

## GLOBALIZATION OF LOCAL MIRROR FUNCTORS

ABSTRACT. Motivated by SYZ mirror symmetry, we study a homological algebra of gluing of Yoneda functors of  $A_\infty$ -category. We combine a technique of weakly unobstructed deformation of a single  $A_\infty$ -algebra and a general homotopy theory of  $A_\infty$ -categories and find a condition for gluing several Yoneda functors in a suitable sense. We also prove some descent property for matrix factorization categories. As an application, we globalize a local mirror construction for pair-of-pants to a pair-of-pants decomposition of generic hypersurface.