## Ultrasonic non destructive testing advance lecture

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## Content

- Element of acoustic
- Few words on piezoelectricity
- US transducer.
- Applications:
  - Medicine
  - High temperature US characterization
  - Reverberation

## **Element of acoustic and piezoelectricty**

ElyT School Guy Feuillard

- Outline
  - Acoustic waves in fluids
  - One dimensional acoustic waves
  - Fundamental laws of acoustics
  - Energy and acoustics
  - Transmission and reflexion

## Acoustic waves

The wave vector 
$$\vec{k} = \frac{\omega}{c} \mathbf{u}$$

Bulk waves



Longitudinal waves : Displacement // propagation (fluids & solids)



Transverse waves Displacement ⊥ propagation (solids only)

## Ultrasonic celerity

In solids

$$c = \sqrt{\frac{1}{\rho_0 \chi}}$$
 In fluids

$$c_L = \sqrt{\frac{M}{\rho_0}}$$
$$c_T = \sqrt{\frac{G}{\rho_0}}$$

$$M = K + \frac{4}{3}G$$

Material	Density [Kg/m3]	Longitudinal celerity [m/s]	Shear velocity [m/s]
Air (0 degree)	1,293	331	
Air (20 degree)	1,20	344	
Alcohol	790	1207	
Water (pure)	998	1480	
Aluminum	2790	6320	3130
Steel	7800	5900	3200

### Waveform



### Mathematical expression of a plane wave



Progression d'un ébranlement. Repéré par le niveau u au point  $x_0$  et à l'instant  $t_0$ , l'ébranlement, se propageant à la vitesse c, atteint, à l'instant t, le point x tel que  $x = x_0 + c(t - t_0)$ .

$$x = x_0 + c(t - t_0)$$
  
$$x - ct = x_0 - ct_0 \text{ ou } t - \frac{x}{c} = t_0 - \frac{x_0}{c}$$

 $u(x,t) = F(t - \frac{x}{c}) = f((x - ct) \text{ Forward propagation x})$  $u(x,t) = G(t + \frac{x}{c}) = g((x + ct) \text{ Backward propagation x})$ 

Acoustic wave generated @ x=0

$$u_M = A \cos \omega t$$
 with  $\omega = \frac{2\pi}{T}$   
At a position x  
 $u(x,t) = A \cos \omega (t - \frac{x}{c})$ 

Usefull parameters:

$$\lambda = cT = \frac{c}{f}$$
 Wavelength  

$$k = \frac{2\pi}{\lambda} = \frac{\omega}{c}$$
 Wave number  $u = A\cos(\omega t - kx)$   
 $\varphi = \omega t - kx$  Phase

### Correspondance



## Complex notation $u_C = A e^{j(\omega t - \phi)}$ $v_C = Be^{j(\omega t - \psi)}$ $u = \Re e(u_C)$ $\frac{du_C}{dt} = j\omega u_C$ $\frac{du_C}{dx} = -jku_C$ derivative $A^2 = u_C u_C^*$ modulus $\langle u(t)v(t)\rangle = \frac{1}{2}(u_C.v_C^*)$ Mean value

Exercice : demonstrate the relation above

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One dimensional equations of acoustic





# Fundamental laws wave propagation in a perfect, non turbulent fluid



P, pressure

 $\dot{v}$  Particle velocity

 $\rho$ , density

F an external force an q an acoustic source

 $P, \dot{v}, \rho$ 

Relations betweeen these 3 variables and the sources ?

Hypothesis :

: -small acoustic perturbations -Adiabatic phenomenon



3 unknown



3 équations

Linear acoustic equations

$$P = c^{2}\rho$$

$$\rho_{0} \frac{d\dot{v}}{dt} = -grad(P) + \rho_{0} \overset{\mathsf{r}}{F}$$

$$\frac{\partial \rho}{\partial t} + \rho_{0} div(\vec{v}) = \rho_{0}q$$

State	(1)
Euler	(2)
Mass	(3)

Rq: 
$$\dot{v} = -grad(\phi) + rot(\psi)$$
  
Vortex potential (div v =0)  
Velocity potential (rot v =0)  
Velocity potential (rot v =0)

No vortex

Wave equation

$$\begin{cases} \Delta P - \frac{1}{c^2} \frac{\partial^2 P}{\partial t^2} = \rho_0 (div(\vec{F}) - \frac{\partial q}{\partial t}) & \text{Exercises} \\ \Delta \vec{v} + rot \ rot \ \vec{v} - \frac{1}{c^2} \frac{\partial^2 \vec{v}}{\partial t^2} = grad \ q - \frac{1}{c^2} \frac{\partial \vec{F}}{\partial t} \end{cases}$$

φ gives v et P

Exercice : with eq 1,2,3 show that we obtain these wave equations

I I I Very complicated if

$$\vec{v} = -grad(\phi)$$
 then  
 $\vec{F} = -grad(U)$ 

$$\Delta \phi - \frac{1}{c^2} \frac{\partial^2 \phi}{\partial t^2} = -q + \frac{\partial U}{\partial t}$$
$$P = \rho_0 \frac{\partial \phi}{\partial t} - \rho_0 U \qquad \text{Euler}$$

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### Without sources



General form

$$\phi(x,t) = F(t \pm \frac{x}{c}) = f((x \pm ct))$$

Exo : demonstrate that the above form is solution

For a plane wave propagating in the x direction

$$\rho_0 \frac{d\vec{v}}{dt} = -grad(P)$$

$$v_{x} = V_{M}e^{j(\omega t - kx)} \quad \text{Toward } x > 0$$
  

$$j\omega\rho_{0}v_{x} = -\frac{\partial P}{\partial x} = jkP = j\frac{\omega}{c}P$$
  

$$P = \rho_{0}cv_{x}$$

### **Energy considerations**

Kinetic energy density  $E_C = \frac{1}{2}\rho_0 v^2$  [J/m3]

$$dW = -PdV$$

Remember the state equation

Per vol unit

$$dE_{P=}\frac{dW}{V} = P\frac{d\rho}{\rho_0} = \frac{c^2}{\rho_0}\rho d\rho$$
$$E_P = \frac{1}{2}\frac{c^2}{\rho_0}\rho^2 = \frac{1}{2}\frac{P^2}{\rho_0}$$

[J]

 $P = c^2 \rho$ 

then

$$E_P = \frac{1}{2} \frac{c^2}{\rho_0} \rho^2 = \frac{1}{2} \frac{P^2}{\rho_0 c^2}$$

Energy density (J/m3) :

$$E_I = E_C + E_{P=} \frac{1}{2}\rho_0 v^2 + \frac{1}{2}\frac{P^2}{\rho_0 c^2}$$
 In J/m3

### Acoustic intensity:

$$v = V_m \sin(\omega t - kx) P = P_m \sin(\omega t - kx)$$

The acoustic intensity is I = Pv in  $W/m^2$ 

$$I = P_m V_m \sin^2(\omega t - kx)$$
$$\langle I \rangle = \frac{P_m V_m}{2}$$
Harmonic regime
$$\tilde{v} = V_m e^{i(\omega t - kx)} \qquad \tilde{P} = P_m e^{i(\omega t - kx)}$$

Complex quantities contain information on the magnitudes and phases of the wave.

Average Intensity

$$\langle I \rangle = \frac{\tilde{P}\tilde{v}^*}{2}$$

### Rq 1: acoustic impedance

$$Z = \frac{P}{v} = |Z|e^{j\phi}$$

For a plane wave

 $Z = \rho_0 c$  Acoustic impedance in kg m<sup>-2</sup> s<sup>-1</sup> Or Rayl (Lord Rayleigh)

Rq 2: 
$$E_I = E_C + E_{P=} \frac{1}{2} \rho_0 v^2 + \frac{1}{2} \frac{P^2}{\rho_0 c^2}$$

$$E_{I} = \frac{1}{2}\rho_{0}\nu^{2} + \frac{1}{2}\frac{P^{2}}{\rho_{0}c^{2}} = \frac{1}{2c}\frac{P^{2}}{Z} + \frac{1}{2c}\frac{P^{2}}{Z} = \frac{P^{2}}{cZ}$$

$$\langle I \rangle = \frac{Pv^*}{2} = \frac{1}{2}Zv^2 = \frac{1}{2}\frac{P^2}{Z} = cE_I$$

RMS pressure 
$$P_{rms} = \frac{P_m}{\sqrt{2}}$$
 RMS velocity  $v_{rms} = \frac{v_m}{\sqrt{2}}$   
 $E_I = \rho_0 v_{rms}^2 + \frac{P_{rms}^2}{\rho_0 c^2}$ 

### P and v are conjugated variables like U et I in electricity



### Order of magnitude

Audible soundsAir:
$$\rho=1,28 \text{ kg/m3}$$
 $c=340 \text{ m/s}$  $Z=440 \text{ Rayl}$ 

Limit of sensitivity of the human ear  $10^{-12}$  W/m<sup>2</sup> or P<sub>r</sub> = 2 10<sup>-5</sup> Pa à 1 kHz

$$I_{dB} = 10\log_{10}\frac{I}{I_s}$$
 ou  $I_{SPL} = 20\log_{10}\frac{P_{eff}}{P_r}$ 

Quite house air sound 40 à 50 dB Conversation : 60 dB soit 10<sup>-6</sup> W/m<sup>2</sup> concert: 80 à 90 dB aircraft: 120 dB threshold of pain



Exercice : Calculate the mean displacement and velocity f = 1 kHz I = 60 dB, in air

In  $W/m^2$   $\langle I \rangle = 10^{-6}/10^{-12}$ 

The complex particle velocity is  $v = V_m e^{i(\omega t - kx)}$ , `In air  $Z = \rho_0 c = 440 \text{ Rayl}$  and thus the intensity is :  $\langle I \rangle = \frac{1}{2} Z v^2 = \frac{1}{2} Z V_m^2$ 

The particle velelocity is

$$V_m = \sqrt{\frac{2\langle I \rangle}{Z}} = \sqrt{\frac{2 * 10^{-6}}{440}} = 67 \ \mu m/s$$
$$U_m = \frac{V_m}{\omega} = \frac{V_m}{2\pi f} = 10 \ nm!!!$$

In water Calculate the mean displacement and velocity  $f = 5 \text{ MHz I} = I = I_{max} = 100 \text{ mW/cm}^2 \text{ in water}$ Density  $\rho = 1000 \text{ kg/m}3$  Celerity c = 1500 m/s

$$V_m = 3.6 \ cm/s$$
$$U_m = 1.2 \ nm$$

### Transmission and reflexion (plane waves)

### Normal incidence



Reflexion coefficient

$$r = \frac{p_r}{p_i}$$

**Transmission Coefficient** 

$$t = \frac{p_t}{p_i}$$

En x = 0 : continuity equations  $p_i + p_r = p_t$   $v_i + v_r = v_t$ With  $p = \pm Zv$ Depending on the direction

 $\frac{p_i}{Z_1} - \frac{p_r}{Z_1} = \frac{p_t}{Z_2}$ 

Amplitude transmission coeffcient

$$r = \frac{Z_2 - Z_1}{Z_2 + Z_1} \qquad t = \frac{2Z_2}{Z_2 + Z_1}$$

Energy transmission coefficient



with: R+T=1 energy is conservative

Exercice: Determine the transmission coefficient between air and water

In air Z = 440 Rayl in water  $Z = 1.5 \ 10^6 Rayl$  thus R = 0.9988 and T = 0.0012In dB, the attenuation due tu transmission is close to 30 dB

### Oblique incidence



Exemple : propagation through a rigid wall surface density  $\mu$  in kg/m<sup>2</sup> Normal incidence

$$Z_{1} = \rho_{1}c_{1}$$

$$Z_{1} = \rho_{1}c_{1}$$

$$V_{i} + v_{r} = v_{t}$$

$$\frac{p_{i}}{Z_{1}} - \frac{p_{r}}{Z_{1}} = \frac{p_{t}}{Z_{2}} = v(t)$$

$$p_{i} = P_{i}e^{j(\omega t - k_{1}x)}$$

$$p_{r} = P_{r}e^{+j(\omega t + k_{1}x)}$$

$$x(t) = 0$$
If  $Z_{1} = Z_{2}$ 

$$Dynamic equation$$

$$p_{i} + p_{r} - p_{t} = \mu \frac{dv(t)}{dt}$$

For a sinusoidal wave

$$p_i + p_i - p_t - p_t = \mu \frac{dv(t)}{dt} = j\omega\mu\frac{p_t}{Z_1} \qquad p_i - p_t = j\frac{\omega\mu}{2}\frac{p_t}{Z_1}$$



Numerical application Concrete wall: e = 10 cm,  $\rho = 2600 \text{ kg/m}^3 => \mu = 260 \text{ kg/m}^2$ 

T = 46 dB à 100 Hz



Attenuation due to viscosity.  $\eta$ ,  $\mu$ 

Dynamic equation

$$\rho_0 \frac{d\vec{v}}{dt} = -grad(P) + (\eta + \frac{4}{3}\mu)\Delta\vec{v} \qquad \text{i.e} \qquad \frac{d^2\vec{u}}{dt^2} = c^2\Delta\vec{u} + \frac{1}{\rho_0}(\eta + \frac{4\mu}{3})\Delta\frac{d\vec{u}}{dt}$$

Harmonic regime 
$$u_x = U_M e^{j(\omega t - kx)}$$

$$\frac{d^{2}\vec{u}}{dt^{2}} = (c^{2} + j\omega\frac{1}{\rho_{0}}(\eta + \frac{4\mu}{3}))\Delta\vec{u}$$

Complex celerity

$$c^{2^{*}} = c^{2}(1 + j\omega \frac{1}{\rho_{0}c^{2}}(\eta + \frac{4\mu}{3})) \quad \text{First order dev.} : c = c(1 + j\omega \frac{1}{2\rho_{0}c^{2}}(\eta + \frac{4\mu}{3}))$$

Complex wave number

$$k^{*} = \frac{\omega}{c^{*}} = \frac{\omega}{c} (1 - j\omega \frac{1}{2\rho_{0}c^{2}} (\eta + \frac{4\mu}{3}))$$
<sup>29</sup>

Expression of the particule displacement

$$u_{x} = U_{M}e^{j(\omega t - k^{*}x)} \qquad \text{Soit} \qquad u_{x} = U_{M}e^{j(\omega t - \frac{\omega}{c}x)}e^{-\alpha x}$$
Attenuation coefficient Propagation Attenuation
$$\alpha = \frac{\omega^{2}}{2\rho_{0}c^{3}}(\eta + \frac{4\mu}{3})x \qquad \text{Neper/m} \quad \text{In dB} \qquad \begin{array}{l} A(dB) = 20\log_{10}(e^{-\alpha x}) = 8.686\alpha x \\ A(dB) = 8,686\frac{\omega^{2}}{2\rho_{0}c^{3}}(\eta + \frac{4\mu}{3})x \end{array}$$

Attenuation proportionnal to the square frequency

Other causes : thermal conductivity Molecular relaxation



Attenuation in air in dB/m at 1 kHz, 1 MHz,  $\mu = 1.910-5, \eta = 0.6\mu$ 

What is the viscous interaction length?

$$\alpha = \frac{\omega^2}{2\rho_0 c^3} (\eta + \frac{4\mu}{3}) x$$



(a) 1 kHz  $\delta = 150 \ km!!$ (a) 1 MHz  $\delta = 0.15 \ m$ 

Fig. 7.3. Absorption of sound in air at 20°C as a function of frequency. (After Bass, et al.)

## Attenuation in liquids $\eta \ll \mu$

$$\alpha \approx \frac{\omega^2}{\rho_0 c^3} \frac{2\mu}{3} x$$
 In Neper

$$\alpha_{water} = 0.22 \text{ dB/m}$$



**Fig.** 7.5. Sound absorption in freshwater and in seawater (35 ppt salinity) at 5°C and 1 atm. (According to Fisher and Simmons.)

## Conclusion

- Some concepts have been defined such as wave characteristics, acoustic impedance, transmission reflexion coefficients, attenuation factor...
- These concepts are essentials understand the interaction of a wave with mater, it is essential to know the essential characteristics of the wave celerity attenuation.
- We will use these concept to understand the electroacoustic behavior of a transducer and the wave interaction with materials

# Few words on Piezoelectricity

Définition Material properties Ferroelectric materials The piezoelectricity is the property of several materials that are able to generate an electric charge when mechanically deformed. Conversely, when an external electric field is applied to piezoelectric materials they mechanically deform.



### Direct effet

# Mechanical to electrical energy conversion and conversely



actuators



Mechanical displacement

Inverse effet

## Discovery of the piezoelectric effect





charges under mechanical deformation





## Discovery of the piezoelectric effect





## Fisrt World War 1916: ultrasonic transmission using

### Quartz crystal

Work commissioned by the Anti-Submarine Division, in a joint research effort by the French, British and American lead to the development of early sonar (ASDIC)





Quartz Transducer sandwich type h (A. B. Wood, A Textbook of Sound (1932))



6164\_\_NoiseCollector\_\_jillys\_sonar.wav

6165\_\_NoiseCollector\_\_jillys\_son<sup>40</sup>2.wav

## World War II & beyond

The origin of the high dielectric constant in barium titanate was discovered to be a result of its ferroelectric properties



XCVI. Theory of Barium Titanate.-Part I.

By A. F. DEVONSHIRE, H. H. Wills Physical Laboratory, University of Bristol\*.

[Received July 26, 1949.]

#### SUMMARY.

The theory of the dielectric and crystallographic properties of barium titanate is considered. By expanding the free energy as a function of polarization and strain and making reasonable assumptions about the coefficients, it is found possible to account for the various crystal transitions. Calculations are made of the dielectric constants, crystal stains, internal energy, and self polarization as functions of temperature. Finally relations are obtained between the coefficients in the free energy and the ionic force constants. These are used to estimate some of the coefficients which are not completely determined by experimental data.

### High dielectric constant ceramics

A. von Hippel, R. G. Breckenridge, F. G. Chesley, and Laszlo Tisza

LABORATORY FOR INSULATION RESEARCH, MASSACHUSETTS INSTITUTE OF TECHNOLOGY, CAMBRIDGE, MASS.

Results of an investigation are presented in this paper on titanium dioxide and the alkaline earth titanates, including some mixtures and solid solutions of the barium and -trontium compounds. Dielectric measurements over a wide range of frequencies, temperatures, and voltages, and thermal expansion and x-ray studies have yielded a rather complete picture of the properties and usefulness of these titania ceramics. Barium titanate and the barium-strontium titanate solid solutions prove to be a new class of ferroelectric materials. Their peculiar dielectric behavior was first noted by the Titanium Alloy Manufacturing Company, and this behavior proves to be connected with a lattice transition from pseudocubic to cubic. Additional maxima have been found in the dielectric characteristics which correspond to transitions of the second order. These maxima are being studied further.

A complete theory predicting the structural phase transitions in BaTiO<sub>3</sub> was proposed by Devonshire

## Why in several materials

Piezoelectricity appears in non centro symetrical crystals



# Example: Quartz crystal charges appear on top and bottom faces



## The ferroelectricity and the Piezoelectricity barium titanate ceramics



Before polarisation





## The development of ceramics

In 1949 a US patent was filed by Erie Resistor Corporation, for a piezo transducer that used the first poled ceramic samples.





INVENTOR

Ralph Hamma

### UNITED STATES PATENT OFFICE

2,486,560

TRANSDUCER AND METHOD OF MAKING THE SAME

Robert B. Gray, Eric Pa., assignor to Eric Resistor Corporation, Eric, Pa., a corporation of Pennsylvania

Application September 20, 1946, Serial No. 698,374

15 Claims. (CL 171-327)

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## PZT and PLZT ceramics

- $Pb[Zr_{x}Ti_{1-x}]O_{3} (0 \le x \le 1) \& Pb_{1-x}La_{x}(Zr_{y}Ti_{1-y})_{1-x/4}O_{3}$
- Higher electromechanical coupling
- Higher TC values, resulting in higher operational and processing temperatures
- Easily poled for applications, versatility
- Possess a wide range of dielectric constants across the phase diagram



Hans Jaffe (far right)

PZT ceramics (www.fujicera.co.jp)

## New technological processes Enhancement of the performances

1978 : composites materials R.E. Newnham, D.P. Skinner, L.E. Cross, **Connectivity and piezoelectric-pyroelectric composites**, *Materials Research Bulletin*, *Volume 13*, *Issue 5*, *May 1978*, *Pages 525-536* 

90 Piezoelectric single crystals with giant properties

Jun Kuwata, Kenji Uchino, and Shoichiro Nomura, **Phase Transitions in the Pb(ZnlnNbm)O,-PbTiO, System**, *Ferroelecrrics, vol. 37, pp. 579-582, 1981* T. R. Shout, Z.P. Chang, N. Kim and S. Markgraf, **Dielectric Behavior of single Crystals Near the (1 x)Pb(Mg1/3Nb2/3)03 (x)PbTi03 Morphotropic Phase Boundary**, *Ferroelectr. Let., vol. 12, pp. 63-69, 1990*.



http://www.ndt.net/article/v06n08/fleury/fig1.gif



### 2000 : lead free ceramics

### Published Items in Each Year



### DIRECTIVE 2002/95/EC OF THE EUROPEAN PARLIAMENT AND OF THE COUNCIL

of 27 January 2003

on the restriction of the use of certain hazardous substances in electrical and electronic equipment

### Accelerometers.

 Flow meters: Blood, industrial processes, waste

water.

• Medical: Imaging, HIFU, IVUS, surgical knives,

and cleaning of blood veins.

• Underwater acoustics: echosounders, sonar

systems, fish-finders, seabed mapping.

 Industrial sensors based on ultrasound: Level

control, detection, and identification.

• Hydrophones: Seismic, biologic, military, underwater communication.

Inkjet printheads.

· Dental work: Removal of plaque.

 Alarm systems: Movement detectors, broken

window sensors.

• NDT: Transducers for Non Destructive Testing.

Musical instrument pickups.

Acoustic emission transducers.

Actuators.

• Micro positioning devices: Optics, scanning tunneling microscopes.

 Surface Acoustic Waves: Personal Computer touch

screens, filters.



## Material and properties

## Fabrication process of ceramics

## Powder



http://www.ferroperm-piezo.com/

## Piezo ceramics



### **Mains characteristics**

- •High stress
- •Linear response
- •Small deformations

Piezo oefficient= 100 pC/N thickness= 1 mm Volatge = 10 V

displacement $\Delta l=1 nm !$ 

## Some properties

Electrical

# Piezoelectric material are insulators : caracterised by their ability to accumulate charges



ε dielectric constant



In a conducting metal electrons are free In a insultator In V/C Electrons are located on electrodes

### Mechanical Elasticity or stifness



http://www.insep.fr/FR/Sports/Gymnastique/PublishingImages/gymnastique.jpg

### c coefficient



http://www.unilim.fr/theses/2003/sciences/2003limo 0004/images/figurevi1.jpg

## In Newton per m<sup>2</sup>

## Electromechanical Ability to accumulate charges for a given force



http://www.piezotest.com/d33piezometer.htm



http://www.kcftech.com/products/documents/PM3001.manual.pdf

### d coefficient

## In Coulomb per Newton or m/Volt

## Electromechanical coupling coefficient

The electromechanical coupling factor, k, of piezoelectric materials, determines the conversion efficiency of mechanical to electrical energy or electrical to mechanical energy.



The coupling factor, k, is associated with a vibration mode and thus do not have a unique expression, k is always bellow 1

## Properties

Material	piezo. Coef. d <sub>33</sub> (10 <sup>-12</sup> m/V)	Relative Permittyvity	Stiffness coef. (10^9N/m²)	Density kg/m3	Thicness coupling coef. (%)
Quartz [1]	2,3	4,5	80	2650	10
Barium Titanante (T57) [2]	105	700	112	5300	40
Lead Titanate (PZ34) [3]	50	210	140	7550	40
Lead Titanate Ziconate (PZ27) [3]	425	1800	113	7700	60
Piezo Polymers	26 [4]	5 [5]	10 [5]	2500 [5]	25 [5]

[1]	Morgan Matroc
[2]	Quartz et Silice
[3]	Ferroperm
[4]	Sasaki <b>ISSN</b> 0386-2186
[5]	Feuillard, thèse de doctorat

## Conclusions

•Piezoelectric materials are used as sensor, actuators or transducers in many applications .

•Covered field : microsystem, microelectronics medicine nuclear or aeronautics.

•Very often hidden but essential in many applications

- Piezo materials are known ...
- We focused mainly in transducer but they are used in many application
- Now it is time to see how we can use them to make transducers and to produce images...

• To be continued...

## Thank you !