

Introduction to Fracture and Fatigue Behavior of Materials

Introduction to Risk-based Inspection - Advanced Mechanical Systems Maintenance Engineering

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Outline

Materials microstructures and defects

- Materials length scales

- Processes, microstructures and defects

Fracture mechanics

- The mechanics of fracture ahead of a crack

- The mechanisms of fracture

Cyclic loading behavior: fatigue

- Cyclic loading

- Fatigue crack initiation and propagation

Summary

Further details

- Energetic approach to fracture

- Playing with the endurance limit

- Typical materials behaviors and properties

Controlled fracture



Source : <https://youtu.be/ekv0kprA3AY>

- ▶ Can opening,
- ▶ Food packaging,
- ▶ Aircraft engines: shear-bolts as safeguards,
- ▶ ...

Motivations and objectives

Objectives

- ▶ Understand the link between materials **processes**, **microstructures** and **defects**.
- ▶ Understand the fundamentals of **fracture** in the presence of defects.
- ▶ Fundamentals of **fatigue** behavior.

Suggested reading

- ▶ Ashby, Shercliff, Cebon. *Materials: engineering, science, processing and design*, Ed. Butterworth-Heinemann, 2007
- ▶ Ashby, Jones. *Engineering materials 1: an introduction to properties, applications, and design*, Ed. Butterworth-Heinemann, 2012
- ▶ Ashby, Jones. *Engineering materials 2: an introduction to microstructures and processing*, Ed. Butterworth-Heinemann, 2013

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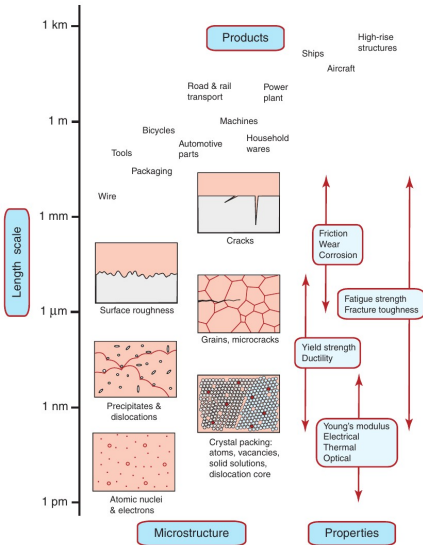
Further details

Energetic approach to fracture

Playing with the endurance limit

Typical materials behaviors and properties

Length scales in metallic materials



- ▶ **Atoms**, crystal packing: Young's modulus E .
- ▶ **Dislocations** and microstructure **obstacles**: strength, toughness.
- ▶ **Grains**, surface roughness and **cracks**: fatigue behavior, friction, wear.

Microstructures, defects

Materials length scales
Processes, microstructures

Fracture

Crack influence
Mechanisms

Fatigue

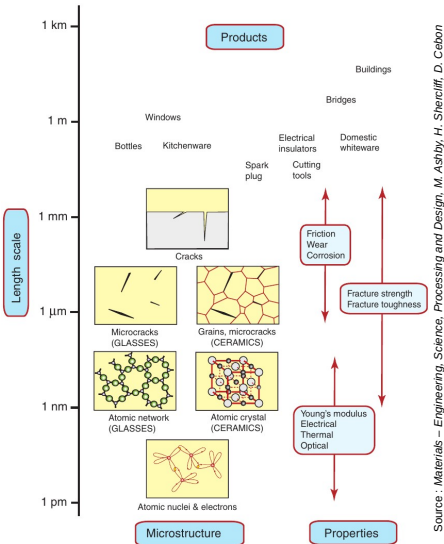
Cyclic loading
Fatigue crack

Summary

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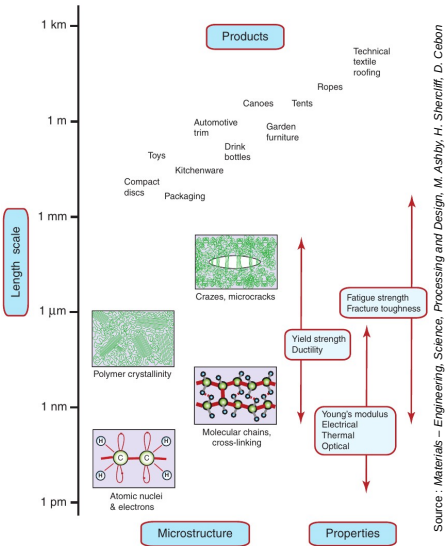
Energetic approach to fracture
Optimizing endurance
Typical behaviors

Length scales in ceramics and glasses



- ▶ Ceramics: mostly crystalline.
- ▶ Glasses: amorphous.
- ▶ Stiff **atomic bonds** and high **lattice friction**: high Young's modulus and hardness.
- ▶ Failure dominated by **cracks** and surface finish.

Length scales in polymers and elastomers



- ▶ Microstructure: (macro-) **molecular** rather than atomic
- ▶ Diverse arrangements: amorphous, crystalline, cross-linked, ...
- ▶ Foams, composites: additional length scale → **architecture**.

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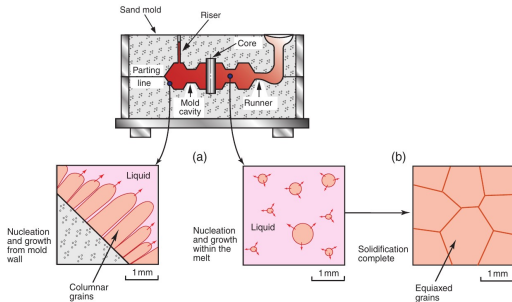
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Energetic approach to fracture

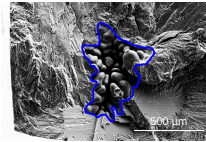
Playing with the endurance limit

Typical materials behaviors and properties

Metal casting and solidification



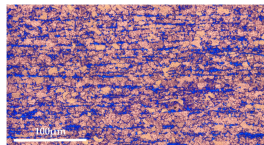
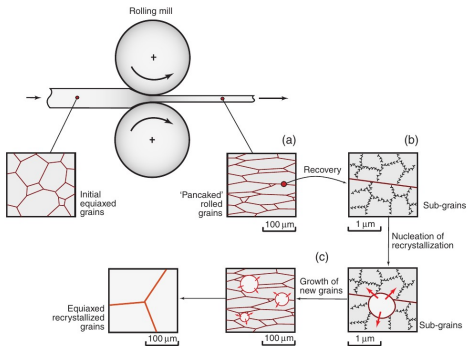
Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon



Sub surface micro-shrinkage in a A357 cast aluminum alloy. Source : *Serrano Munoz 2014, PhD thesis*

- ▶ Low production cost, complex shapes, massive use in car industry.
- ▶ Control of **grain size**: (i) inoculant (stimulate nucleation) and (ii) cooling rate.
- ▶ Casting **defects**: shrinkages, gas pores, oxides and impurities due to segregation. \implies limited **fatigue** properties.

Deformation processing of metals and alloys



Microstructure of a DP600 steel.
Source: Huin 2017, PhD thesis.

Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ Deformation processing (e.g. rolling) strongly affects **microstructure**: grain size/shape, distribution of 2nd phase particles or impurities, dislocation density
- ▶ Microstructural **transformations** often occur: recovery/recrystallization, phase transformations, ...

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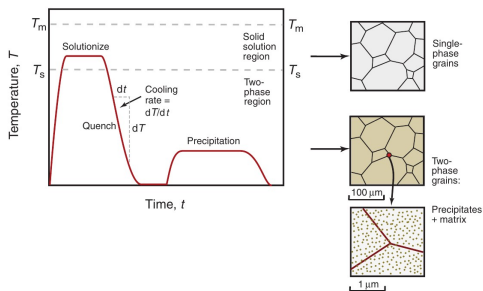
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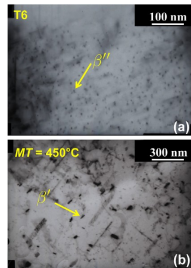
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Heat treatment of metallic alloys



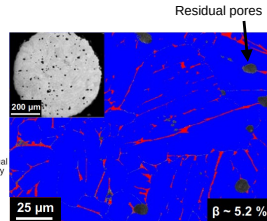
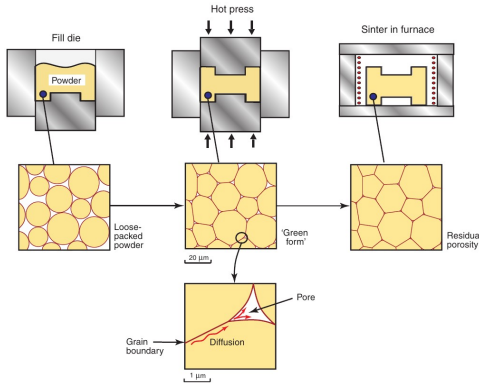
Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon



Nanosize precipitates in an 6061 aluminum alloy. Bardel et al. *Acta Mat.* 2015

- ▶ Metal alloys: usually **heat treated** for optimized strength.
- ▶ **Precipitates** and 2nd phase particles: some useful for **hardening**, others detrimental for **toughness** (e.g. crack initiation sites).

Powder processing

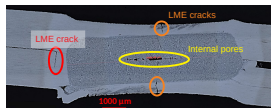
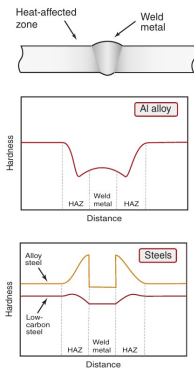
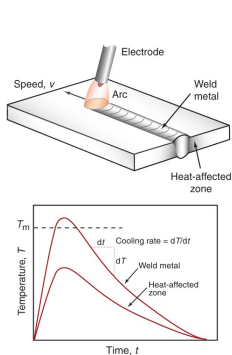


Sintered sample, Ti alloy. *Coffigniez 2021, PhD thesis.*

Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ Common process for high performance ceramics and many metals, complex shapes achievable.
- ▶ **Residual porosity** remains even after optimized compaction and sintering. Defect **size** critical!

Welding

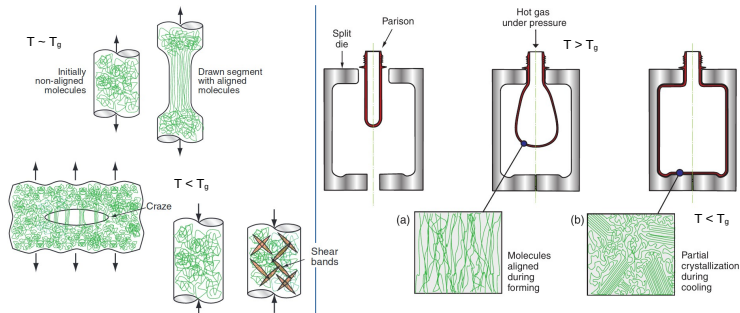


Different defects in a steel resistance spot weld. Siar et al., Mat. Char. 2022

Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ Welding severely alters the **local** microstructure in the joint.
- ▶ Welding **defects** (shrinkage pores, cracks, gaz bubbles, ...) often present. Harmful to be checked.

Thermoplastic polymer molding



Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ **Glass transition temperature T_g** : strong impact on deformation mechanism and arrangement of macromolecules.
- ▶ Different types of defects depending on **process/service temperature wrt T_g** : crazes, micro cracks, shear bands etc...

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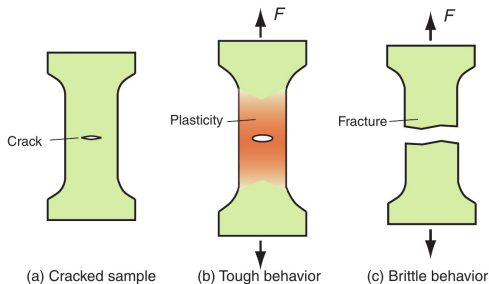
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Strength vs Fracture toughness

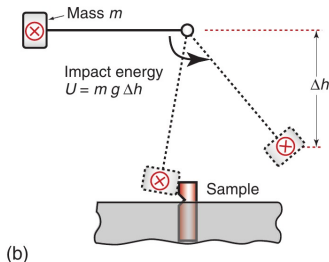
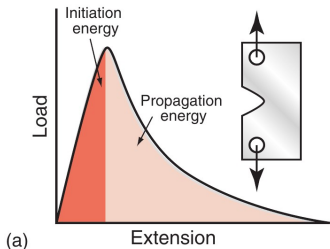


Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ Strength \neq Toughness.
- ▶ **Strength**: resistance to plastic flow (yield stress σ_Y).
- ▶ **Toughness**: resistance to crack propagation (fracture toughness K_{Ic}).
- ▶ Facing a crack/defect, 2 extreme behaviors:
 - ▶ **Ductile** behavior (low σ_Y , high K_{Ic}),
 - ▶ **Brittle** behavior (high σ_Y , low K_{Ic}).

Macroscopic tests

Quickly assessing the type of fracture behavior



Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ Ex: tear test (a), impact test (b).
- ▶ Quick assessment of either ductile or brittle behavior
⇒ quality control, ranking.
- ▶ Not a **true** material property measurement (sample dependent).

Ductile to Brittle transition

Transition from ductile to brittle behavior at low temperature

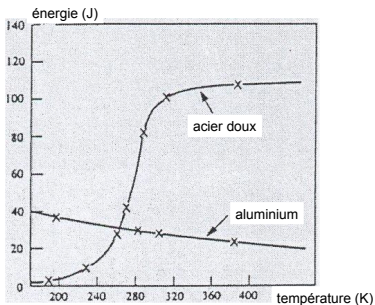
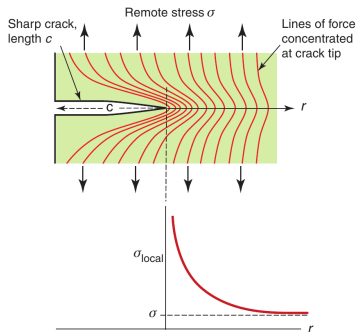


Figure: Charpy impact test, V notch

- ▶ HC and BCC material behavior changes at low T (not FCC materials).
- ▶ Ductile to Brittle **transition temperature**.
- ▶ **⚠** Test conditions greatly influence the results.

Singularity of the stress field at the crack tip



Source : *Materials – Engineering, Science, Processing and Design*,
M. Ashby, H. Shercliff, D. Cebon

- ▶ $\sigma_{local} = \sigma \left(1 + Y \sqrt{\frac{\pi C}{2\pi r}} \right)$ with $Y \sim 1$. (geometry)
- ▶ $\sigma_{local} \approx \sigma Y \sqrt{\frac{\pi C}{2\pi r}}$ close to the crack tip.
- ▶ $K_I = Y\sigma\sqrt{\pi c}$: **stress intensity factor** (mode I: opening direction perpendicular to the crack plane).
- ▶ $\forall r, \sigma_{local} \propto K_I$

Stress Intensity Factor tables

K_I is known for many standard situations

	<p>Continued through crack $K_I = \sigma\sqrt{\pi c}$ ($c \ll w$)</p>
	<p>Single edge notch $K_I = 1.1\sigma\sqrt{\pi c}$ ($c \ll w$)</p>
	<p>Through crack with pressure p $K_I = p\sqrt{\pi c}$ ($c \ll w$)</p>
	<p>Cracked beam with central load F; $b =$ thickness $K_I = 3 \frac{FL}{bw^2} \sqrt{\pi c}$ ($c \ll w$)</p>
	<p>Contained, penny-shaped crack $K_I = 0.7\sigma\sqrt{\pi c}$ ($c \ll w$)</p>

Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

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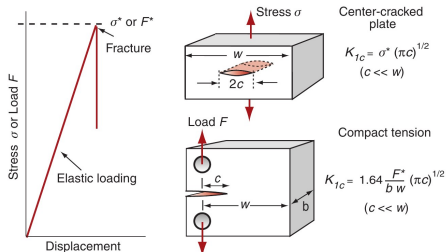
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Measuring fracture toughness

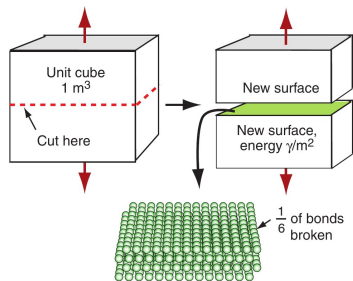
Linear elastic fracture mechanics



Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ Standardized samples, tracking crack propagation.
- ▶ Infinitely sharp initial crack.
- ▶ K_I evolution is known (unit: $\text{MPa}\sqrt{\text{m}}$).
- ▶ K_{Ic} (plain-strain **fracture toughness**): critical value of K_I for F^* , c^* (material property: sample **independent**)

Energetic approach

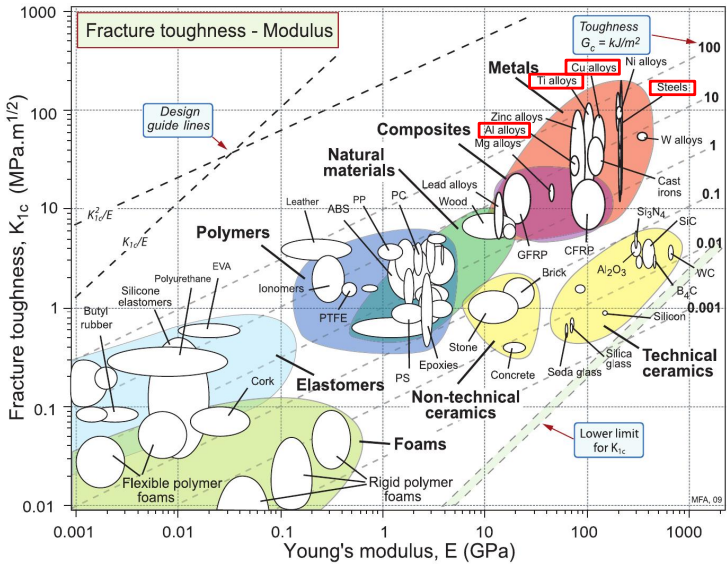


Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ Crack: **2 new surfaces**, energy γ (J/m²).
 $\gamma \sim 1 \text{ J/m}^2$ typically
- ▶ **Necessary condition** for a crack surface extension dA :
 - ▶ $GdA \geq 2\gamma dA$
 - ▶ G : energy release rate (J/m²).

- ▶ Real life: $G_c \gg 2\gamma$ (local plasticity).
- ▶ G_{Ic} (J/m²): mode I **toughness**, or critical energy release rate.
- ▶ K_{Ic} proportional to G_{Ic} :
 $K_{Ic} = \sqrt{EG_{Ic}}$ (cf. demo, Appendix)

Fracture toughness – Young's modulus chart

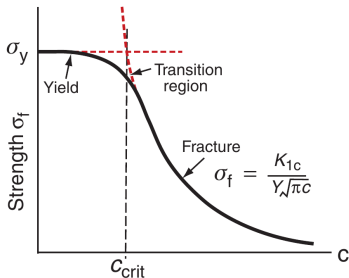


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Source : www.grantadesign.com/education/resources

Critical crack size

Transition from yield to fracture



Source : Materials – Engineering, Science, Processing and Design, M. Ashby, H. Shercliff, D. Cebon

- ▶ $K_{Ic} = Y\sigma_f\sqrt{\pi c}$
- ▶ σ_f : **failure** stress for a given c value.

$$\sigma_f = K_{Ic} / (Y\sqrt{\pi c})$$
- ▶ If $\sigma_f > \sigma_y$:
 global **yielding** before failure.

- ▶ c_{crit} defined by $\sigma_f = \sigma_y$:

$$c_{crit} = K_{Ic}^2 / (Y^2 \pi \sigma_y^2) \quad \text{with } Y \sim 1$$

- ▶ **Damage tolerance:**

- ▶ **Metals** (high K_{Ic}): still yield in a predictable, ductile, manner even with **large cracks**.
- ▶ **Ceramics** (low K_{Ic}): fail in a brittle manner at stresses far below σ_y because of **small cracks**.

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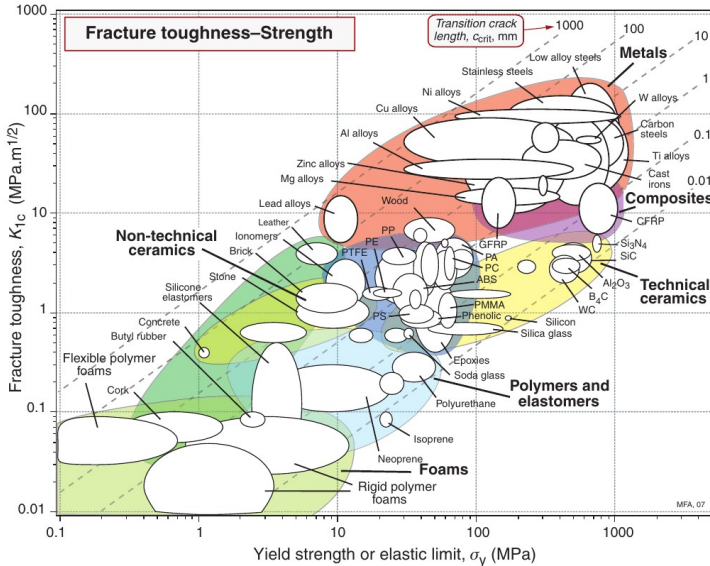
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Fracture toughness – strength chart



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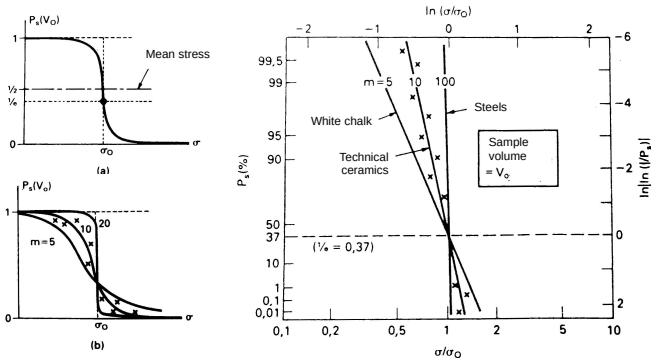
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Statistical variation in strength: Weibull

Brittle materials: dispersion of strength rather than a unique value



Source : Engineering materials 2: an introduction to microstructures and processing, M. Ashby, D. Jones

- ▶ **Survival** probability P_s , n samples of volume V_0 :
$$P_s(V_0) = \exp[-(\sigma/\sigma_0)^m] \quad \sigma_0, m \text{ constants.}$$
- ▶ σ_0 : stress for 37% of survival,
- ▶ m : **Weibull modulus** (m small \Rightarrow high deviation).

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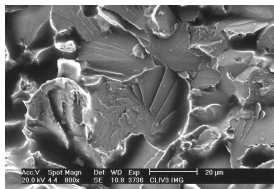
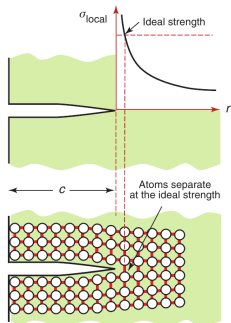
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The origins of toughness

Brittle 'cleavage' fracture



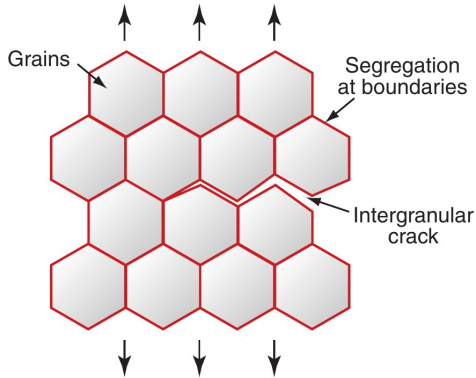
Cleavage of atomic planes

Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ Hard and brittle materials: no way to release the crack tip stresses by plastic flow.
- ▶ σ_{local} about $E/15$ (ideal strength).
- ▶ **atomic bonds** fracture (**cleavage**): crack propagation and acceleration.
- ▶ NB: FCC materials not affected (many slip systems).

The origins of toughness

Brittle intergranular fracture

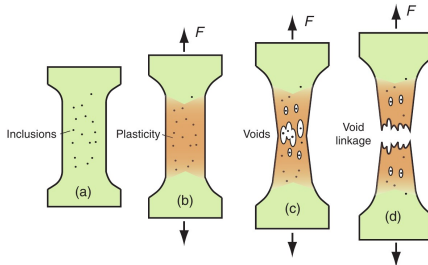


Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ Grain boundary **segregation** (impurities in the alloy, ex: during solidification): network of **low-toughness paths** through the material.
- ▶ Possible **intergranular** cracking.

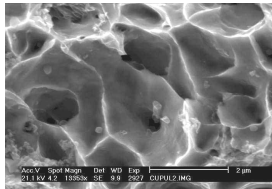
The origins of toughness

Ductile fracture



Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

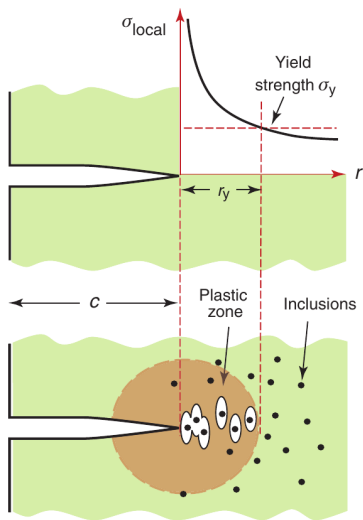
Deformed dimples and the inclusions leading to decohesion



- ▶ **Inclusions** act as stress concentration sites.
- ▶ **Nucleation, growth and coalescence** of cavities.

The origins of toughness

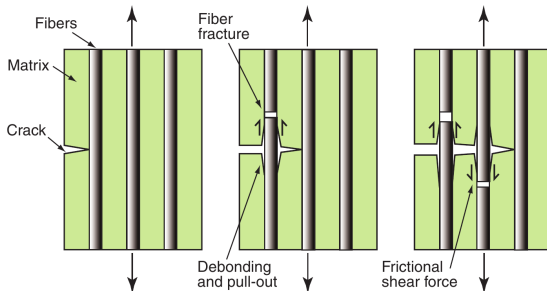
Cracks in ductile materials



- ▶ Voids nucleate, grow and coalesce at the crack tip.
- ▶ Crack tip is **blunted** ($\implies \sigma_{local}$ decreases).
- ▶ Plastic work at the crack tip **dissipates** (a lot of) **energy**:
the work of fracture G_{Ic} is high, so is K_{Ic} .
- ▶ ($K_{Ic} = \sqrt{EG_{Ic}}$, see Further details)

Manipulating toughness

Composite/architected materials: additional energy dissipation mechanisms can improve toughness



Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ Polymer matrix: $K_{Ic} = 3 \text{ MPa}\sqrt{\text{m}}$
- ▶ Glass fiber: $K_{Ic} = 0.8 \text{ MPa}\sqrt{\text{m}}$
- ▶ Composite (matrix+fibers): up to $K_{Ic} = 10 \text{ MPa}\sqrt{\text{m}}$
- ▶ Multiple cracking, fiber debonding/pullout, friction: crack propagation **delayed**, energy **dissipated**.

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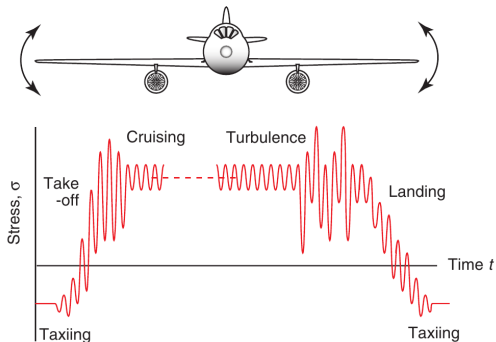
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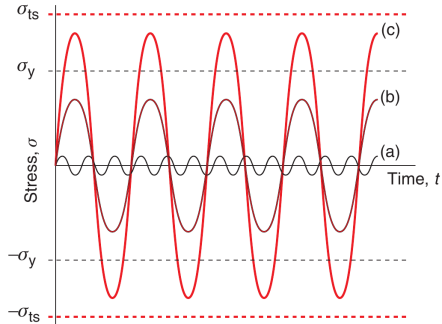
Cyclic loading



Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ **Cyclic loadings** are legion: waves on off-shore platforms, gas tank under cyclic pressure, axles of coaches, etc...
- ▶ Materials grow tired if repeatedly stressed, leading to failure.
- ▶ **Failure can happen** even if $\sigma < \sigma_y$.

Different types of fatigue

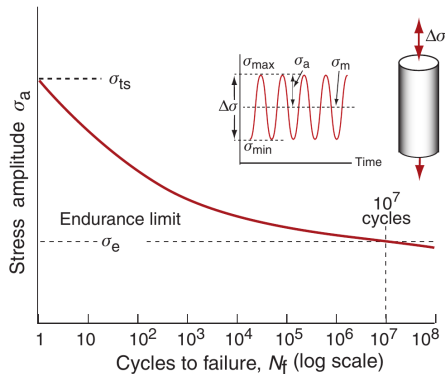


Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ (a): acoustic vibration ($\sigma \ll \sigma_y$),
- ▶ (b): high-cycle fatigue ($\sigma < \sigma_y$),
- ▶ (c): low cycle fatigue ($\sigma_y < \sigma < \sigma_R$).

Wöhler curve - the endurance limit

S-N or Wöhler curve: number of cycles to fracture as a function of stress

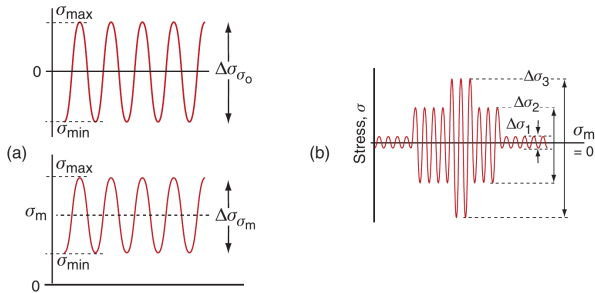


Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ $\sigma_a = \frac{\sigma_{max} - \sigma_{min}}{2}$, $\sigma_m = \frac{\sigma_{max} + \sigma_{min}}{2}$, $R = \frac{\sigma_{min}}{\sigma_{max}}$.
- ▶ Lifetime $N_f = f(\sigma_a)$ (cycles to failure).
- ▶ **Endurance limit** σ_e for 10^7 cycles, with $\sigma_m = 0$.

Real-life fatigue

When the applied stress is not constant



Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ If $\sigma_m \neq 0$, **Goodman's** law: look for $\Delta\sigma_{\sigma_0}$ such that
$$\Delta\sigma_{\sigma_m} = \Delta\sigma_{\sigma_0} \left(1 - \frac{\sigma_m}{\sigma_R}\right)$$
($\sigma_a = \frac{\Delta\sigma_{\sigma_0}}{2}$ on Wöhler curve)
- ▶ If σ_a changes, **Miner's** cumulative damage rule:
$$\sum_{i=1}^n \frac{N_i}{N_{f,i}} = 1 \quad (\text{failure: sum} = 1)$$

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Fracture mechanics

The mechanics of fracture ahead of a crack

The mechanisms of fracture

Cyclic loading behavior: fatigue

Cyclic loading

Fatigue crack initiation and propagation

Summary

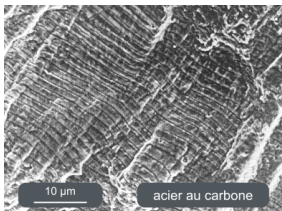
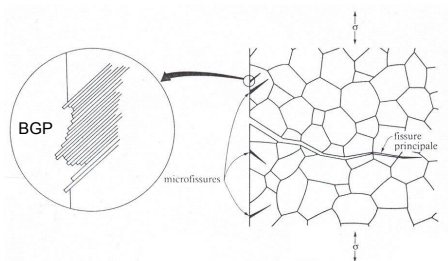
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Crack growth during cyclic loading



Source : <http://nte.mines-albi.fr/SciMat/co/SM6uc3-3.html>

- ▶ 3 main stages for fatigue failure:
 - ▶ Stage I: crack **initiation**,
 - ▶ Stage II: crack **growth**,
 - ▶ Stage III: fast **fracture**.
- ▶ Stage I in crystalline ductile materials: microcracks initiation in **Persistent Gliding Bands**.
- ▶ Stage II: main crack grows along a plane almost perpendicular to the applied stresses.
- ▶ Fracture surface: micro-roughness \implies **fatigue striations**.

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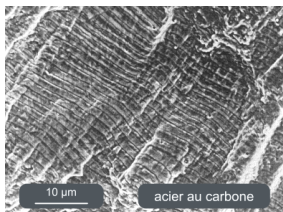
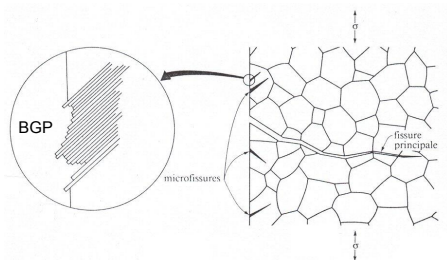
Cyclic loading
Fatigue crack

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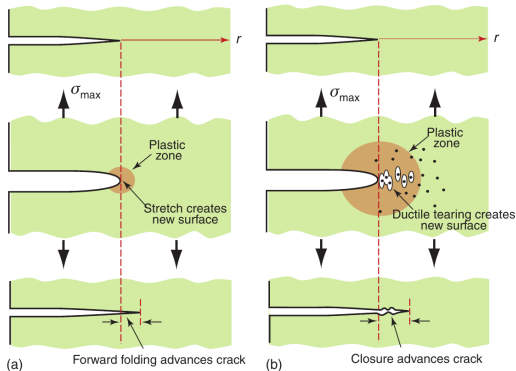
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Fatigue crack propagation mechanism

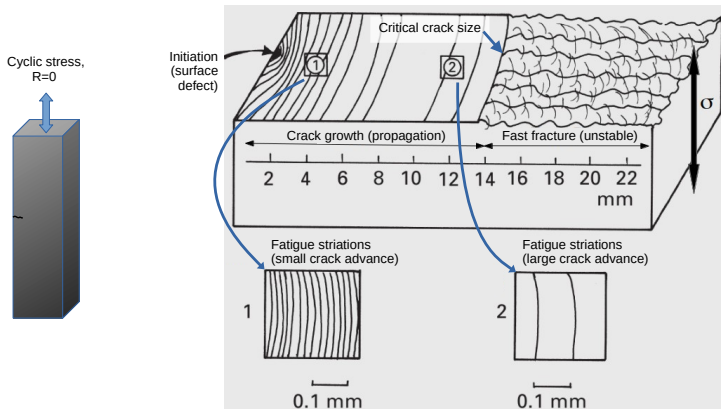


Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ High-cycle fatigue (a): small plastic zone and crack advance.
- ▶ Low-cycle fatigue (b): large plastic zone and crack advance

Fracture surface

Sketch of a typical fracture surface, tensile cyclic loading



- Details of fracture surface:
⇒ A lot can be learned on the material and fatigue crack propagation mechanism.

Summary

Fracture

- ▶ All materials: microstructure and/or process **defects**.
- ▶ **Ductile** behavior v.s. **Brittle** behavior .
- ▶ Transition with temperature for many metals.
- ▶ Macroscopic tests (ex. impact test) do NOT measure true (sample independent) properties.
- ▶ $K_I - K_{Ic}$ (or $G_I - G_{Ic}$) to describe sudden fracture.

Fatigue

- ▶ Fatigue: **cyclic** loading propagates small cracks in materials.
- ▶ **Paris** law to describe **propagation**.
- ▶ **Wöhler** curve to assess **lifetime** under given stress amplitude.

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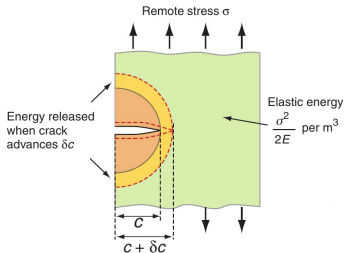
Energetic approach to fracture

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$$K_{Ic} = f(G_{Ic})$$

simplified demonstration



Source : Materials – Engineering, Science, Processing and Design, M. Ashby, H. Shercliff, D. Cebon

- ▶ sample, thickness b .
- ▶ stored elastic energy (J/m³) :
- ▶ Crack, length c .
Approximately:

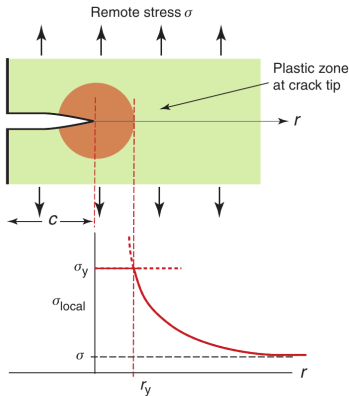
- ▶ σ relaxed in a $\frac{1}{2}$ cylinder, radius c .

- ▶ released energy:

$$U(c) \approx \frac{\sigma^2}{2E} \times \frac{\pi}{2} c^2 b$$

- ▶ $\partial U(c)/\partial c = \frac{\sigma^2 \pi b}{2E} \times c$
- ▶ $\delta U = \frac{\sigma^2 \pi c}{2E} \times b \delta c$ with $K_I^2 = \sigma^2 \pi c$ ($Y \sim 1$)
- ▶ Failure condition: $\delta U = G_{Ic} \times b \delta c$
- ▶ $G_{Ic} = K_{Ic}^2 / (2E)$ ou $K_{Ic} = \sqrt{2EG_{Ic}}$
- ▶ More accurate analysis $\implies K_{Ic} = \sqrt{EG_{Ic}}$

Plastic zone at the crack tip



Source : Materials – Engineering, Science, Processing and Design, M. Ashby, H. Shercliff, D. Cebon

- ▶ Crack tip: σ_{local} very high. Consequences :
 - ▶ plasticity in ductile materials,
 - ▶ micro-cracks in ceramics,
 - ▶ decohesion in composites.
- ▶ $G_c \gg 2\gamma$
(necessary work of fracture higher than the sole surface creation).

- ▶ plastified area r_y such as $\sigma_{local}(r) = \sigma \sqrt{\frac{\pi c}{2\pi r}} \geq \sigma_y$.
- ▶ σ redistribution: factor 2 on resulting r_y .
- ▶ $r_y = 2 \times \frac{\sigma^2 \pi c}{2\pi \sigma_y^2} = \frac{K_I^2}{\pi \sigma_y^2}$

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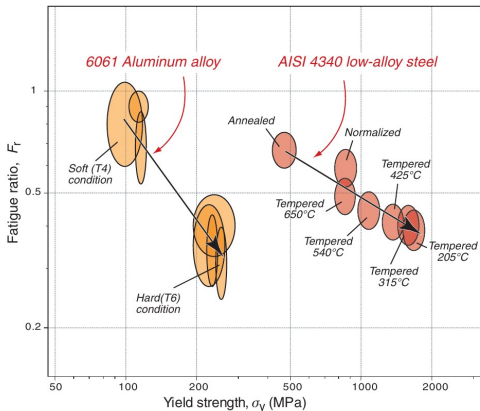
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Effect of hardening heat treatments



Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Cebon

- ▶ Fatigue ratio $F_r = \sigma_e / \sigma_y$.
- ▶ F_r decreases with hardening heat treatment, but σ_y strongly increases !

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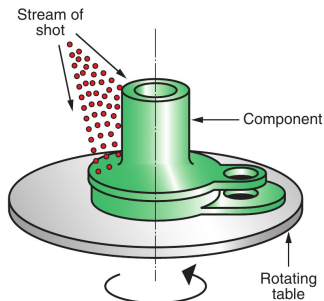
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Enhancing resistance to fatigue

Playing with defects and surface



Source : *Materials – Engineering, Science, Processing and Design*,
M. Ashby, H. Shercliff, D. Cebon

- ▶ Minimize **defects**, pre-cracks, porosity etc...
- ▶ Introduce **compressive stresses** at the surface:
 - ▶ cracks often start at the surface
⇒ compressive stresses tend to close the cracks.
 - ▶ **Shot peening**, sanding, but also carburizing, nitriding, etc...

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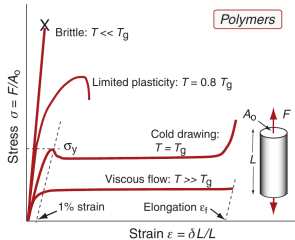
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Typical materials behaviors and properties

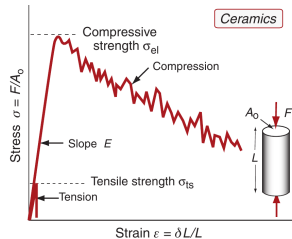
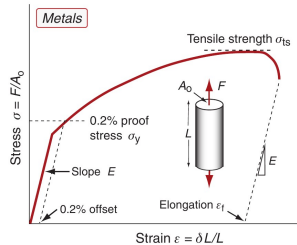
Typical behaviors

Uniaxial tension/compression

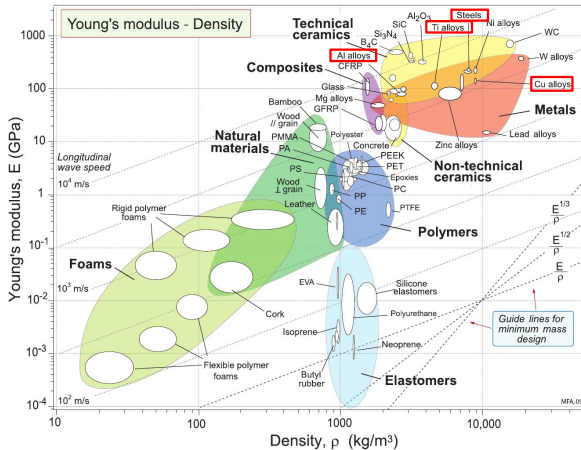
- ▶ **Stiffness** : E (elasticity)
- ▶ **Strength** :
 $\sigma_y, \sigma_{0.2\%}, \sigma_{ts}$
- ▶ **Ductility** : ε_f



Source : *Materials – Engineering, Science, Processing and Design*, M. Ashby, H. Shercliff, D. Ceban



Stiffness



Source : www.grantadesign.com/education/resources

- ▶ Pure materials: atomic bounds and crystallography.
- ▶ Hybrids, composites, etc... : structure / architecture also.

Fatigue and Fracture

S. Dancette

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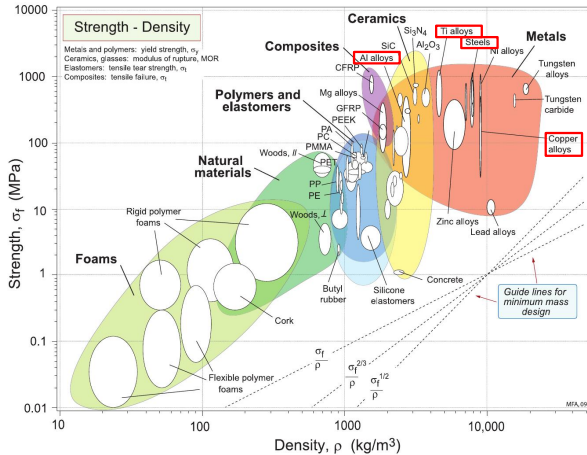
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Strength



Source : www.grantadesign.com/education/resources

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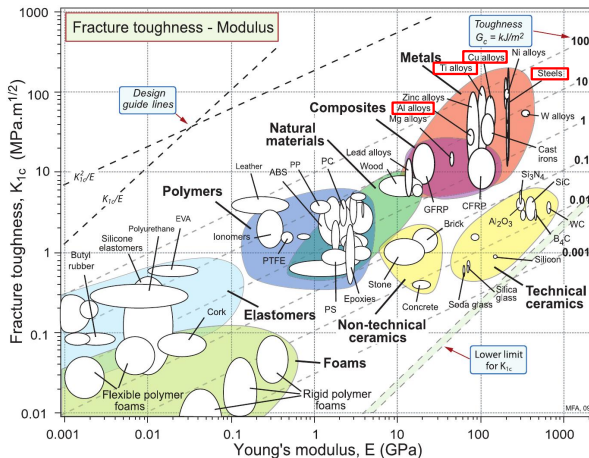
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- ▶ Huge effect of microstructure and defects.
- ▶ Highly sensitive to composition and process.

Toughness



Source : www.grantadesign.com/education/resources

► Huge effect of microstructure and defects.

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