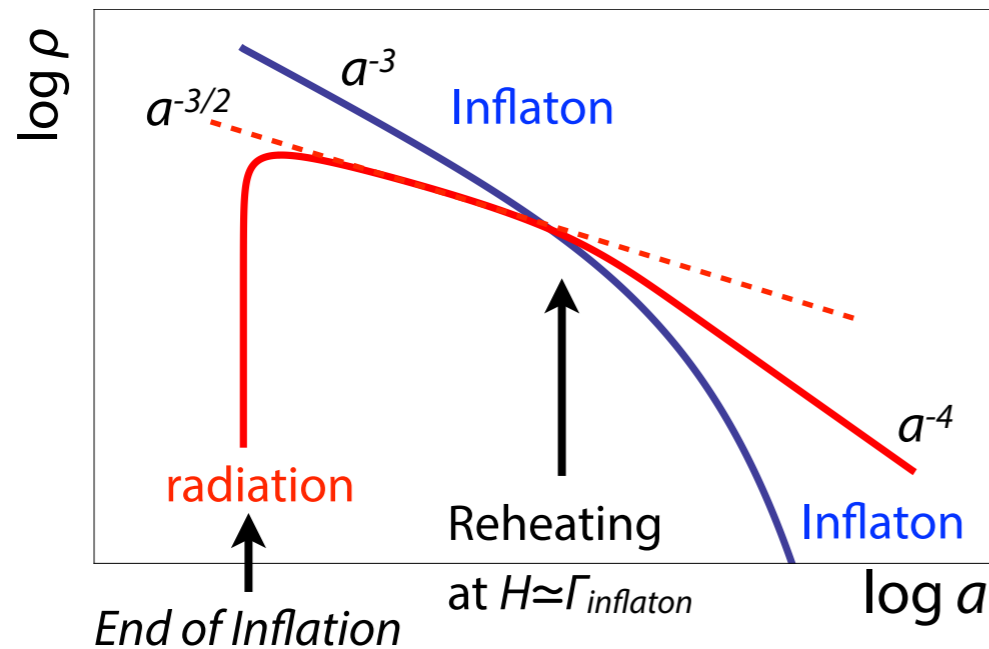
Hypercharged minimal dark matter is revived as the so-called **WIMPZILLA** without extending the dark matter sector at all!

[ WIMPZILLA ['98 Kolb, Chung, Riotto]: weakly interacting *very heavy* dark matter ]

Hypercharged minimal dark matter can be also revived by introducing mass splitting between Dirac neutral components to avoid the constraint from direct detection experiments... no more Simple though.

# Hypercharged Minimal Dark Matter

✓ Dark Matter production during reheating between  $T_{MAX}$  and  $T_R$



During reheating

✓  $H = H_R (a/a_R)^{-3/2}$

✓  $T = T_R (a/a_R)^{-3/8}$

After reheating

✓  $H = H_R (a/a_R)^{-2}$

✓  $T = T_R (a/a_R)^{-1}$

$$T_{MAX} = T_R (H_{inf}/H_R)^{1/4}$$

[ When the inflaton feels significant back-reaction from the thermal bath, the evolutions of  $\rho_{inflaton}$  and  $\rho_R$  get more complicated...

(e.g. '12 Mukaida & Nakayama) ]

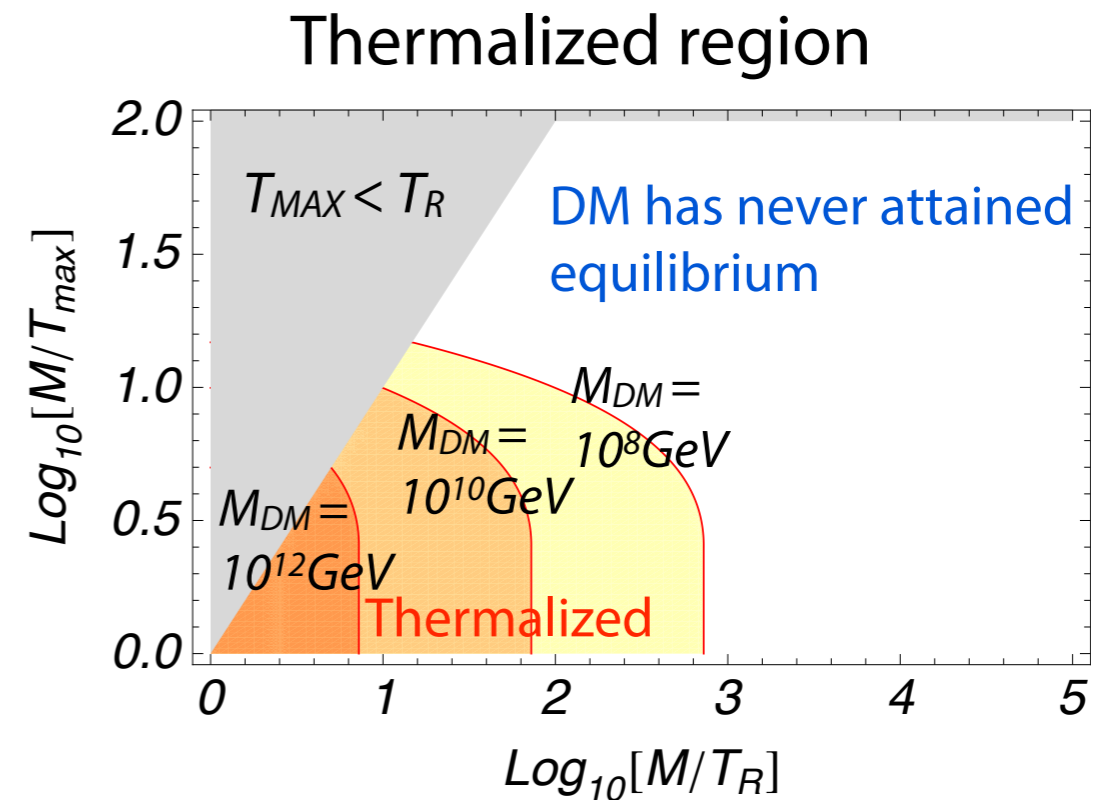
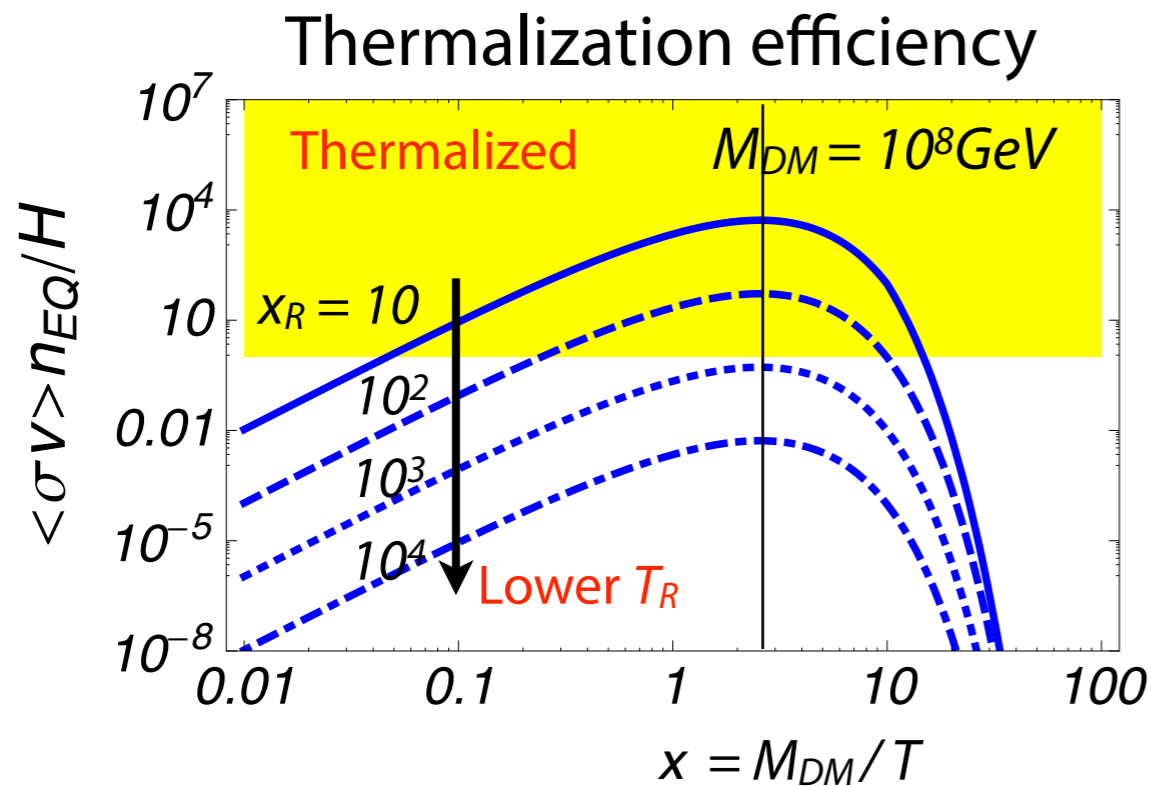
Boltzmann Equation :

$$\frac{d}{dt}n + 3Hn = - \langle \sigma v \rangle (n^2 - n_{EQ}^2) \quad (n_{EQ} = 2 (M_{DM}T/2\pi)^{3/2} \text{Exp}[-M_{DM}/T])$$

with boundary condition :  $n = 0$  at the end of inflation.

# Hypercharged Minimal Dark Matter

✓ Dark Matter has attained thermal equilibrium?



The efficiency has a peak at around  $x_{med} \approx 3 - 4$ .

[ Even if we take  $T_{MAX} \gg M_{DM}$ , DM has not necessarily attained equilibrium! ]

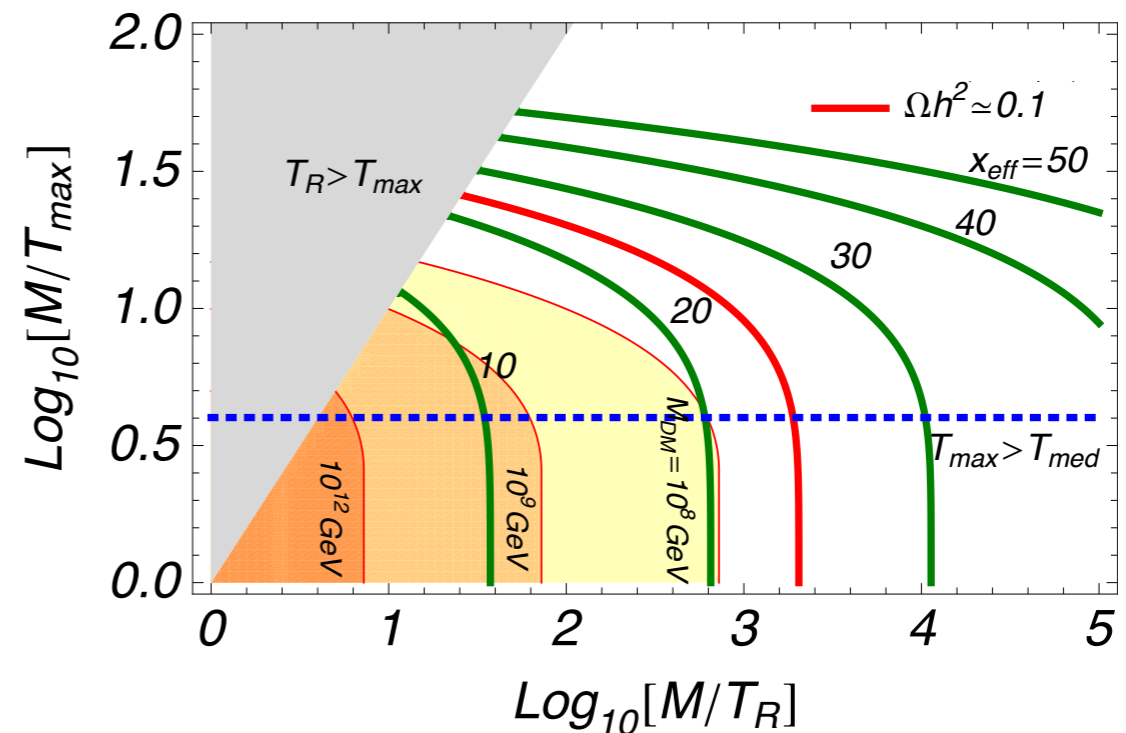
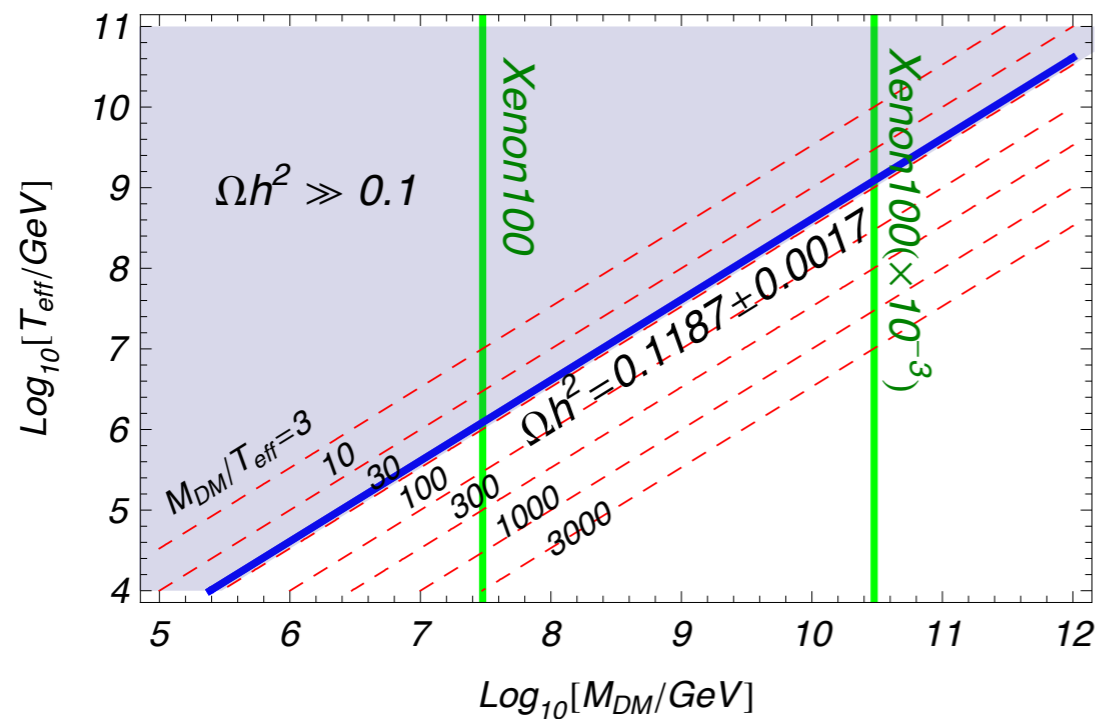
The efficiency decreases for a lower  $T_R$  for a given  $x$  ( efficiency  $\propto T_R^2$  )

The efficiency decreases for a larger  $M_{DM}$  for a given  $x$  ( efficiency  $\propto M_{DM}^{-1}$  )

In most parameter space, DM has never attained thermal equilibrium after inflation !  $\rightarrow$  Non-thermal Minimal Dark Matter !

# Hypercharged Minimal Dark Matter

✓ The relic abundance of non-thermal minimal dark matter :



$$\Omega_{DM} h^2 \simeq \frac{4}{\pi^6} \left( \frac{45}{8g_*} \right)^{3/2} \frac{s_0 \langle \sigma v \rangle M^2}{H_0^2 M_{pl}} e^{-2x_{eff}}$$

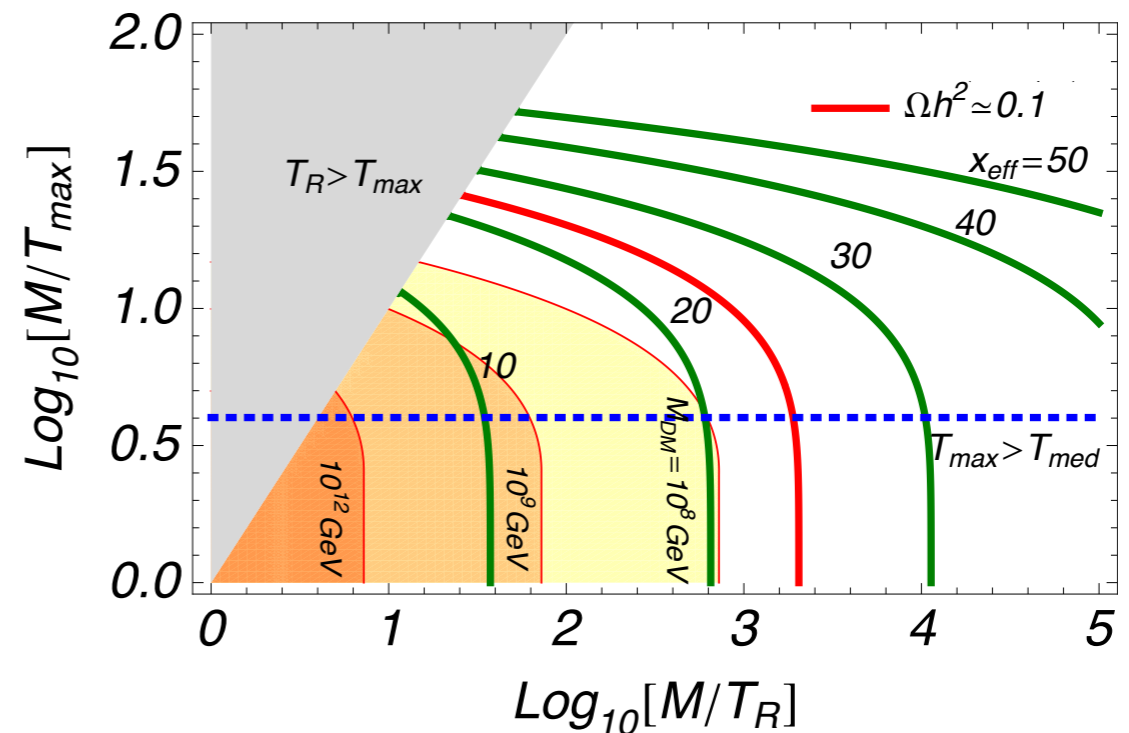
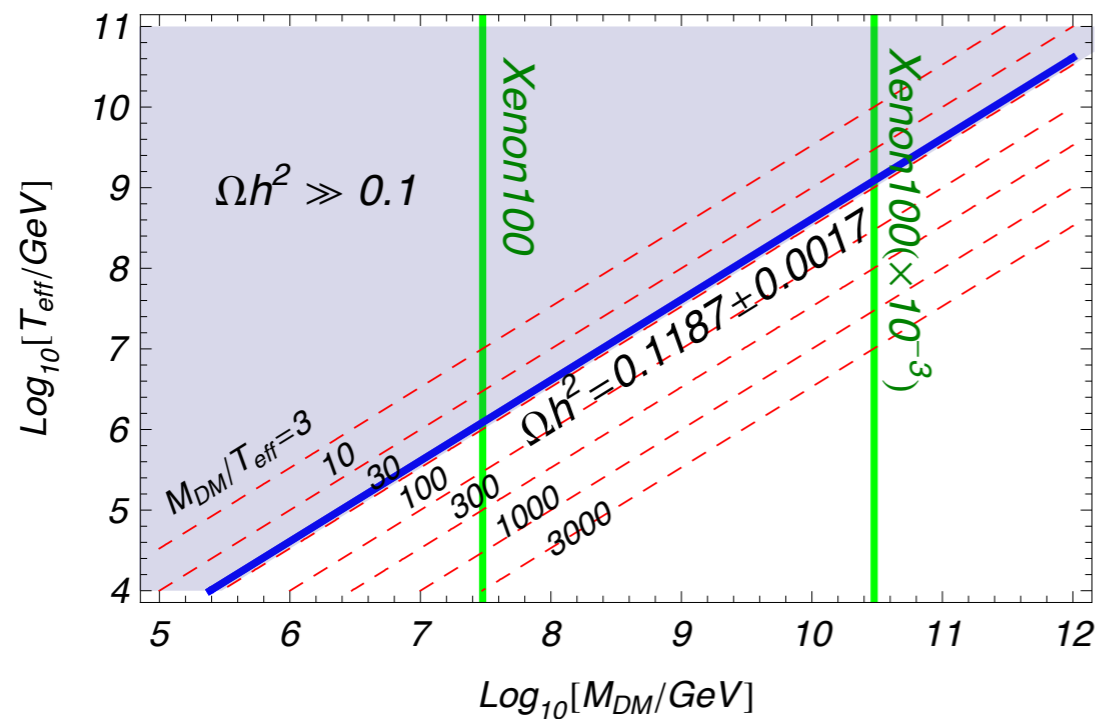
( $x_{eff} = M_{DM}/T_{eff}$ ,  $s_0$  entropy density at present,  $H_0 = 100 \text{ km/s/Mpc}$ )

- ✓ The relic abundance depends on  $M_{DM}$  only through  $x_{eff}$  ( $\langle \sigma v \rangle \propto M_{DM}^{-2}$ )
- ✓ The observed dark matter abundance is realized for  $x_{eff} \approx 26$ .



# Hypercharged Minimal Dark Matter

✓ The relic abundance of non-thermal minimal dark matter :



✓ The relation between  $T_{eff}$  and  $T_{MAX}, T_R$  :

$$x_{eff} = (x'_{med} - 1) \log x_R - \frac{1}{2} \log \left[ \epsilon^{-1} 2^{-2x'_{med}} \Gamma[2x'_{med}, 2x_{max}] \right] \quad (x'_{med} = 4.5)$$

✓  $T_{eff}$  becomes independent of  $T_{max}$  (thermalization peaks at  $T_{med}$ )

Once  $M_{DM}$  is determined by the direct detection experiments :

$$T_R \sim 10^{7-9} \text{GeV} (M_{DM}/2 \times 10^{10} \text{GeV})$$



# Hypercharged Minimal Dark Matter

- ✓ Can we test Hypercharged Minimal Dark Matter Further ?  
Can we distinguish from the Higgs portal dark matter ?
- ✓ The direct detection cross section shows the isospin violating nature due to the Z-boson exchange !

$$\sigma_{\chi N} = \frac{G_F^2 \mu_N^2}{2\pi} Y^2 (N - (1 - 4 \sin^2 \theta_W) Z)^2$$

Isospin preserving

$$\frac{\sigma_{\chi N_1}}{\sigma_{\chi N_2}} = \frac{A_1^2}{A_2^2}$$

Xe/Ge : 3.27  
Xe/Ar : 10.8

Isospin violating

$$(1 - 4 \sin^2 \theta_W) \approx 0.04$$

$$\frac{\sigma_{\chi N_1}}{\sigma_{\chi N_2}} \simeq \frac{N_1^2}{N_2^2}$$

Xe/Ge : 3.62  
Xe/Ar : 12.4

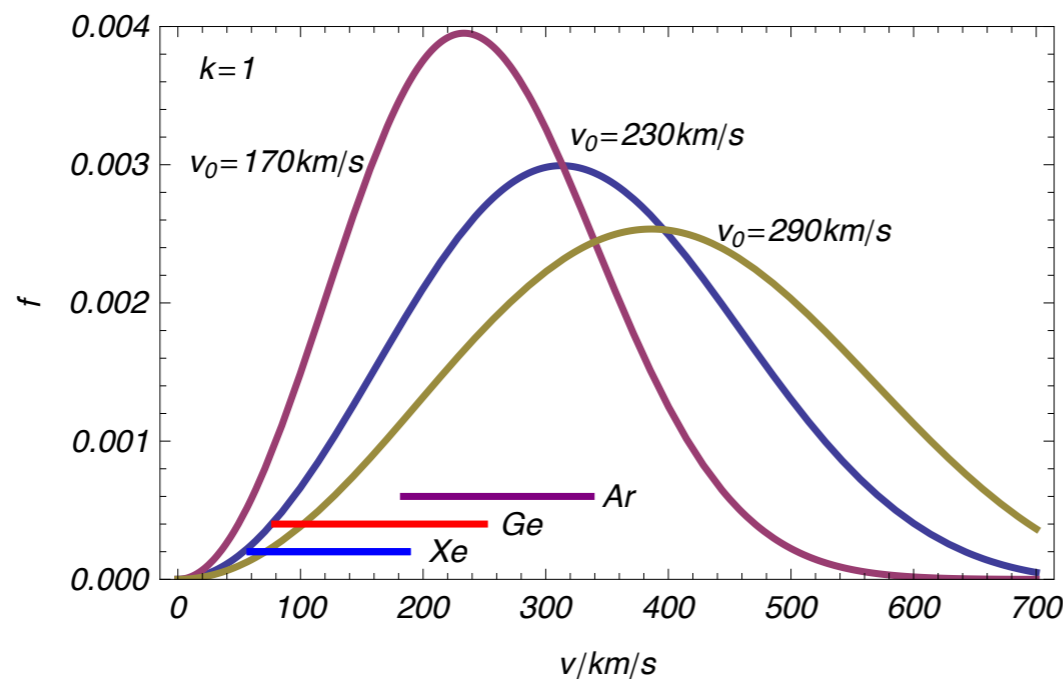
About a 10%  
difference !

By comparing signals at different target materials, we can test the isospin violation !

# Hypercharged Minimal Dark Matter

- ✓ Can we test Hypercharged Minimal Dark Matter Further ?  
Can we distinguish from the Higgs portal dark matter ?

- ✓ One caveat : We do not know the DM velocity distribution very precisely...



Minimal velocity for  $E_{recoil}$ .

$$v_{\min} = \sqrt{\frac{E_{recoil}}{2M_N}}$$

Velocities for a given  $E_{recoil}$  are different for different target...

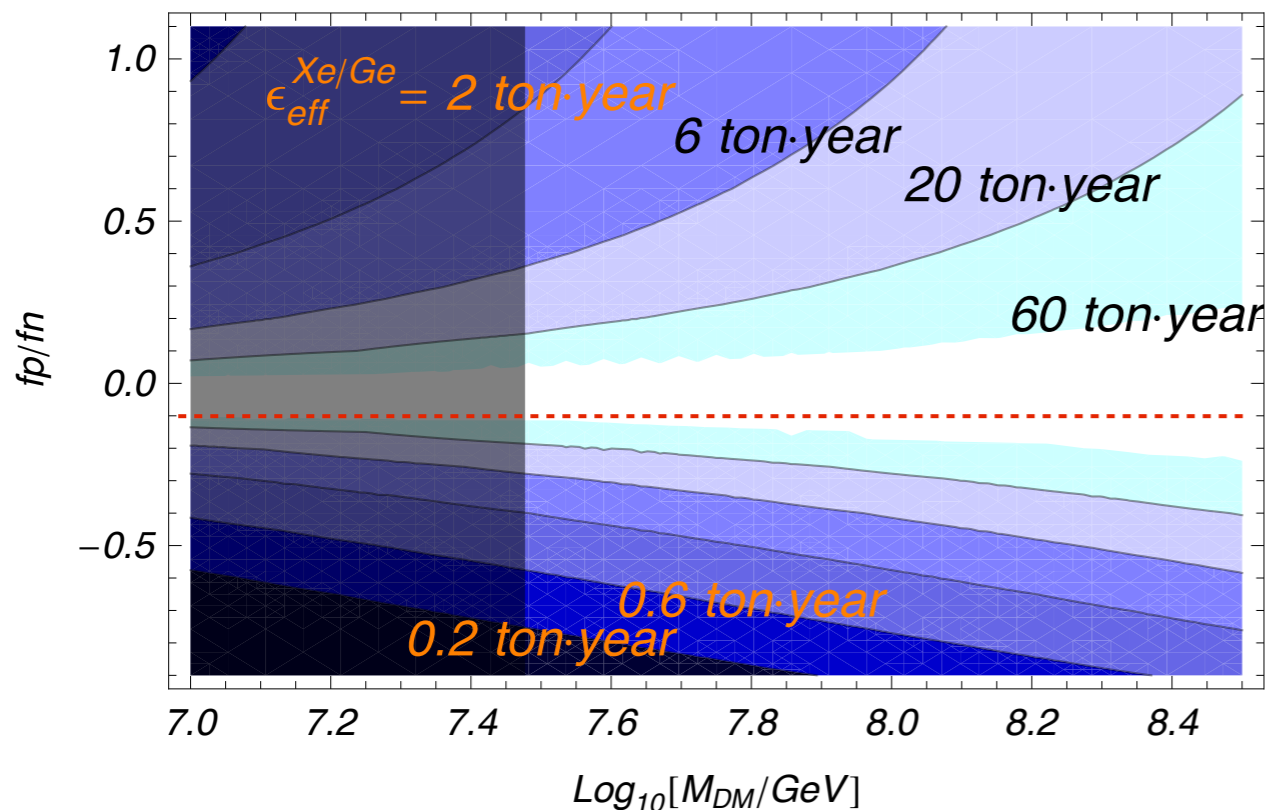
The effects of the isospin violation can be mimicked by the small change of the velocity distributions in the  $Xe/Ar$  comparison.

→ We only use  $Xe/Ge$  comparison.

# Hypercharged Minimal Dark Matter

- ✓ Can we test Hypercharged Minimal Dark Matter Further ?
- Can we distinguish from the Higgs portal dark matter ?

90% exclusion of  $f_p/f_n$



The effective exposure after background rejection to exclude  $f_p/f_n$

$$\sigma_{\chi N} = \frac{G_F^2 \mu_N^2}{2\pi} Y^2 (N^2 + f_p/f_n Z)^2$$

Irreducible background from nuclear scattering by the atmospheric neutrino becomes non-negligible for  $O(10-100)$  ton.year...

With a multi-ton effective exposure ( $\sim O(100)$  events), we can exclude the isospin preserving model, i.e.  $f_p/f_n = 1$ , for hypercharged minimal dark matter of  $M_{DM} < 10^{8-9} \text{ GeV}$ !

Multi-ton scale detectors :

- ✓ Ge : superCDMS/GEODM, EURECA...
- ✓ Xe : Xenon1T, DARWIN...

# Summary

$SU(2)_L$  charged dark matter

{	$Y = 0$ : minimal dark matter → a viable <b>WIMP</b> candidate !
	$Y \neq 0$ : hypercharged minimal dark matter → a viable <b>WIMPZILLA</b> candidate !

## ✓ Which scenario is more favorable ?

- ✓ The WIMP scenario fits together well with the *Naturalness* arguments.
- ✓ From the view point of *Simplicity* of the dark matter sector, however, **both scenarios** are equally acceptable !

## ✓ Features of hypercharged minimal dark matter.

- ✓ Next generation direct detection experiments reach to  $M_{DM} = 10^{10-11} \text{GeV}$ .
- ✓ Through the direct detection experiments we can determine the reheating temperature to  $T_R \sim 10^{7-9} \text{GeV} (M_{DM}/2 \times 10^{10} \text{GeV})$ .
- ✓ By collecting  $O(100)$  DM signal events on different target materials, we will get strong hints on the hypercharged DM through the test of the isospin violation !

# Z-boson exchange

$$\begin{aligned}\mathcal{L} = & \bar{q}i\gamma^\mu(\partial_\mu - iQ_{\text{EM}}A_\mu)q \\ & + \frac{g}{\sqrt{2}}W_\mu^+ \bar{q}_L\gamma^\mu\tau_+q_L + h.c. \\ & + \frac{g}{2\cos\theta_W}Z_\mu (\bar{q}_L\gamma^\mu\tau_3q_L - Q_{\text{EM}}\sin^2\theta_W\bar{q}\gamma^\mu q)\end{aligned}$$

$$g_V = \tau_3 - 2Q_{\text{EM}}\sin^2\theta_W \quad g_A = -\tau_3$$

q	$g_V$	$g_A$
u	$\frac{1}{2} - \frac{4}{3}\sin^2\theta_W$	$\frac{1}{2}$
d	$-\frac{1}{2} + \frac{2}{3}\sin^2\theta_W$	$-\frac{1}{2}$

$$P(uud) : g_V = (1 - 4\sin^2\theta_W)/2$$

$$n(udd) : g_V = -1/2$$

# Putting *Simplicity* on Dark Matter

✓ The neutral component is the lightest !

The Coulomb generated by  $\gamma, Z, W$  potentials pushes up each masses:

$$\delta M = \int d^3x \left[ \frac{1}{2} (\nabla\varphi)^2 + \frac{M_V}{2} \varphi^2 \right] = \frac{g^2 e^{-M_V r}}{8\pi r} (1 + M_V r) \Big|_{r=0}^{r=\infty}$$

$$\varphi = \frac{g}{4\pi r} e^{-M_V r}$$

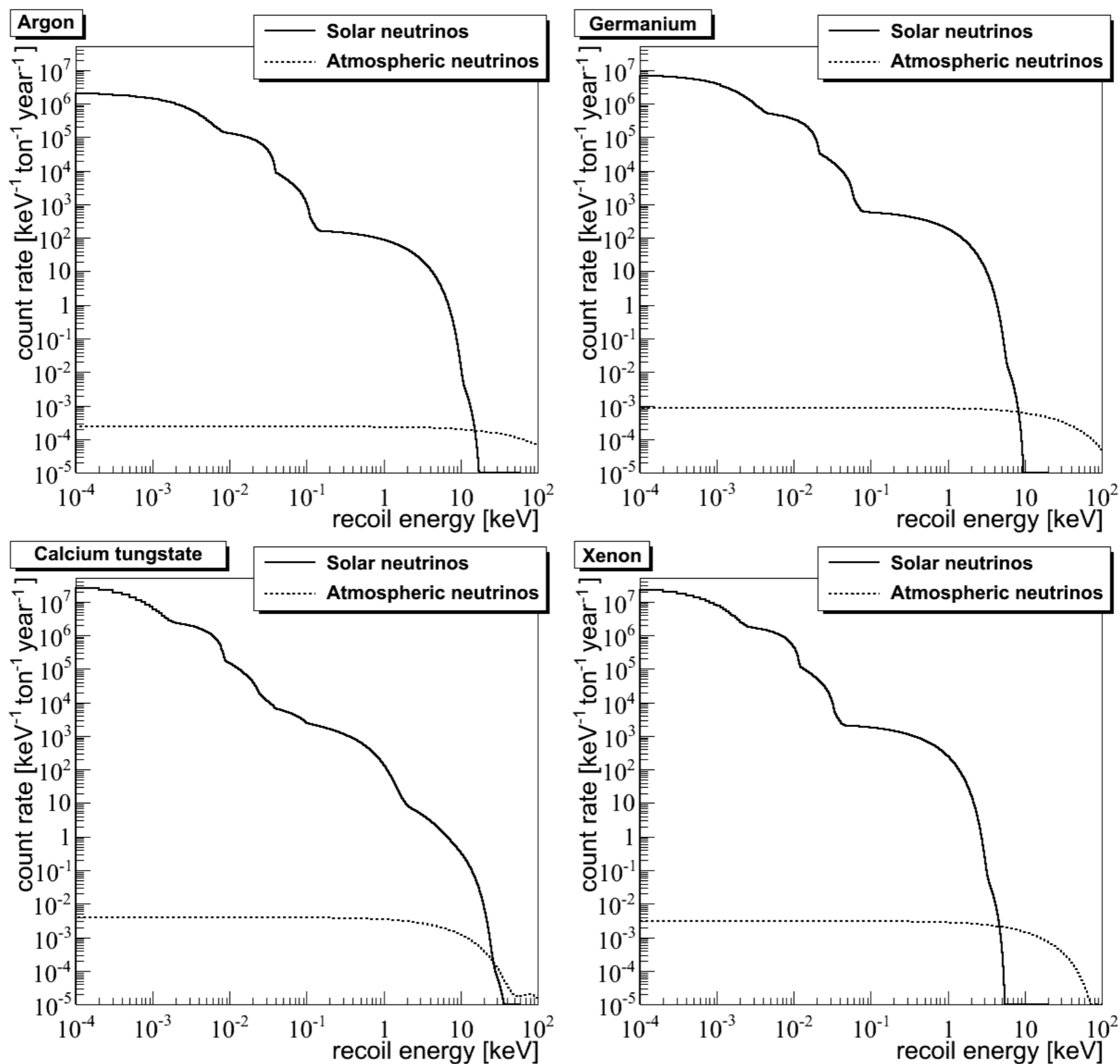
Ex) doublet  $Y=1/2$

	$\gamma$	$Z$	$W$
$\chi^0$	0	$g_2/2c_W$	$g_2$
$\chi^\pm$	1	$g_2/2c_W(1-s_W^2)$	$g_2$

Mass difference :  $M_{charged} - M_{neutral} = \alpha_2 s_W^2 M_Z / 2 = 350 \text{ MeV}$ .

# Direct Detection @ Tree-level

Recoil nuclear spectrum by neutrinos [arxiv:1003.5530]



# Constraints on the minimal triplet DM

## Triplet Dark Matter Search (indirect detections, $\chi\chi \rightarrow WW$ )

### ✓ Continuum gamma ray from dSph

Robust constraint on the DM annihilation cross section from the Fermi-LAT 2year data of **Ursa Minor dSph** ['12 Cholis and Salucci]

More stringent constraint is obtained with 6 classical and 4 ultra-faint dSphs ['11 Fermi-LAT]

J-factors of the ultra-faint dSphs are not well known.  
BG from some classical dSphs are not well understood.

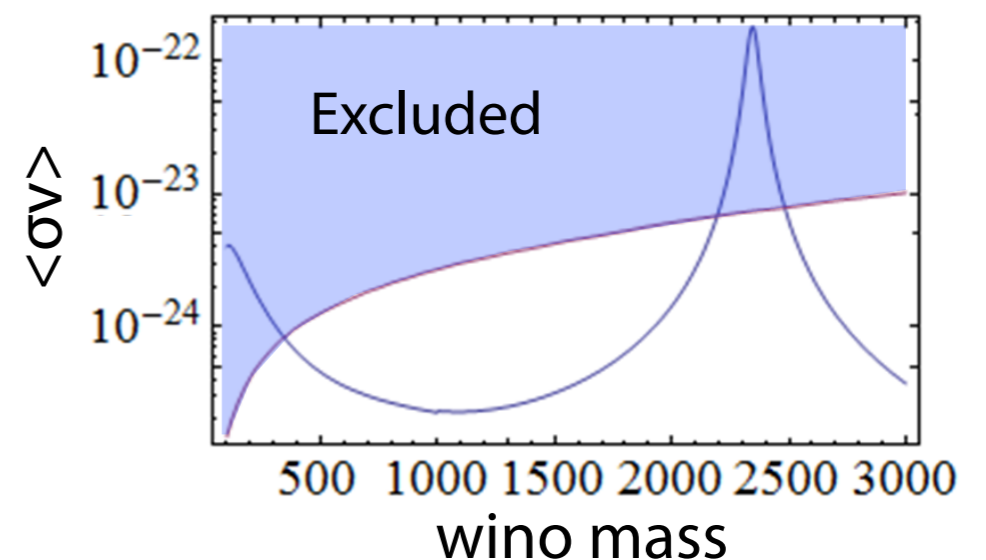
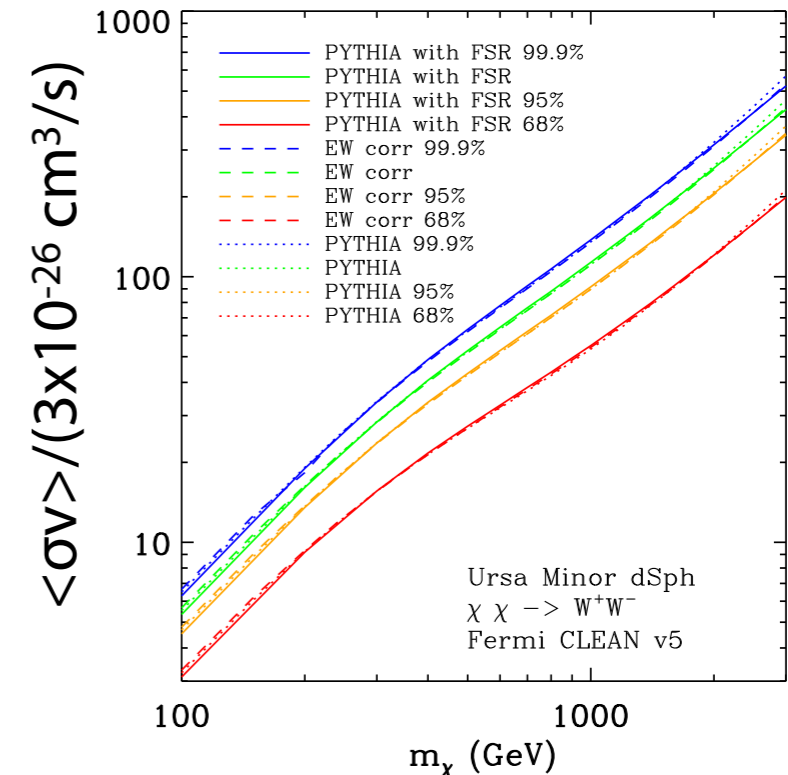
The dSph continuum gamma ray search by Fermi-LAT has excluded the wino mass in

$$m_{wino} < 340\text{GeV}$$

$$2200\text{GeV} < m_{wino} < 2500\text{GeV}$$

→ the whole range ( $m_{wino} < 3\text{TeV}$ ) will be covered if the ultra-faint dSphs are well understood!

['12 Cholis and Salucci]



[Figure by Matsumoto san]



# Constraints on the minimal triplet DM

## Triplet Dark Matter Search (indirect detections, $\chi\chi \rightarrow WW$ )

### ✓ Line gamma ray from GC

The constraints depend on the DM density profile (i.e. the J-factor) ...

A stringent constraint is obtained by assuming the NFW (cuspy) DM profile [‘13 Fan, Reece].

The Burket (cored) profile is getting favored now... [‘13 Nesti, Salucci]

The line gamma ray search from GC by H.E.S.S. has excluded the wino mass in

$$2200\text{GeV} < m_{\text{wino}} < 2500\text{GeV}$$

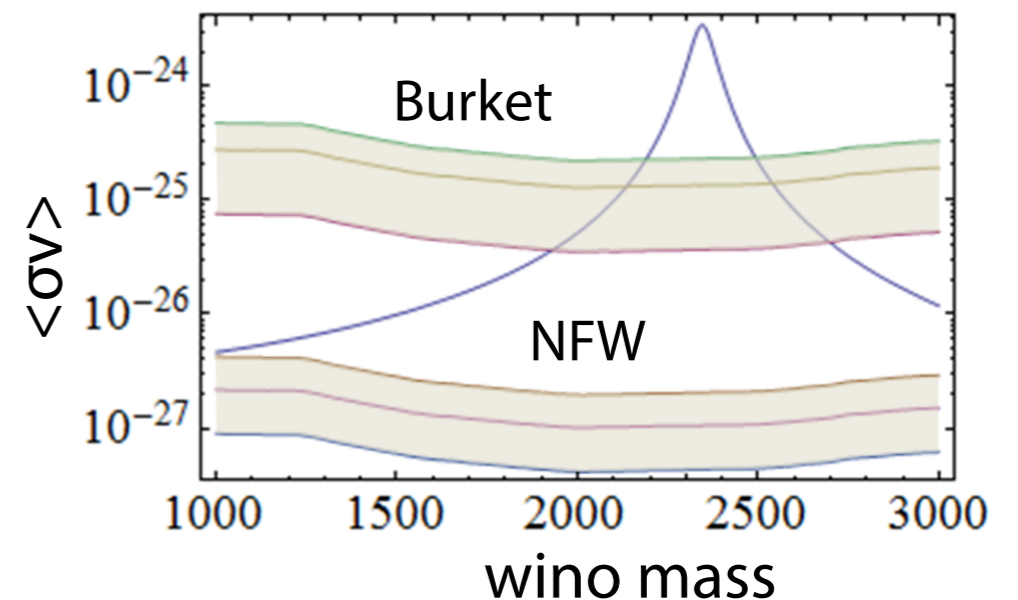
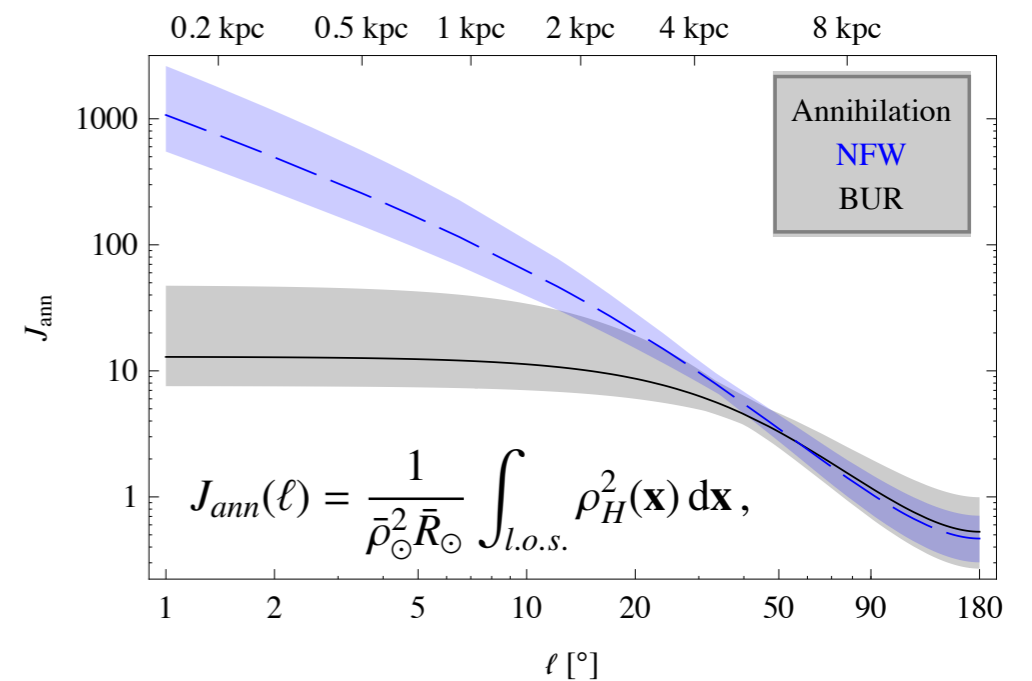
assuming the Burket profile.

→ CTA has a lot of chance to find the wino DM!

The constraint on the wino mass from the continuum gamma ray from GC has been obtained by assuming NFW [‘12 Hooper et.al.].

BG from the GC is not well understood.

[‘13 Nesti, Salucci]



# Hypercharged Minimal Dark Matter

$SU(2)_L$  charged dark matter

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	$Y \neq 0$ : hypercharged minimal dark matter → a viable <b>WIMPZILLA</b> candidate ?

## ✓ Which scenario is more favorable ?

- ✓ The WIMP scenario fits together well with the *Naturalness* arguments (cf. the neutralino in Supersymmetry)
- ✓ From the view point of *Simplicity* of the dark matter sector, however, **both scenarios** are equally acceptable !

How hypercharged dark matter works as *WIMPZILLA* ?

What can we learn if dark matter is hypercharged?